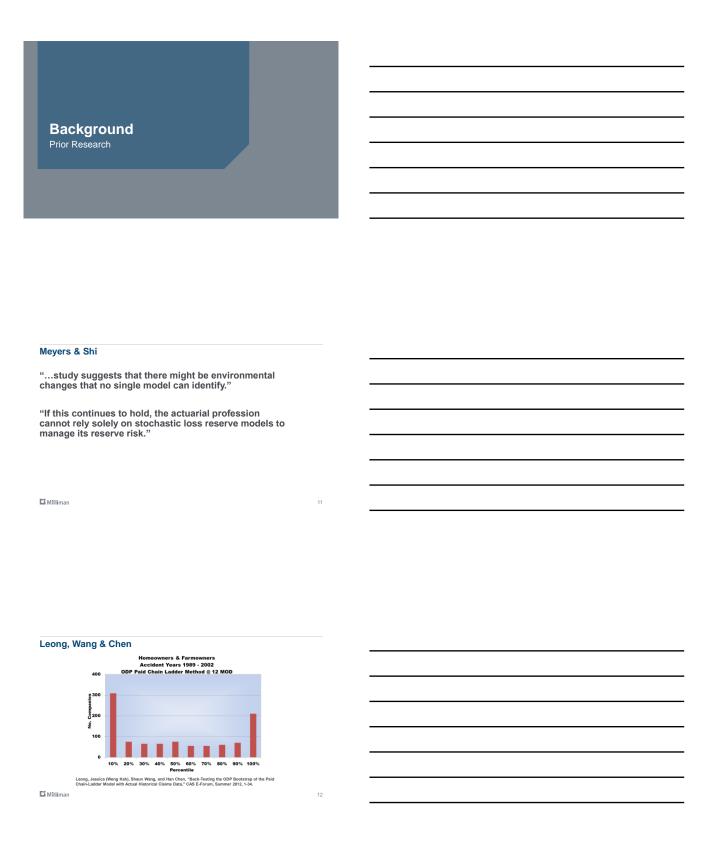


Benchmarking Unpaid Claim Estimates Outline	
1 Background	
2 Analysis Summary	
3 Model Limitations	
4 Model Projections – Are they Unbiased?	
5 Proposed Adjustments	
6 Conclusions	
7 Claim Variability Guidelines	
Li Milliman 4	
Background	
Hindsight Analysis	
Hypothetical Unpaid Claim Distribution	
Distribution of Possible Outcomes	
Actual "Hindsight" Unpaid = \$92 (77 th Percentile)	
(77 th Percentile)	
Mean — Me	

If Model is Correct... 180 180 140 120 100 80 60 40 20 Milliman If Model Underestimates Distribution... 180 160 140 120 100 80 Milliman If Model Overestimates Distribution... Sample Line of Business bution too Wide (Overpredicted) Sample Evaluation Period Accident Year Analysis

□ Milliman



Large Way 9 Ohan		
Leong, Wang & Chen		
"the popular ODP bootstrap of the paid chain-ladder method		
is underestimating reserve risk."		
"the bootstrap model does not consider systemic risk, or, to put it another way, the risk that future trends in the claims		
environment - such as inflation, trends in tort reform,		
legislative changes, etc. – may deviate from what we saw in the past."		
Leong, Jessica (Weng Kah), Shaun Wang, and Han Chen, "Back-Testing the ODP Bootstrap of the Paid		
Leong, Jessica (Weng Kah), Shaun Wang, and Han Chen, "Back-Testing the ODP Bootstrap of the Paid Chain-Ladder Model with Actual Historical Claims Data," CAS E-Forum, Summer 2012, 1-34.	13	
Loong Wong & Chon		
Leong, Wang & Chen Workers' Compensation		
Accident Years 1989 - 2002 ODP Incurred Chain Ladder Method @ 12 MOD		
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50		
10% 20% 30% 40% 50% 60% 70% 80% 90% 100% Percentile Leona, Jessica (Wena Kah), Shaun Wana, and Han Chen. "Back-Testina the ODP Bootstrap of the Paid		
Leong, Jessica (Weng Kah), Shaun Wang, and Han Chen, "Back-Testing the ODP Bootstrap of the Paid Chain-Ladder Model with Actual Historical Claims Data," CAS E-Forum, Summer 2012, 1-34. Li Milliman	14	
Lagra Mana 9 Chan		
Leong, Wang & Chen		
"it appears that the incurred bootstrap model is also underestimating the risk of falling in these extreme		
percentiles."		
Note: This is not the same incurred ODP bootstrap model		
as described in the Shapland Monograph.		
Leong, Jessica (Weng Kah), Shaun Wang, and Han Chen, "Back-Testing the ODP Booststrap of the Paid Chain-Ladder Model with Actual Historical Claims Data," CAS E-Forum, Summer 2012, 1-34.		
Chain-Ladder Model with Actual Historical Claims Data," CAS E-Forum, Summer 2012, 1-34. Lä Milliman	15	

