

Correlations between insurance lines of business: An illusion or a real phenomenon?

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- 1 Introduction
- 2 What are we measuring?
- 3 A play of hide and seek
- 4 Some examples based on real data
- 5 Modelling the past vs Forecasting the future
- 6 Some conclusions

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Background

Linkage Project grant awarded by the **Australian Research Council**

- Subject: “Modelling claim dependencies for the general insurance industry with economic capital in view. . .
- Term: 3 years +
- Collaborative between, and jointly funded by Government, industry (Allianz, IAG, Suncorp) and UNSW
- This presentation relates to one of the projects funded by the Linkage Project grant.

Paper in May 2016 issue of the ASTIN Bulletin.

Accepted manuscript can be downloaded from UNSWorks.

<http://bit.ly/1Ob9Y7B>

Dependency between lines of business (LoBs)

- Relevant to **diversification**, as it affects:
 - Risk margins
 - Capital margins
- Risk margins
 - V@R 75%: centre of distribution: **(Pearson) correlation** a reasonable measure of dependency
 - V@R 99.5%: right tail of distribution: correlation unlikely to be helpful, some measure of **tail dependency** more useful
 - This presentation concerned with correlation and risk margins

Notation

We focus on claims triangles:

- Claim array Δ for LoB n
 - Same shape Δ for all n
- Observation in (k, j) cell of Δ is $Y_{kj}^{(n)}$
- $R_{kj}^{(n)}$ is the standardised residual associated with $Y_{kj}^{(n)}$

Pearson correlation (between claim arrays of two LoBs)

- Well known definition

$$r^{(n_1, n_2)} = \frac{T^{-1} \sum_{k, j \in \Delta} \left(R_{kj}^{(n_1)} - \bar{R}^{(n_1)} \right) \left(R_{kj}^{(n_2)} - \bar{R}^{(n_2)} \right)}{S^{(n_1)} S^{(n_2)}}$$

Where

- T = number of observations in Δ
- $\bar{R}^{(n)}$ = mean of the residuals
- S^n = sample standard deviation of the residuals $R_{kj}^{(n)}$

Note: This definition can be improved to allow for different expected volumes in each cell (see paper)

Cross-LoB correlations: “conventional wisdom”

- In the Australian context, published papers on numerical values of cross-LoB correlations are:
 - Bateup & Reed (2001)
 - Collings & White (2001)
- Some insurers may rely on other proprietary work, but the above papers form, in some sense, an industry benchmark

Cross-LoB correlations: “conventional wisdom” (continued)

- The example contains some large correlations
 - Many of 0.4 or more
 - Up to a maximum of 0.75
- We do not assert that these correlations are wrong
- Rather that they should be **model dependent**
 - And we consider how changing the model might change the correlations that should be incorporated in these triangles

1 Introduction

2 What are we measuring?

3 A play of hide and seek

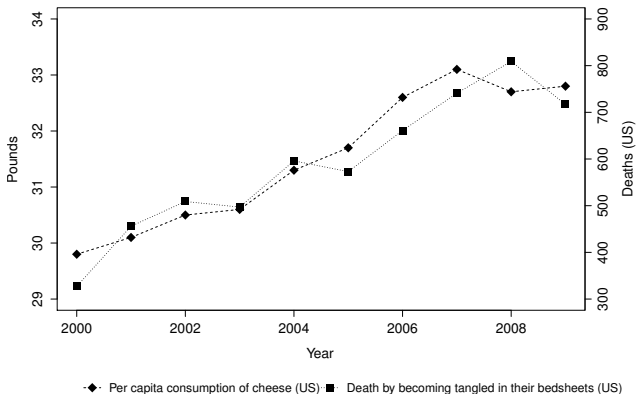
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└ What are we measuring?

Pearson correlation blooper



Correlation = 0.95 !

Example from <http://www.tylervigen.com>

Pearson correlation blooper (cont'd)

- This calculation would be awarded an F grade in Time Series 101
 - **Rule:** de-trend all time series before calculating correlations
- Why?
 - Otherwise the example tells us only that the trends of the two time series are of similar form (roughly linear)
 - This could have been deduced without any concept of correlation
 - Similar (high) correlations can be obtained from claims (and other financial) data simply because of inflation
- So, correlation calculated **after** de-trending of the time series provides a much more powerful tool
 - Because it measures the sympathy in departures of the two time series from their trends

Back to claim data correlations: how should they be calculated

- In the blooper example
 - Estimating a trend (in this case, perhaps just with respect to time) is equivalent to creating a model
 - Correlations calculated after de-trending are correlations between departures from the models
 - i.e. between residuals
- This is the case for all data sets
 - First, model the data (de-trend) to capture all deterministic effects
 - Calculate some form of residuals (stochastic effects)
 - Correlate the residuals
- Correlation is then a function of stochastic quantities, as it should be.

