Background Model and properties Statistical estimation Expert functions Application 1 Application 2 Conclusions

A New and Flexible Regression Model for Ratemaking and Reserving

Andrei Badescu

Department of Statistical Sciences University of Toronto badescu@utstat.utoronto.ca

Joint work with Tsz Chai (Samson) Fung and Sheldon Lin

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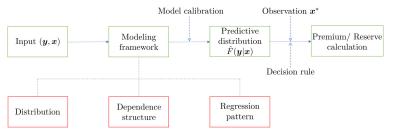


- 2 Model and properties
- 3 Statistical estimation
- 4 Expert functions
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- 6 Application 2



Process on ratemaking and reserving/prediction

- Policy attributes (covariates) and data:
 - $\mathbf{x} = (x_0, x_1, \cdots, x_P)^T$: Policyholder information (covariates)
 - y = (y₁, y₂, · · · , y_K)^T: Claim frequencies or severities of multiple business lines
- A typical modelling process



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Some of existing modelling approaches

Parametric models

- GLM, GAM, copula, ...
- Specified assumptions
- Easy to interpret/ compute
- but often inflexible due to linear or special structure of the models

Machine learning models

- Decision tree, neural network
- Fewer assumptions
- More flexible
- Hard to interpret (problematic for inference)
- Potentially overfitting to data and hence not robust

Alternative approach: Mixture-based models

- Mixture of Erlang distribution (Lee and Lin (2010, 2012)), Multivariate Pascal distribution (Badescu et al. (2015)), ...
- Semi-parametric and interpretable: Classification of policyholders into various risk subgroups
- Flexible and data-driven: Number of subgroups can be adjusted to control model complexity

Desirable properties for a "good model"

A model should be

- Flexible and parsimonious so that it can fit (without overfitting) any type of insurance claim data (multi-modal, light/heavy tailed..) and accommodate various dependence structures. We can also minimize the issue of model selection, an often difficult task;
- Interpretable in order to identify the (often highly nonlinear) relationships between policy attributes and claims;
- Mathematical tractable so that premiums, reserves, dependency measures and other quantities of interest can be calculated with ease;
- Statistical tractable, i.e. having efficient estimation/fitting algorithms.

Our proposed model

Start with a class of Generalized Mixture of Experts (GMoE) models...

$$h^{*}(\boldsymbol{y};\boldsymbol{x}) := h^{*}(\boldsymbol{y};\boldsymbol{x},\boldsymbol{\alpha}^{*},\boldsymbol{\beta}^{*},g) = \sum_{j=1}^{g} \pi_{j}^{*}(\boldsymbol{x};\boldsymbol{\alpha}^{*}) \prod_{k=1}^{K} f_{k}(y_{k};\boldsymbol{\theta}_{jk}^{*}(\boldsymbol{x};\boldsymbol{\beta}_{jk}^{*}))$$
gating function expert function

• Flexible, but extremely complicated!

How to make the GMoE useful in general/P&C insurance applications?

• Logit-weighted reduced Mixture of Experts Models (LRMoE)

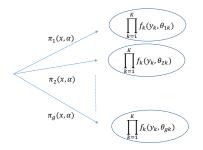
$$h(\boldsymbol{y};\boldsymbol{x}) := h(\boldsymbol{y};\boldsymbol{x},\boldsymbol{\alpha},\boldsymbol{\Theta},g) = \sum_{j=1}^{g} \pi_j(\boldsymbol{x};\boldsymbol{\alpha}) \prod_{k=1}^{K} f_k(y_k;\boldsymbol{\theta}_{jk})$$

logit-linear gating
$$\pi_j(\boldsymbol{x};\boldsymbol{\alpha}) = \frac{exp\{\boldsymbol{\alpha}_j^T\boldsymbol{x}\}}{\sum_{j'=1}^{g} exp\{\boldsymbol{\alpha}_{j'}^T\boldsymbol{x}\}}$$
no regression

Model description

- Interpretation
 - Policyholders classified in various homogeneous risk subgroups
 - Policyholder characteristics affects probabilities of assignments
 - Each risk group has its own frequency/severity distribution

A graphical interpretation



Denseness property

The full flexibility of the LRMoE is theoretically justified by its "denseness properties" = "approximates close enough"

- Denseness of LRMoE in the space of GMoE
 - Reducing GMoE to LRMoE does not reduce flexibility
 - Model parsimony
- Denseness in any regression distributions
 - LRMoE can be "fully flexible" to capture any distribution, dependence and regression patterns including nonlinear regression and covariate interactions

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• Calibrated model resembles any input data