Gremillet & Miehe Total (CAL, PPAL, WC, Oth Liab) Accident Years 1989 - 1997 RJMCMC Stochastic Method @ 12/31/1997 120 **□** Milliman **Gremillet & Miehe** $\lq\lq\ldotp$...it is core to have adjustments by actuaries prior to running the stochastic methods 'automatically.' " "Actuary in the box" dream for stochastic reserves valuation not yet happening Milliman **Analysis Summary**

Comparison of Analyses

Item	Meyers & Shi	Shi Wang & Miehe Chen Miehe			
Data	50 Companies	21 (MPL) to 78 (PPAL) Companies	?	1,679 Companies	
Evaluations	1	11	5	9	
Models	2	2	3	8	
Lines of Business	1	9	4	16	
Triangle Sets	50	~4,950	296	30,707	

Analysis Details

- ODP Bootstrap
 - Paid Chain Ladder
 - Incurred Chain Ladder
 - Paid Bornhuetter-Ferguson
 - Incurred Bornhuetter-Ferguson
 - Paid Cape Cod
 - Incurred Cape Cod
 - Weighted
- Mack Bootstrap
 - Paid Chain Ladder

Milliman		

Analysis Details

- Beginning Data
- NAIC Schedule P 4,796 Companies (& Groups)
- Remove all triangles without 10 years of data (Paid, Incurred, etc.)
- Other data quality tests → "quality data"
- Test whether next 9 years are identical → "complete data"
- Test Data
- 2,104 Companies with at least 2 Schedule P LOBs of "quality data"
- Total of 75,000+ LOBs with "quality data"
- 1,679 Companies with at least 1 Schedule P LOB of "complete data"
- Total of 30,707 LOBs with "complete data"
- Approx. 27,000 LOBs with at least 2 for same Company

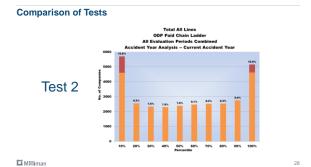
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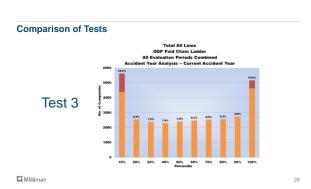
Analysis Details		
Model Output		
Accident Year Totals (by Year & All Years Combined)		
Calendar Year Totals (by Year)		
Calendar Year Runoff Totals (by Year)		
 Ultimate Loss Ratios (by Year) 		
Incremental Results (by Year and Development Period)		
Diagnostic Statistics		
™ Milliman	22	
WILLINGS	22	
Analysis Details		
, manyoto Bottano		
Model Options (Tests)		
Test 1 – Defaults		
No Tail factors (i.e., 1.000)		
■ BF – a priori based on hindsight L/R, No CoV		
 CC – Trend = 2.5%, Decay Ratio = 90% 		
 Test 2 – Selected Limiting of Incrementals 		
 Test 3 – Selected Limiting & Suggested 		
Heteroscedasticity Groups		
T Milliman	23	
Model Limitations		
Woder Limitations		

Model Limitations	
 Model Risk Limited to known data A single model can underestimate variability Systemic risk In addition to model risk 	
 A shift in claims environment Need to Understand Assumptions 	
Need to Oliderstand Assumptions	
Li Milliman 25	
Major Assumption	
Bootstrap models (ODP & Mack) assume Chain Ladder projections are unbiased	
™illiman 26	
	_
Model Projections	
Are they Unbiased?	