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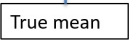
Measured correlations are model dependent

- It has been shown that measured correlations are based on residuals
- Residuals are departures from model fitted values
- Residuals are therefore model-dependent
- Correlations are therefore model-dependent

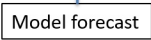
How are measured correlations affected by quality of modelling?

- Let future observations be denoted $Y_{kj}^{*(n)}$ (past $Y_{kj}^{(n)}$)
- Write all the $Y_{kj}^{*(n)}$ as a vector $Y^{*(n)}$
- Prediction error is

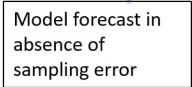
$$e^{(n)} = \underbrace{\left[Y^{*(n)} - \mu^{*\text{true}(n)} \right]}_{\text{Process Error}} + \underbrace{\left[\mu^{*\text{mod}(n)} - \hat{\mu}^{*(n)} \right]}_{\text{Parameter Error}} + \underbrace{\left[\mu^{*\text{true}(n)} - \mu^{*\text{mod}(n)} \right]}_{\text{Model Error}}$$



True mean



Model forecast



Model forecast in
absence of
sampling error

How are measured correlations affected by quality of modelling? (cont'd)

$$e^{(n)} = \underbrace{\left[Y^{*(n)} - \mu^{*\text{true}(n)} \right]}_{\text{Process Error}} + \underbrace{\left[\mu^{*\text{mod}(n)} - \hat{\mu}^{*(n)} \right]}_{\text{Parameter Error}} + \underbrace{\left[\mu^{*\text{true}(n)} - \mu^{*\text{mod}(n)} \right]}_{\text{Model Error}}$$

- Omission of predictive variables from the model (enlarging model error) shifts some of the signal in the data from measured explanatory effects to perceived random effects (noise)
- If the omitted explanatory variables are common to different LoBs, this is likely to create correlation between the “noise” of those LoBs
- Poor modelling may create apparent correlation where none actually exists
 - And none would be estimated with higher quality modelling

↑

Small for good models
Large for poor models

**The paper contains
an algebraic proof of
this result**

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Data set

AUSI (Allianz, UNSW, Suncorp, IAG) data set

- Contributed by UNSW's Linkage Project Partners
- Unit record files for a number of LoBs per Partner
 - Exposure files
 - Claim files
- Number of years varies by Partner and LoB
 - Up to 10 years for Home and Motor
- At present 4 LoBs:
 - Home
 - Motor
 - CTP
 - Public Liability

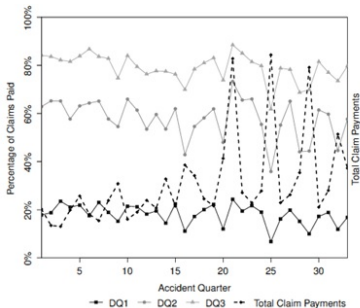
Data analysis

- Each Partner/LoB data summarised in a paid loss triangle
- Each triangle modelled with increasing attention to detail
- For each model
 - Standardised deviance residuals computed
 - Pearson correlations of residuals computed for various LoB pairs within Partner

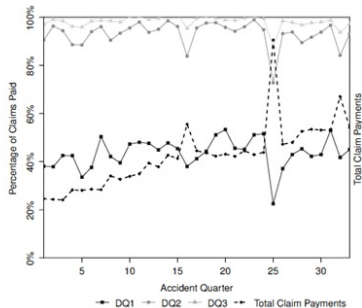
Results of real data analysis (conventional chain ladder)

		Cross-LoB Pearson correlation (whole triangles)					
		Insurer A				Insurer B	
		Home	Motor	CTP	PL	CTP	PL
Insurer A	Home	1	+0.59	+0.04	+0.06		
	Motor		1	+0.04	-0.02		
	CTP			1	-0.02		
	PL				1		
Insurer B	CTP					1	-0.09
	PL						1

Effects of major events?



6.4 (a) Home



6.4 (b) Motor

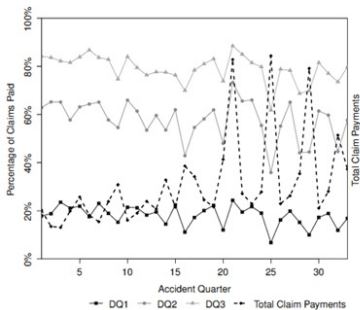
Major events cause sympathetic changes in both LoBs affecting:

- Volume of claim payments
- Rate of settlement

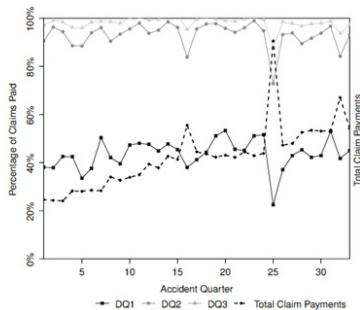
Results of real data analysis (AQs of major events simply deleted from chain ladder)

		Cross-LoB Pearson correlation (whole triangles)					
		Insurer A				Insurer B	
		Home	Motor	CTP	PL	CTP	PL
Insurer A	Home	1	+0.11	+0.04	+0.09		
	Motor		1	+0.02	-0.02		
	CTP			1	-0.02		
	PL				1		
Insurer B	CTP					1	-0.09
	PL						1

Seasonal effects?