Mathematical tractability

Marginalization properties (the LRMoE is closed under marginalization)

- Response marginalization: any marginal distribution is in the same class of distributions with easily calculated parameters
- Covariates marginalization: if some covariates are missing the response is still in the same class of distributions with with easily calculated parameters

Moment properties

• Mean, Variance, Covariance as well Kendall's tau and Spearman's rho all have analytical expressions

Identifiable - unique interpretation

Statistical estimation: an ECM algorithm

- Aim: Efficiently estimate maximum-likelihood parameters $\Phi = (lpha, \Theta)$
- Observed data log-likelihood (hard to optimize directly!):

$$l(\mathbf{\Phi}; \mathbf{y}, \mathbf{x}) = \sum_{i=1}^{n} \log \left[\sum_{j=1}^{g} \pi_j(\mathbf{x}_i; \alpha) \prod_{k=1}^{K} f(y_{ik}; \boldsymbol{\theta}_{jk}) \right]$$

Expectation conditional maximization (ECM) algorithm:

- E-step: Compute the expectation of complete data log-likelihood
- M-step: Maximize the likelihood requires high-dimensional optimization of non-concave functions!

How to choose an appropriate expert function?

Recall the denseness mild regularity condition:

• the expert function can be arbitrarily close to any degenerate distributions.

Frequency distributions

- Poisson X
- Negative Binomial X
- Conway-Maxwell-Poisson (CMP)
- Renewal Count model
- Discretized Severity model

Severity distributions Gamma Weibull Log-normal Inverse Burr Exponential X Pareto X

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The choice of experts for frequency distributions

Erlang Count Model

$$f(y; \theta) := P(N_1 = y; m, \beta) = e^{-\beta} \sum_{b=0}^{m-1} \frac{\beta^{my+b}}{(my+b)!}, \qquad y = 0, 1, 2, \dots$$

- Denseness condition
- Closed-form pmf
- Interpretation as a renewal process

The resulting model is called Erlang Count LRMoE (EC-LRMoE)

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The choice of experts for severity distributions

Transformed Gamma Model

$$ilde{Y}_i = rac{(1+Y_i)^\gamma - 1}{\gamma}, \qquad \gamma > 0$$

- Box Cox transforming the response variable
- Transformed variable \tilde{Y}_i follows LRMoE with gamma expert function

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• Captures light tail ($\gamma > 1$), heavy tail ($0 < \gamma < 1$) and extreme tail ($\gamma \rightarrow 0$)

The resulting model is called Transformed Gamma LRMoE (TG-LRMoE)

Data Overview

- European automobile insurance dataset
- 18,019 policyholders
- Bivariate response Y_i (2 business lines):
 - Y_{i1} : number of claims of motor third part liabilities
 - Y_{i2}: number of claims of car damages
- 11 covariates for *x_i*: Policyholder age, car age, geographical location etc.

Covariate Information

	Discret	e valued co	variates			
Variable	Description	Mean	Stddev	Minimum	Maximum	
x _{i1}	Age of policyholder	51.000	11.702	20	88	
× _{i2}	Car age	6.248	3.335	0	26	
		Categori	cal covariat	es		
Variable	Description	Levels				Proportions
x _{i3}	Car fuel	Diesel: x	$r_{i3} = 1$			0.383
		Gasoline	$x_{i3} = 0$			0.617
$x_{i4} - x_{i5}$	Policyholder's history	Renewal	with claims	alast year: x _{i4}	= 1	0.148
		New con	tract: x _{i5} =	= 1		0.235
		Renewal,	no claims	last year: x _{i4} ,	$x_{i5} = 0$	0.618
xi6-xi9	Geographical location	Region I:	$x_{i6} = 1$			0.187
		Region I	$x_{i7} = 1$			0.146
		Region I	II: $x_{i8} = 1$			0.111
		Capital:	$x_{i9} = 1$			0.420
		Region I	$V: x_{i6}, x_{i7},$	$x_{i8}, x_{i9} = 0$		0.136
xi10-xi11	Car brand class	Class A:	$x_{i10} = 1$			0.193
		Class B:	$x_{i11} = 1$			0.513
		Class C:	x _{i10} , x _{i11} =	= 0		0.284

Table: Summary of the covariates.

