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Applications, Complications and Considerations

- Application of projection methods
- loss development methodloss ratio method
- Bornhuetter-Ferguson technique
- other methods
- Complications
- parameter uncertainty
 volatility in RTR factors
- tail factor selection loss trend factors
- expected loss ratios
- data constraints
- line of business definition lack of claim count information
- Other considerations
 - qualitative information

Loss Development Method – Assumptions

- Assumes the relative change in a given year's reported loss & ALAE from one evaluation to the next will be similar to the relative change in prior years' reported loss & ALAE at similar evaluation points
- age-to-age factors measure change in reported loss & ALAE at successive evaluations
- tail factor allows for development beyond the observed experience
- Assumes the relative adequacy of the company's case reserves has been consistent over time
- Assumes no material changes in the rate claims are paid or reported

Loss Development Method – Suggestions for Tail Factors

Industry benchmarks

- excess of loss reinsurance: Reinsurance Association of America (RAA)
- reinsurance industry data going back 40+ years
- available for treaty vs. facultative and by attachment range pro-rata reinsurance: lagged primary sources
- ISO
- A.M. Best NCCI
- Curve fitting
- compare to benchmarks for reasonability

Loss Develo ment Method

Loss Development Method -

How to deal with variability in historical development

- Data organization is very important
 - · line of business mix
 - at the very least need to split property vs. casualty & pro-rata vs. excess
 - treaty vs. facultative
 - facultative often develops faster
 - attachment points/limits
 - need to understand attachment points on a "from ground-up" (FGU) basis need to understand how attachment points/limits are changing over time
 - segregate catastrophes

 - assess whether or not data is still credible after making refinements
 - data granularity
 - quarterly evaluations may be appropriate for fast reporting lines of business like property but will be too volatile for casualty













oplication sam	ne as for prir	mary business		
Layer	Accident Year	Excess Loss & ALAE @ 12/31/2011 (3)	LDF (4)	Ultimate Loss & ALAE (3) × (4)
(.)	(=)	(0)	(.)	(0)
800 x 200	2006	\$1,543	1.355	\$2,091
800 x 200	2007	1,255	1.488	1,867
800 x 200	2008	1,988	1.755	3,489
750 x 250	2009	1,868	2.336	4,364
750 x 250	2010	863	3.473	2,997
700 x 300	2011	0	8.196	0
	Total	\$7,517		\$14,808
esults levera	aed			

Loss Development Method

- Paid Loss Development Method not very common for reinsurance reserving
- little data
- no industry benchmarks on development
- may be appropriate for property or low limit proportional business (e.g., nonstandard auto liability)

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Loss Ratio Method

- Useful for new business or immature years
- Need premium base and a-priori expectation regarding loss ratio
- Advantage: stability
 - ultimate loss estimate does not change unless the premium or loss ratio are revised

Loss Ratio Method

- Potential problem: lack of responsiveness
- ignores actual loss experience as it emerges

Loss Ratio Method • Ultimate Loss = Earned Premium x ELR Ultimate Loss & ALAE Accident Expected Earned Year Premium Loss Ratio (2) × (3) (1) (2) (3) (4) 2006 \$3,994 66.5% \$2,656 3,577 4,161 2,564 70.0% 73.5% 76.5% 78.8% 2007 2008 2,504 3,058 1,961 2,182 2009 2010 2,769 2011 2,654 85.4% 2,267 \$19,719 Total \$14,628

Loss Ratio Method

Loss Ratio Method

- · Selecting the loss ratio
 - historical experience
 - paid and incurred loss experience
 - loss development method indications
 - adjust to appropriate year based on rate changes, trends and coverage changes underwriting considerations

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- underwriting files
- actuarial pricing
 market considerations
- benchmarks (industry results)
- · Don't be afraid to update based on actual results How has ELR performed in actual vs. expected calculations?