Total All Lines OP Paid Chain Ladder All Evaluation Periods Combined Accident Year Analysis – Current Accident Year Test 1 Test 1

Milliman



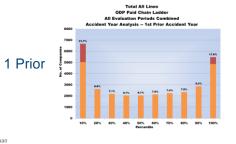


Current Cur

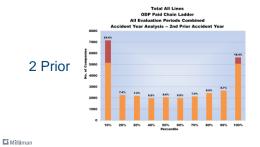
Comparison of Accident Years

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Comparison of Accident Years



Page 11 of 31

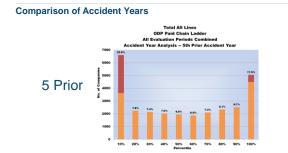
Operation of Accident Years Total All Lines OP Pald Chain Ladder All Evaluation Periods Combined Accident Year Analysis – 3rd Prior Accident Year 3 Prior

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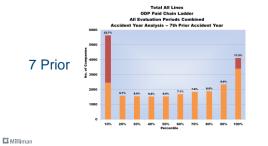
Comparison of Accident Years Total All Lines OP Paid Chain Ladder All Evaluation Perfords Combined Accident Year Analysis - 4th Prior Accident Year 4 Prior



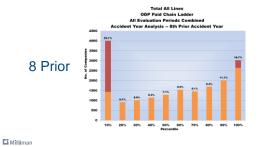
Comparison of Accident Years Total All Lines OP Paid Chain Ladder All Evaluation Periods Combined Accident Year Analysis - 6th Prior Accident Year

Comparison of Accident Years

Milliman



Comparison of Accident Years



Page 13 of 31

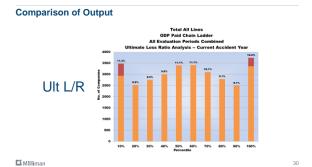
ACC Yr Total All Lines OP Pall Chain Ladder All Evaluation Periods Combined Accident Year Analysis - Current Accident Year

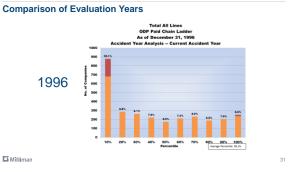
Comparison of Output

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Cal Yr Cal Yr Milliman

Cal Yr Runoff Total All Lines OP Paid Chain Ladder All Evaluation Periods Combined Calendar Year Runoff Analysis – 1st Calendar Year Runoff Total All Lines OP Paid Chain Ladder All Evaluation Periods Combined Calendar Year Ladder Year

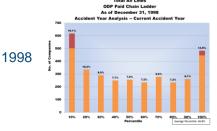




Comparison of Evaluation Years Total All Lines ODP Paid Chain Ladder As of December 31, 1987 Accident Year Analysis – Current Accident Year 1997 1

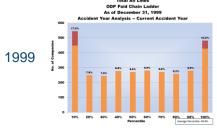
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Comparison of Evaluation Years



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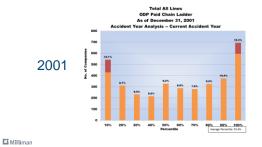
Comparison of Evaluation Years



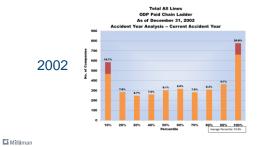
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Comparison of Evaluation Years

Milliman



Comparison of Evaluation Years



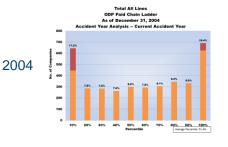
Page 17 of 31

Comparison of Evaluation Years Total All Lines OOP Paid Chain Ladder As of December 31, 2003 Accident Year Analysis – Current Accident Year

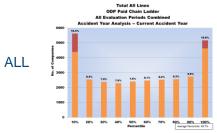
Comparison of Evaluation Years

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Comparison of Evaluation Years