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Fitting result (EC-LRMoE)

• 5 components detected based on AIC

	ĥ			\hat{eta}	E[Y _{ik}]	$Z_{ij} = 1$]	$P(Z_{ij}=1)$
	k = 1	k = 2	k = 1	k = 2	k = 1	k = 2	-
i = 1	15	3	3.299	0.732	0.000	0.038	0.743
j = 1	(12.975,15)	(3,3)	(2.550,7.123)	(0.374,0.799)	(0.000,0.008)	(0.007,0.048)	(0.689,0.756)
i — 2	3	1	1.470	2.042	0.188	2.042	0.087
<i>j</i> = 2	(1,3)	(1,1)	(0.207,1.587)	(1.839, 2.229)	(0.147,0.236)	(1.839,2.229)	(0.073,0.107)
: _ 2	1	1	1.585	2.487	1.585	2.487	0.003
<i>j</i> = 3	(1,3)	(1, 15)	(0.807,7.661)	(1.899,27.036)	(0.752,2.742)	(1.449,3.128)	(0.001,0.010)
: 4	2	4	0.650	5.232	0.143	0.933	0.119
j = 4	(2,3)	(4,4)	(0.506,1.239)	(4.653,5.570)	(0.100,0.183)	(0.786, 1.018)	(0.098,0.166)
; _ E	6	3	5.665	1.902	0.513	0.310	0.047
<i>j</i> = 5	(4,8)	(3,3)	(2.621,7.648)	(1.415,2.465)	(0.191,0.578)	(0.172,0.420)	(0.037,0.076)

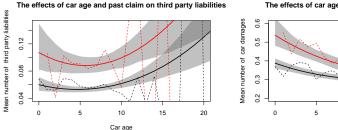
Table: Estimates of parameters

- Subgroup 1 is the lowest risk group
- Subgroup 3 is the highest risk group

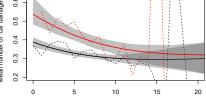
Preliminary fitting

Y_{i1}	Empirical	Fitted			Y _{i2}	Empirical	Fitted		
		NB GLM	ZINB GLM	EC-LRMoE			NB GLM	ZINB GLM	EC-LRMoE
0	16971	16975.06	16976.66	16965.19	0	14182	14177.32	14205.60	14188.88
1	991	972.64	969.88	1001.73	1	2499	2498.57	2386.71	2484.87
2	48	65.90	66.81	40.75	2	752	810.45	883.92	777.23
3	3	4.95	5.14	7.31	3	359	307.02	333.24	317.83
4	5	0.41	0.45	2.82	4	129	125.77	127.56	155.43
5+	1	0.04	0.05	1.20	5	66	54.19	49.51	64.01
					6	22	24.22	19.46	22.04
					7	7	11.15	7.74	6.52
					8+	3	10.30	5.26	2.19
χ^2		81.31	70.61	5.66	χ^2		22.59	33.88	11.13
loglik		-4224.94	-4213.99	-4208.77	loglik		-13279.18	-13204.95	-13178.68
mean	0.062	0.062	0.062	0.062	mean	0.340	0.340	0.340	0.340
% diff		0.011%	-0.001%	0.161%	% diff		-0.011%	-0.037%	-0.007%
variance	0.069	0.068	0.068	0.069	variance	0.649	0.669	0.644	0.650
% diff		-2.148%	-1.857%	-0.426%	% diff		3.077%	-0.805%	0.221%
skewness	5.084	4.522	4.544	5.096	skewness	3.265	3.672	3.305	3.261
% diff		-11.049%	-10.615%	0.244%	% diff		12.451%	1.215%	-0.132%
kurtosis	40.248	26.386	26.755	41.938	kurtosis	16.509	23.063	17.988	16.399
% diff		-34.441%	-33.526%	4.199%	% diff		39.702%	8.962%	-0.668%

Model visualization - Covariates influences



The effects of car age and past claim on car damages



Car age

Three individual profiles

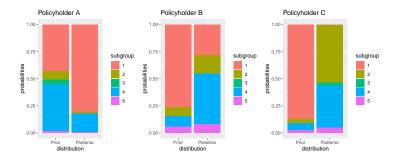
Policyholder	<i>y</i> ₁	<i>y</i> ₂	<i>x</i> ₁	<i>x</i> ₂	<i>x</i> 3	<i>x</i> ₄	<i>x</i> 5	x ₆	<i>x</i> ₇	<i>x</i> 8	<i>x</i> 9	x ₁₀	<i>x</i> ₁₁
A	0	0	36	1	1	1	0	0	0	1	0	0	0
В	0	1	59	7	1	0	1	0	0	1	0	0	1
С	1	2	72	7	0	0	0	1	0	0	0	1	0

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Table: Three selected policyholders to be considered for the calculations of subgroup probabilities.