Bornhuetter-Ferguson Method

Bornhuetter-Ferguson Method -

- · Created specifically for reinsurers
- Needed a bridge between loss ratio method and development method
- · Essentially a blend of loss development method and expected loss method
 - begins with an a-priori estimate of expected losses
 - IELR (Initial Expected Loss Ratio) × Earned Premium = Initial Expected Loss (IEL)
 - splits a-priori estimate into two pieces
 - expected reported losses = (IEL × % reported)
 - expected unreported losses (IBNR) = (IEL × % unreported)
 - · replaces expected reported losses with actual reported (case incurred) losses
- Restated ultimate loss estimate equals
- expected unreported (IBNR) plus actual reported (case incurred)

Layer	Accident Year (1)	Earned Premium (2)	Initial Expected L/R (3)	Initial Expected Loss & ALAE (2) x (3) (4)	Expected Percent Reported (5)	Expected Reported Loss & ALAE (4) x (5) (6)	Expected Unreported Loss & ALAE (4) - (6) (7)
800 x 200	2006	\$3,994	66.5%	\$2,656	73.8%	\$1,960	\$696
800 x 200	2007	3 577	70.0%	2 504	67.2%	1 683	82
800 x 200	2008	4 161	73.5%	3.058	57.0%	1 743	1 31
750 x 250	2009	2.564	76.5%	1.961	42.8%	840	1.12
750 x 250	2010	2,769	78.8%	2.182	28.8%	628	1.55
700 x 300	2011	2,654	85.4%	2,267	12.2%	277	1,99
Total		\$19,719		\$14,628		\$7,130	\$7,498
(3) (5)	Based on analys Expected percer	is of historical acc	ident year results on excess loss di	adjusted for chang evelopment pattern	jes in retention. s.		



	Accident	Initial Expected	Expected Reported	Expected Unreported Loss & ALAE	Actual Case Inc'd	Ultimate Loss & ALAE
Layer	Year	Loss & ALAE	Loss & ALAE	(9) - (10)	Loss & ALAE	(11) + (12)
	(8)	(9)	(10)	(11)	(12)	(13)
800 x 200	2006	\$2,656	\$1,960	\$696	\$1.543	\$2.23
800 x 200	2007	2.504	1.683	821	1.255	2.07
800 x 200	2008	3,058	1,743	1,316	1,988	3,30
750 x 250	2009	1,961	840	1,122	1,868	2,99
750 x 250	2010	2,182	628	1,554	863	2,41
700 x 300	2011	2,267	277	1,990	0	1,99
Total		\$14,628	\$7,130	\$7,498	\$7,517	\$15,01



Bornhuetter-Ferguson Method - Advantages

- · Allows for smoothing of results
- LDF method understates when case incurred losses are small
- LDF method overstates if losses large (ELR may understate in this instance) Incorporates changes in the environment

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- attachment point, coverage changes, layer restructuring, price strengthening/deterioration should be captured in the ELR
- Balances stability and actual loss emergence
- Estimates IBNR when loss activity is sparse
- ideal for long tailed lines (umbrella, xs casualty)
- · less applicable for short tailed lines (approximates LDF method)

Bornhuetter-Ferguson Method

Bornhuetter-Ferguson Method - Disadvantages

Be

- Reporting pattern
 - expected percentage reported = 1 / LDF
- difficulty in estimating pattern for LDF method also applies here
- Initial expected losses
 - IBNR is directly related to a-priori estimate
 - double the expected losses \rightarrow double the IBNR
 - importance of IELR may be lost in the analysis need to step back and determine % of total IBNR that is loss ratio driven
- Ultimate Premium
 - most recent year may be difficult to estimate
 - booked premium is probably under-reported due to timing lags
 - seek underwriting estimate consider historical premium development

Bornhuetter-Ferguson Method - Sources of Initial Expected Loss

- Loss Ratio Method (incorporates pricing indices)
- Underwriting estimate from pricing study
- by definition it is the a-priori estimate
 verify that parameters for pricing and reserving are consistent
- Increased limits factors and direct premium
 - may be used if you feel primary company's higher limits pricing is inadequate
 - should have been incorporated in pricing study
 - · may also be used for changes in layer and/or attachment point
- Stanard-Buhlman estimates
- Frequency/Severity estimates