□ Milliman

Incrementals Milliman **Comparison of Models** ODP Pd CL Milliman **Comparison of Models** Mack Pd CL

□ Milliman

Comparison of Models Total All Lines ODP Incurred Chain Ladder All Evaluation Periods Combined Accident Year Analysis – Current Accident Year ODP Inc CL Total All Lines ODP Incurred Chain Ladder All Evaluation Periods Combined Accident Year Analysis – Current Accident Year ODP Inc CL Total All Lines ODP Incurred Chain Ladder All Evaluation Periods Combined Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP Incurred Chain Ladder Accident Year Analysis – Current Accident Year ODP In

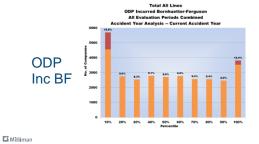
Comparison of Models

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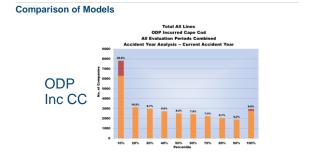
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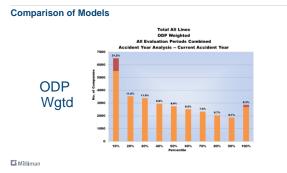
Comparison of Models

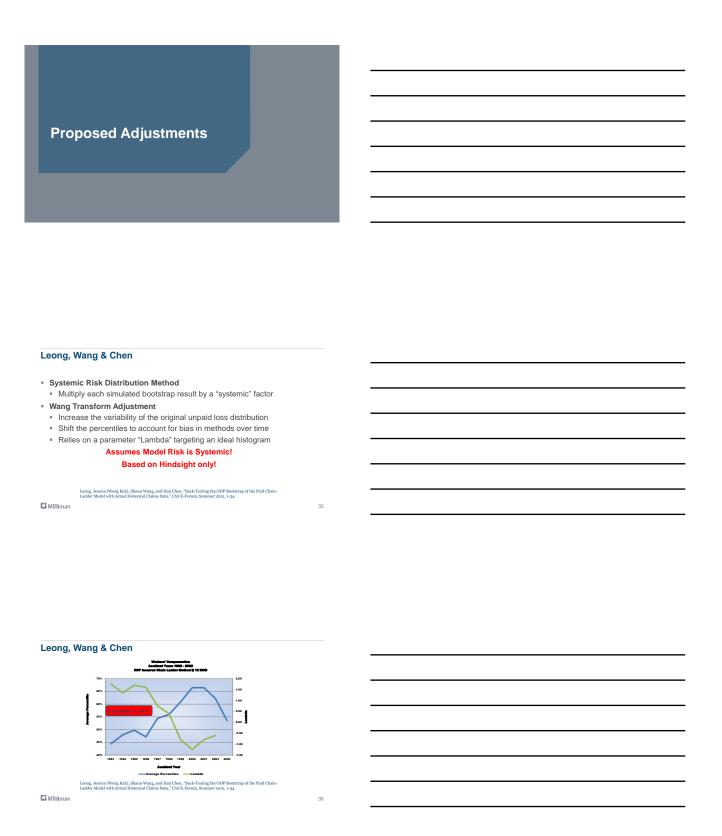


Comparison of Models Total All Lines OD Paid Cape Cod All Evaluation Periods Combined Accident Year Analysis - Current Accident Year Analysis - Current Accident Year Accident Year Analysis - Current Accident Year Analysis - Current Accident Year Accident Year Analysis - Current Accident Year Analysis - Curre



Milliman





HDR Adjustment

- Shift distribution by multiplying unpaid claim estimates by the HDR
- Coefficient of variation unchanged
- Additive shift will not address variance
- Hindsight adjustment, but we are not advocating, just testing how much bias vs. not enough variance

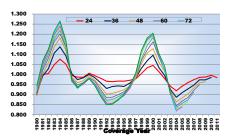
□ Milliman

Example - Coverage Year 2000 (\$B)