Model visualization – Subgroup probabilities

- Consider 3 policyholders with very different characteristics
- Prior and posterior subgroup probabilities:



Predictive Applications

• Construct 6 hypothetical risk profiles: "Best", "Good", "Average 1", "Average 2", "Bad", "Worst"

Profile	<i>x</i> ₁	<i>x</i> ₂	<i>x</i> 3	<i>x</i> 4	<i>X</i> 5	<i>x</i> 6	<i>x</i> ₇	<i>x</i> 8	<i>X</i> 9	<i>x</i> ₁₀	<i>x</i> ₁₁
Best	60	8	0	0	0	0	0	0	0	1	0
Good	40	5	0	0	0	1	0	0	0	1	0
Average 1	40	6	0	0	0	0	0	0	1	0	1
Average 2	80	10	1	0	0	0	0	1	0	0	0
Bad	30	0	1	0	1	0	1	0	0	0	1
Worst	30	1	1	1	0	0	0	0	1	0	0

Table: Six different hypothetical risk profiles to be considered.

Predictive Applications

		Mean	and vari	ance of cla	ims	
Profile	$E[Y_{i1}]$	$Var[Y_{i1}]$	$E[Y_{i2}]$	$Var[Y_{i2}]$	$E[L_i]$	$Var[L_i]$
Best	0.033	0.035	0.179	0.316	0.212	0.396
Good	0.040	0.048	0.246	0.440	0.286	0.565
Average 1	0.050	0.051	0.347	0.710	0.397	0.847
Average 2	0.053	0.054	0.331	0.710	0.383	0.850
Bad	0.098	0.147	0.482	0.873	0.580	1.237
Worst	0.121	0.152	0.677	0.909	0.798	1.227

Table: Mean and variance of the number of claims.

Predictive Applications

• Various premiums based on the fitted model and various decision rules

	Quantile Premium		SD Pr	emium	SD Prem (Indep)		
Profile	75%	95%	$\gamma = 0.1$	$\gamma=0.5$	$\gamma = 0.1$	$\gamma = 0.5$	
Best	0.219	0.232	0.275	0.526	0.271	0.508	
Good	0.302	0.321	0.361	0.662	0.356	0.635	
Average 1	0.411	0.427	0.489	0.857	0.484	0.833	
Average 2	0.407	0.452	0.476	0.844	0.471	0.820	
Bad	0.595	0.680	0.691	1.136	0.681	1.085	
Worst	0.835	0.921	0.908	1.352	0.901	1.313	

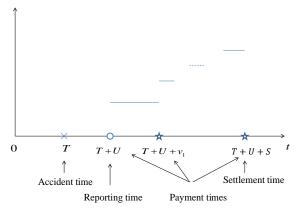
A micro-level approach

- Instead of looking at aggregate level as the classical "triangle" type methods, the idea is to look at granular level where one can use more information with respect to each indivudual claim development
- The number of accidents form a homogenous Poisson process

- Let T_i , $i = 1, ..., N^a(t)$, represent the i^{st} arrival eppoch
- Associated to each arrival time T_i we have
- U_i the reporting delay
- S_i the settlement delay
- Z_i the payment mark

A sample path of the claim developmental process

Amount



Data Overview

- European automobile insurance dataset
- Observation period: 1/1/2007 12/31/2012
- Verification period: 1/1/2013 01/01/2018
- 594,908 motor third-party liability insurance contracts
 - Contract number, start date and end date
 - Covariates information x_i available
- 28,256 reported claims
 - Contract number, loss date, reporting date, loss severity

Covariate information

Variable	Description	Туре	Levels
<i>x</i> _{k1}	Policyholder age	Discrete	
x_{k2}	Car age	Discrete	
<i>x</i> _{k3}	Car fuel	Categorical	Diesel: $x_{k3} = 1$
			Gasoline: $x_{k3} = 0$
$x_{k4} - x_{k7}$	Geographical location	Categorical	Region I: $x_{k4} = 1$
			Region II: $x_{k5} = 1$
			Region III: $x_{k6} = 1$
			Region IV: $x_{k7} = 1$
			Capital: $x_{k4} = x_{k5} = x_{k6} = x_{k7} = 0$
$x_{k8} - x_{k9}$	Car brand class	Categorical	Class A: $x_{k8} = 1$
			Class B: $x_{k9} = 1$
			Class C: $x_{k8} = x_{k9} = 0$
x_{k10}	Contract type	Categorical	Renewal contract: $x_{k10} = 1$
			New contract: $x_{k10} = 0$

Table: Summary of the covariates for the k^{th} contract.