Example of change in layer structuring – Effect on IELR Restated Ultimate Loss & ALAE Loss & ALAE Accident Limits Ratio **Year** (1) Ratio (2) Layer (3) Adj Factor Layer (2) x (4) (4 800 xs 200 2006 66.5% 800 x 200 66.5% 1.00 70.0% 73.5% 72.7% 74.8% 1.00 1.00 1.05 1.05 800 x 200 800 x 200 750 x 250 750 x 250 70.0% 73.5% 76.5% 78.8% 2007 2008 2008 2009 2010 2011 77.1% 800 xs 200 1.11 700 x 300 85.4% Notes: (4) assumes that loss ratio increases 5% due to change in retention.

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Stanard-Buhlman Estimate

Essentially the Bornhuetter-Ferguson estimate with "on average"
 perfect information

Other Reserving Methods

- Uses actual loss ratio indices multiplied by average loss ratio
 incorporates loss trend and pricing changes
- Balances the expected average loss ratio so that
 expected reported losses = actual reported losses

				Other Res	erving Methods
Stanard- Tradition	-Buhlman – a al Calculation	n Example			
Acc	Earned	Average Ultimate	Pricing	Adjusted Ultimate L/R	Expected Ultimate Loss & ALAE
(1)	_ Premium			(3 X 4) (5)	(2 x 3)
(1)	(2)	(3)	(4)	(5)	(0)
2006	\$3,994	70.0%	0.95	66.5%	\$2,656
2007	3,577	70.0%	1.00	70.0%	2,504
2008	4,161	70.0%	1.05	73.5%	3,058
2009	2,564	70.0%	1.17	81.8%	2,097
2010	2,769	70.0%	1.23	86.2%	2,387
2011	2,654	70.0%	1.39	97.2%	2,580
Total	\$19,719				\$15,283
					22
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Acc	Earned	Expected Ultimate Loss & ALAE	Percent	Expected Reported Loss & ALAE	Actual Case Inc'd
(1)	(2)	(6)	(7)	(8)	(9)
2006	\$3,994	\$2,656	73.8%	\$1,960	\$1,54
2007	3,577	2,504 3.058	57.0%	1,683	1,25
2009	2,564	2,097	42.8%	898	1,86
2010 2011	2,769 2,654	2,387 2,580	28.8% 12.2%	687 315	86
Total	\$19,719	\$15,283		\$7,285	\$7,51
			Ratio of ac	tual to expected:	1.03
			Rest	ated Loss Ratio:	72.29















			Expected		
	Initial	Expected	Unreported	Actual	Ultimate
Acc	Expected	Reported	Loss & ALAE	Reported	
(1)		LUSS & ALAE	(2)-(3)	LUSS & ALAE	(4) + (5)
(1)	(2)	(3)	(4)	(5)	(0)
2006	\$2,740	\$2,022	\$718	\$1,543	\$2,26
2007	2,583	1,736	847	1,255	2,10
2008	3,156	1,798	1,358	1,988	3,34
2009	2,164	926	1,237	1,868	3,10
2010	2,463	709	1,754	863	2,61
2011	2,662	325	2,337	0	2,33
	\$15,769	\$7,517	\$8,252	\$7,517	\$15,76

Frequency/Severity Method – Basic Steps

- Pick a data limit where credible excess claims data exists · Estimate the annual number of claims above the data limit
- 37.5 claims greater than \$150,000
- Use size-of-loss curves to project the number of claims above the reinsurance retention
- 7.9 (of 37.5 claims) greater than \$300,000 · Use size-of-loss curves to project average severity of claims in
- reinsurance layer
- \$224,014 average severity of claims in \$700,000 excess of \$300,000 layer Multiply the frequency and the severity projections to estimate the total ultimate losses

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- Incorporate frequency/severity estimate into Bornhuetter-Ferguson method
- Most common distribution used is the Single-parameter Pareto

Frequency/Severity Method - Why use the Single-parameter Pareto Distribution?