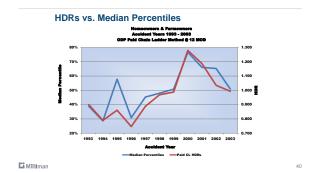


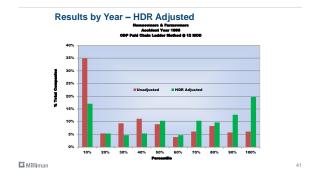
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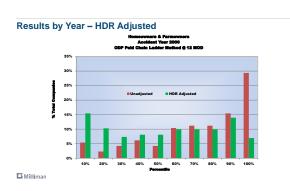
HDR by Evaluation Month



Milliman







Conclusions		
Contractions		
Conclusions		
Ocal of Ideal History Houselined by Brid Ol Bootston		
 Goal of Ideal Histogram Unrealized by Paid CL Bootstrap Both ODP Bootstrap and Mack Bootstrap 		
Confirms Other Research		
Other ODP Bootstraps – Much Closer to Theoretical Ideal		
Milliman Incurred models different (Shapland Monograph)		
Bornhuetter-Ferguson and Cape Cod models		
 Cyclical Bias in Reserve Distributions – Paid and Incurred 		
Consistent with Deterministic Projections		
™ Milliman	44	
Conclusions		
"Corrections" to Other ODP Models may be Unnecessary		
Addressing Model Risk is very important		
 Can't "blindly" accept model results Use diagnostics to assess model strengths / weaknesses 		
 Use diagnostics to assess model strengths / weaknesses Implications for weighting 		
Still need to address systemic risks		
 Guidelines (i.e., benchmarks) to Assess Results 		
Based on hindsight, but forward looking		
Correlations Distributions by LOB and Bramium		
■ Distributions by LOB and Premium	45	
	-	

Claim Variability Guidelines The Way Forward	
Claim Variability Guidelines Types of Benchmarks 1 Loss Development Patterns 2 Unpaid Claim Distributions	
Correlation Between Segments Li Milliman 47	
Claim Variability Guidelines Loss Development Patterns Back-testing output includes VWA factors for all paid data triangles Back-testing output includes VWA factors for simulated paid data Actual incurred data is part of the data set, but output for incurred simulations is not readily available	
By Schedule P Line of Business, a "distribution" of the patterns were created for both actual and simulated data Milliman 48	

Claim Variability Guidelines As an example of how you might use this information, suppose you are analyzing Commercial Auto data and have selected the following LDF pattern: **Claim Variability Guidelines** Overall the 71st percentile fit the best, but this varies by development age. Alternatively, the 55th percentile fits better in the early and later ages: **□** Milliman **Claim Variability Guidelines** Loss Development Patterns To develop a range, you could then calculate new unpaid claim estimates by selecting development patterns +/- 20% from the best fit:

□ Milliman

Claim Variability Guidelines

Unpaid Claim Distributions

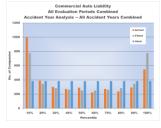
- For each Schedule P LOB, the back-testing results contain thousands of simulated distributions for companies of all different sizes
- Regression models were used to fit the distributions by premium volume for each of the Acc Yr, Cal Yr, Cal Yr Runoff, and Loss Ratio distributions
- Fitted results were smoothed to be consistent between distribution types and to conform with statistical properties

□ Milliman 5

Claim Variability Guidelines

Unpaid Claim Distributions

- Variance Adjustment Factors can be used to correct for back-testing results
- Separate variance adjustments factors for Loss Ratio distributions
- For example, this is the Acc Yr adjustment for Commercial Auto



□ Milliman

Claim Variability Guidelines

Unpaid Claim Distributions

□ Milliman

- The regression model adjusts assumptions to fit statistical properties.
- For example, consider smaller vs larger number of exposures:

Small Insurer								Large	Insurer		
Commercial Auto Liability Accident Year Guidelines (US\$ 000's)							Commercial . ent Year Gui				
Acc Yr					CoV						
2008	5,115	75.3%	17	63	369.8%	2008	40,918	75.3%	131	284	216.4%
2009	5,302	77.1%	42	112	268.7%	2009	42,415	77.1%	323	464	143.5%
2010	5,427	79.4%	95	203	213.1%	2010	43,419	79.4%	735	838	114.0%
2011	5,508	81.7%	196	308	157.3%	2011	44,064	81.7%	1,516	1,223	80.6%
2012	5,668	82.5%	404	498	123.4%	2012	45,343	82.5%	3,124	2,067	66.2%
2013	5,907	82.0%	820	737	89.9%	2013	47,256	82.0%	6,344	3,409	53.7%
2014	6,277	79.2%	1,532	1,019	66.5%	2014	50,215	79.2%	11,850	5,250	44.3%
2015	6,780	74.9%	2,719	1,640	60.3%	2015	54,236	74.9%	21,034	8,442	40.1%
2016	7,214	73.8%	4,278	2,401	56.1%	2016	57,710	73.8%	33,093	12,465	37.7%
Total	53,197	78.3%	10.102	3.654	36.2%	Total	425,576	78,3%	78.152	17.681	22.6%

Page 28 of 31

Claim Variability Guidelines Unpaid Claim Distributions

- The regression model allows for other customizations.
- For example, consider a faster development pattern:

	,	werage Di	CVCIOPITIC	110	r dater bevelopment							
		Commercial . ent Year Gui			Commercial Auto Liability Accident Year Guidelines (US\$ 000's)							
Acc Yr					CoV							
2008	20,459	75.3%	66	157	238.9%	2008	20,459	75.3%	2	25	1506.9%	
2009	21,207	77.1%	162	263	161.9%	2009	21,207	77.1%	18	79	430.9%	
2010	21,709	79.4%	369	475	128.6%	2010	21,709	79.4%	69	173	249.2%	
2011	22,032	81.7%	762	700	91.9%	2011	22,032	81.7%	275	360	131.0%	
2012	22,671	82.5%	1,570	1,171	74.6%	2012	22,671	82.5%	794	721	90.8%	
2013	23,628	82.0%	3,188	1,882	59.0%	2013	23,628	82.0%	2,029	1,320	65.0%	
2014	25,108	79.2%	5,954	2,832	47.6%	2014	25,108	79.2%	4,481	2,227	49.7%	
2015	27,118	74.9%	10,568	4,556	43.1%	2015	27,118	74.9%	8,926	3,945	44.2%	
2016	28,855	73.8%	16,627	6,715	40.4%	2016	28,855	73.8%	15,589	6,351	40.7%	
Total	212,788	78.3%	39,266	9,666	24.6%	Total	212,788	78.3%	32,182	8,202	25.5%	
P-F												

Claim Variability Guidelines

Unpaid Claim Distributions

- The regression model accommodates international use.
- For example, consider a European insurer with the same development pattern:

US Insurer							European insurer							
Commercial Auto Liability Accident Year Guidelines (US\$ 000's)							Commercial Auto Liability Accident Year Guidelines (€ 000's)							
Acc Yr					CoV									
2008	20,459	75.3%	66	157	238.9%	2008	20,459	75.3%	66	161	244.5%			
2009	21,207	77.1%	162	263	161.9%	2009	21,207	77.1%	163	271	166.4%			
2010	21,709	79.4%	369	475	128.6%	2010	21,709	79.4%	370	489	132.2%			
2011	22,032	81.7%	762	700	91.9%	2011	22,032	81.7%	763	722	94.7%			
2012	22,671	82.5%	1,570	1,171	74.6%	2012	22,671	82.5%	1,572	1,205	76.6%			
2013	23,628	82.0%	3,188	1,882	59.0%	2013	23,628	82.0%	3,191	1,926	60.4%			
2014	25,108	79.2%	5,954	2,832	47.6%	2014	25,108	79.2%	5,961	2,884	48.4%			
2015	27,118	74.9%	10,568	4,556	43.1%	2015	27,118	74.9%	10,581	4,638	43.8%			
2016	28,855	73.8%	16,627	6,715	40.4%	2016	28,855	73.8%	16,647	6,834	41.1%			
Total	212,788	78.3%	39,266	9,666	24.6%	Total	212,788	78.3%	39,313	9,870	25.1%			
P.	Milliman										56			