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Modeling framework

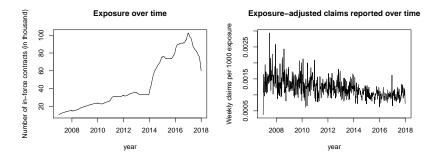


Figure: Number of in-force contracts and weekly number of claims reported (exposure adjusted) versus time.

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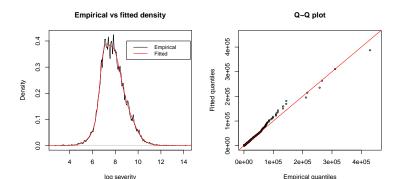
Modeling framework

- Claim arrival process follows a Poisson process with intensity $\lambda(t|\mathbf{x}_k) = \omega_k \exp{\{\mathbf{x}_k^T \boldsymbol{\beta}\}}$ with regression coefficients $\boldsymbol{\beta}$
- Modeling frequency: Poisson GLM by standard R package
- Modeling severity and reporting delay: Transformed Gamma LRMoE (TG-LRMoE)
- 11 covariates for *x_i*: Policyholder age, car age, geographical location etc.

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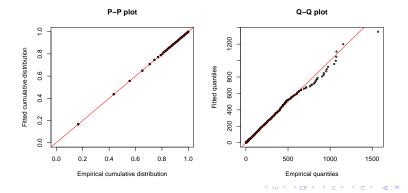
Fitting result (Severity)

- 9 components detected based on AIC
- Heavy-tailed distribution detected ($\hat{\gamma}=0.198<1$)
- Goodness-of-fit tests:



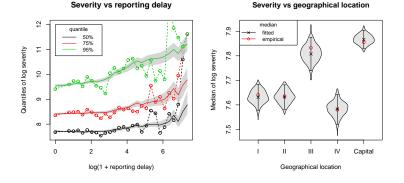
Fitting result (Reporting delay)

- 8 components detected based on AIC
- Goodness-of-fit tests:



• Visualizing covariate influences

 Relationship between loss severity and reporting delay/ geographical location



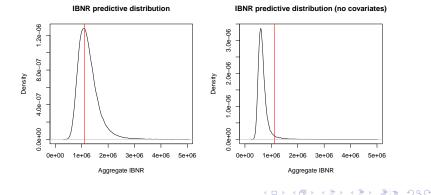
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- Methodology: Monte-Carlo simulation
 - Generate the claim frequency, reporting delay and severity directly from the fitted distributions for each contract

- Ompute the unreported amount of claims
- Aggregate the unreported claims across all contracts

• Out-of-sample IBNR prediction performance

- Left: IBNR prediction by the proposed modeling framework
- Right: IBNR prediction without covariates



Why is the inclusion of covariates important for adequate IBNR prediction?

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		an value/ prop	
	IBNR claims	All claims	Difference (%)
Policyholder age	46.113	45.994	0.3%
Car age	4.429	3.726	18.9%
Car fuel			
>Diesel	0.471	0.410	14.8%
>Gasoline	0.529	0.590	-10.3%
Geographical location			
>Region I	0.131	0.221	-40.6%
>Region II	0.160	0.227	-29.8%
>Region III	0.112	0.107	4.7%
>Region IV	0.089	0.138	-35.6%
>Capital	0.508	0.307	65.7%
Car brand class			
>Class A	0.247	0.268	-7.7%
>Class B	0.394	0.387	1.8%
>Class C	0.359	0.345	3.9%
Contract type			
>Renewal	0.644	0.572	12.7%
>New	0.356	0.428	-17.0%
Reporting delay (days)	308.583	17.839	1629.8%

Table: The mean value of each covariate for all simulated IBNR claims (simulated from the fitted model) and for all claims (based on the empirical training set).

Concluding Remarks

In this presentation, we...

- Propose the LRMoE as a multivariate regression model
 - Transparent interpretation Risk group classification
 - Denseness property "Full flexibility"
 - Mathematical and computational tractability Moment and marginalization properties, efficient model calibration algorithm

- Erlang Count expert function for frequency applications
 - Verify the denseness property empirically
 - Real insurance count data Demonstrate usefulness of EC-LRMoE in insurance ratemaking

Concluding Remarks

- Transformed Gamma expert function for severity modeling
 - Capturing a wide range of tail behavior
 - Fitting severity and reporting delay component of real insurance dataset
 - Predicting adequate IBNR reserves through out-of-sample testing

Upcoming ...

- Fitting censored and truncated data
 - Developing efficient fitting algorithm
 - Modeling reporting delay
 - Modeling losses subject to deductibles and policy limits
- An R package for insurance loss modeling implementation!!

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– Thank You –