6.4 (a) Home



6.4 (b) Motor

- Note seasonal changes in claim volumes
 - Greater in summer (both LoBs)
- Note greater volumes imply slower settlement (both LoBs)

Results of real data analysis (seasonal variates added to chain ladder for DQs 1-3)

		Cross-LoB Pearson correlation (whole triangles)					
		Insurer A				Insurer B	
		Home	Motor	CTP	PL	CTP	PL
Insurer A	Home	1	-0.01	+0.04	+0.09		
	Motor		1	+0.01	-0.02		
	CTP			1	-0.02		
	PL				1		
Insurer B	CTP					1	-0.09
	PL						1

Some observations

- For all pairs of LoBs other than Home-Motor, no statistically significant non-zero correlations are found
 - Even without any attempt to model the esoterica of those LoBs' experience
- Home-Motor requires more care
 - At a superficial level, it exhibits high correlation (0.6)
 - The majority of this is accounted for by a handful of natural events
 - The correlation of experience other than these is low (0.1)
 - This low correlation is accounted for by seasonal factors
 - If the model allows for these, then correlation vanishes

US evidence

- Chain ladder modelling has also been applied to four LoBs in the Meyers-Shi data set that covers many insurers
- Cross-LoB Pearson correlations again computed for 4 LoBs:
 - **PPA**: Private Passenger Auto
 - **CA**: Commercial Auto
 - **WC**: Workers Compensation
 - **OL**: Other Liability

US results

	Pearson correlation (whole triangles)			
	PPA	CA	WC	OL
PPA	1	+0.07	+0.01	+0.06
CA		1	+0.08	+0.00
WC			1	+0.02
OL				1

- Once again, little of interest here
- Even with crude chain ladder modelling

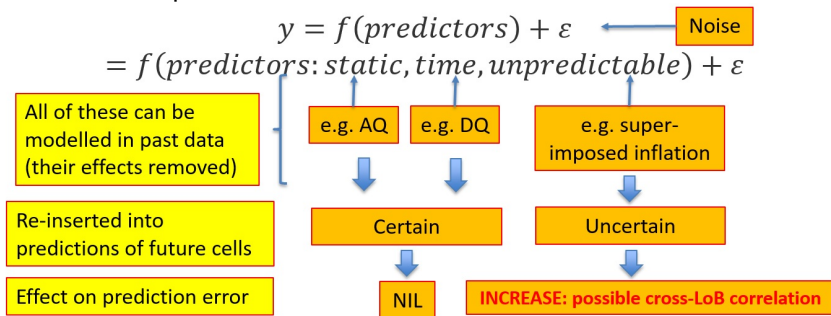
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Different types of predictors

Observation equation:

$$y = f(\text{predictors}) + \varepsilon$$

$$= f(\text{predictors: static, time, unpredictable}) + \varepsilon$$



Inferences

Although it may be possible to model away all cross-LoB correlation in past data

- It may not be correct to assume zero correlation for the future
- The extent to which it is incorrect depends on the extent to which unpredictable predictors are included in the model, e.g.
 - Superimposed inflation
 - Major events
 - Claim management changes
 - etc.
- Again, correlation is model dependent
 - And models of past and future may differ

- 1 Introduction
- 2 What are we measuring?
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Conclusions

- 1 Cross-LoB dependency is not an absolute
- 2 It is heavily dependent on the claims models used
- 3 With some attention to detail, it may be possible to model away virtually all cross-LoB correlation in past data
- 4 As a very broad generalization:
Better (poorer) modelling → less (greater) perceived dependency
- 5 A possible (even frequent) consequence of poor modelling is the creation of perceived correlation where none in fact exists
 - This correlation might very well be positive, which would:
 - Reduce measured diversification credit
 - Increase risk margins
 - Increase the insurance risk capital margin

Conclusions (cont'd)

- 6 Although it may be possible to model away all cross-LoB correlation in past data, it may not be correct to assume zero correlation for the future
 - Consideration will need to be given to allowance for cross-LoB dependency in relation to unpredictable explanatory variables
- 7 The procedure of modelling away dependency, and then re-inserting part of it
 - Is a more accurate reflection of the real world than failing to model it
 - Will not in general produce the same result as failing to model it