- Shape of tail
- Ease of calculation (even though it's not built into Excel)
- survival function $S(X) = (Theta / X) ^ Alpha$
- conditional limited expected value is a simple formula (see following pages) simple to incorporate trend
- Easy to parameterize
- Theta must be set in advance (equal to the data limit)
- maximum likelihood estimated Alpha parameter is simple to calculate
- normalize losses greater than the data limit by dividing by the data limit = X take the natural log of the normalized losses = ln(X) mle Alpha = the number of losses > the data limit / sum[ln(X)]
- Always a good idea to look at the graph of your observations and fitted distribution
 - beware over-weighting to smaller values
 - keep in mind what layer you are interested in

Accident Year	Detrended Data Limit	Act #> Detrended Data Limit	Claim Count Develpoment Factors	Individual Total Excess Counts (3 x 4)
(1)	(2)	(3)	(4)	(5)
2006	\$112.089	38	1.125	42.8
2007	118,814	34	1.282	43.6
2008	125,943	25	1.408	35.2
2009	133,499	31	1.555	48.2
2010	141,509	22	1.927	42.4
2011	150,000	11	2.618	28.8
Total		161		240.9
) Assumes 6	5% trend.			



					Other Res	erving Methods
Frequen Estimate	c y/Severity of claim co	/ Method unts abov	– an Exa /e data lir	imple nit (Con't))	
Acc. Year (1)	Projected # of claims > Data Limit (2)	Subject Earned Premium (3)	On-Level SEP (4)	Indicated Frequency (2 / 4) (5)	Selected Frequency (6)	Selected # of Excess Claims (7)
2006	42.8	\$50,000	\$62,750	0.681		42.8
2007	43.6	50,000	63,550	0.686		43.6
2008	35.2	55,000	63,525	0.554		35.2
2009	48.2	60,000	63,000	0.765	0.750	48.2
2010	42.4	55,000	55,000	0.771	0.750	41.3
2011	28.8	50,000	50,000	0.576	0.750	37.5
Total	240.9	\$320,000	\$357,825	0.673		248.5
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Accident	Lay	Projected #			Average Severity in Layer	Ultimate Loss & ALA in Layer (4 x 5)
Year	Limit XS Retention (2)		> \$150,000 > Retention			
(1)			(3)	(4)	(5)	(6)
2006	\$800.000	\$200.000	42.8	12.5	\$171.963	\$2 147 83
2007	800.000	200.000	43.6	14.4	171,963	2.478.59
2008	800.000	200 000	35.2	13.2	171 963	2 265 46
2009	750,000	250,000	48.2	12.7	210 543	2 675 80
2010	750.000	250.000	41.3	12.3	210,543	2.591.56
2011	700,000	300,000	37.5	8.6	246,020	2,115,01
Total			248.5	73.7		\$14,274,27
Notes:	 (4) from pareto siz (5) from pareto siz [Retention / (A Assumes Alpha pa 	e-of-loss curve f e-of-loss curve s lpha - 1)] * { 1 - rameter of 2.12	requency formula severity formula; [Retention / (Lin 5, basic limit detr	; (3) x [Basic Limit hit + Retention)] ^ (ended at 6%.	/Attachment]^ Alpha - 1)}	Alpha