Claim Variability Guidelines

Unpaid Claim Distributions

		Commercial Auto Liability Accident Year Guidelines (US\$ 000's)						Commercial Auto Liability Calendar Year Guidelines (US\$ 000's)						
	Acc Yr	Premium	L/R	Mean	Std Dev	CoV	CallYr	Premium	L/R	Mean	Std Dev	CoV		
	2008	20,459	75.3%	66	157	238.9%	2017	212,788	78.3%	16,042	4,772	29.7%		
	2009	21,207	77.1%	162	263	161.9%	2018	192,329	78.6%	10,398	3,655	35.2%		
cc Yr	2010	21,709	79.4%	369	475	128.6%	2019	171,122	78.8%	6,136	2,665	43.4%	Cal Yr	
56 11	2011	22,032	81.7%	762	700	91.9%	2020	149,412	78.7%	3,337	1,943	58.2%	Cai II	
	2012	22,671	82.5%	1,570	1,171	74.6%	2021	127,380	78.2%	1,716	1,274	74.3%		
	2013	23,628	82.0%	3,188	1,882	59.0%	2022	104,709	77.2%	879	882	200.4%		
	2014	25,108	79.2%	5,954	2,832	47.6%	2023	81,081	75.9%	435	599	137.5%		
	2015	27,118	74.9%	10,568	4,556	43.1%	2024	55,973	74.3%	224	358	159.8%		
	2016	28,855	73.8%	16,627	6,715	40.4%	2025	28,855	73.8%	99	227	230.0%		
	Total	212,788	78.3%	39,266	9,666	24,6%	Total			39,266	9,666	24,6%		
	Commercial Auto Liability						Commercial Auto Liability Loss Ratio Guidelines (US\$ 000's)							
		Calendar Year Runoff Guidelines (US\$ 000's)												
	Call Yr End		L/R	Mean	Std Dev	CoV	Acc Yr	Premium		Mean	Std Dev	CoV		
	2016	212,788	78.3%	39,266	9,666	24.6%	2007	19,719		73.8%	10.1%	13.6%		
	2017	192,329	78.6%	23,224	6,788	29.2%	2008	20,459		75.3%	10.7%	14.2%		
al Yr	2018	171,122	78.8%	12,826	4,679	36.5%	2009	21,207		77.1%	11.4%	14.8%	Loss Ra	
	2019	149,412	78.7%	6,690	3,166	47.3%	2010	21,709		79.4%	12.2%	15.3%		
unoff	2020	127,380	78.2%	3,353	2,033	60.6%	2011	22,032		81.7%	12.1%	14.9%		
	2021	104,709	77.2%	1,637	1,316	80.4%	2012	22,671		82.5%	13.7%	16.6%		
	2022	81,081	75.9%	758	831	109.6%	2013	23,628		82.0%	13.5%	16.4%		
	2023	55,973	74.3%	323	459	142.1%	2014	25,108		79.2%	13.6%	17.2%		
	2024	28,855	73.8%	99	227	230.0%	2015	27,118		74.9%	13.8%	18.4%		
	ın						2016	28.855		73.8%	15.4%	20.9%		

Claim Variability Guidelines Unpaid Claim Distributions In Excel, these are easy to graph: Acc Yr Cal Yr Loss Ratio Milliman **Claim Variability Guidelines** Back-testing output includes correlation statistics between all pairs of LOBs within a company (i.e., if there was more than one 'complete' LOB) Output includes both paid and incurred, before and after optimal hetero adjustments The mean and std dev (unweighted and weighted) for all specific pairs (i.e., between two specific LOBs) was measured Milliman **Claim Variability Guidelines** Correlation Between Segments • For example, consider the weighted results for 5 LOBs using 1996 data: Standard Deviations Counts **□** Milliman

Claim Variability Guidelines

Other Potential Uses

- Creating aggregate distributions for guidelines at the company level
- Calculating average durations for future cash flows
- Calculating reserve risk margins based on the expected unpaid claim runoff
- Assessing the variance parameter for a priori loss ratio assumptions in models
- Other uses which are only limited by your imagination

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