Initial Expected Expected Expected Actual Layer Year Loss & ALAE Loss & ALAE Loss & ALAE Loss & ALAE (1) (2) (3) (4) (5) 800 x200 2007 2,148 \$1,585 \$566 \$1,545 800 x200 2007 2,479 1,666 \$13 1,255 800 x200 2009 2,2695 1,231 1,989	Actual Ultimate Reported Loss & ALAE (5) (6) 83 \$1,543 \$2,106 13 1,255 2,068 75 1,988 2,963	Expected Unreported	Expected			
(1) (2) (3) (4) (5) 800 x200 2006 \$2,148 \$1,585 \$563 \$1,541 800 x200 2007 \$2,479 1,686 \$131 1,255 800 x200 2007 \$2,479 1,686 \$131 1,255 800 x200 2008 \$2,285 1,945 \$1,985 \$1,888 900 x200 2008 \$2,425 1,945 \$1,957 1,888	(5) (6) 63 \$1,543 \$2,106 13 1,255 2,068 75 1,988 2,963	LOSS & ALAE	Reported Loss & ALAE	Expected Loss & ALAE	Acc Year	Laver
800 x 200 2006 \$2,148 \$1,585 \$563 \$1,543 800 x 200 2007 2,479 1,666 813 1,255 800 x 200 2008 2,265 1,291 975 1,988 750 x 260 2009 2,875 1,145 1,500 1,988	63 \$1,543 \$2,106 13 1,255 2,068 75 1,988 2,963	(4)	(3)	(2)	(1)	
800 x 200 2007 2,479 1,666 813 1,255 800 x 200 2008 2,265 1,291 975 1,988 750 x 250 2000 2,876 1,105 1,590 1,988	13 1,255 2,068 75 1,988 2,963	\$563	\$1,585	\$2,148	2006	800 x 200
800 x 200 2008 2,265 1,291 975 1,988 750 x 260 2009 2,876 1145 1,520 1,988	75 1,988 2,963	813	1,666	2,479	2007	800 x 200
750 250 2000 2676 1145 1520 1969		975	1,291	2,265	2008	800 x 200
730 2009 2,070 1,143 1,330 1,000	30 1,868 3,398	1,530	1,145	2,676	2009	750 x 250
750 x 250 2010 2,592 746 1,845 863	45 863 2,708	1,845	746	2,592	2010	750 x 250
700 x 300 2011 2,115 258 1,857 0	57 0 1,857	1,857	258	2,115	2011	700 x 300
Total \$14,274 \$6,691 \$7,583 \$7,517	83 \$7,517 \$15,100	\$7,583	\$6,691	\$14,274		Total



					Keco	p of Methods
ecap of	Methods	; – Ultim	ate Loss	and ALA	٩Ε	
Acc. Year		Loss Ratio	Bornhuetter Ferguson (w/ IELR)	Stanard- Buhlman	Frequency/ Severity	Bornhuetter Ferguson (w/ F/S)
(1)	(2)	(3)	(4)	(5)	(6)	(7)
2006	\$2.091	\$2.656	\$2.239	\$2.261	\$2,148	\$2.106
2007	1,867	2,504	2,076	2,102	2,479	2,068
2008	3,489	3,058	3,304	3,346	2,265	2,963
2009	4,364	1,961	2,990	3,105	2,676	3,398
2010	2,997	2,182	2,417	2,617	2,592	2,708
2011	0	2,267	1,990	2,337	2,115	1,857
Total	\$14,808	\$14,628	\$15,015	\$15,769	\$14,274	\$15,100
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Final Selection of Ultimates - Rules of Thumb

- · LDF methods for older, more mature accident/policy periods
 - look at LDF/percentage reported to determine maturity
 - Use when LDF is below 2.000, percent reported >= 50% umbrella versus auto physical damage
- Expected loss techniques for newer, less mature accident/policy periods

Recap of

- most recent or two most recent accident years
- Bornhuetter-Ferguson/ Stanard-Buhlman, anywhere in between
- requires judgment: (GL, umbrella, excess casualty) · Frequency/Severity: similar to expected loss techniques
- better estimate when loss ratio is unstable/unreliable high layers, single treaties, single claims
- Benchmarks
- IBNR to case O/S ratios

Adjustment for Incomplete Years

- · Recent underwriting or policy years may not be fully earned as of the evaluation date
 - may need to scale back loss development projections
 - various ways to project the earned portion of the ultimate loss
 - apply ultimate loss ratio to earned premium as of evaluation date remove expected loss on the unearned premium
- Ultimate Loss Ratio = Ultimate Loss / Ultimate Premium
- Ultimate premium can be based on projected premium development
- seek underwriter input

Other Co

Other Considerations

- Look for trends, stability, shocks
- are they reasonable ?
- Communicate with the underwriting and claims departments good fodder for next underwriting audit or pricing season
- Gather knowledge on reserving philosophy (level of Additional Case Reserves or ACRs)
- make adjustments where necessary to benchmarks
- Understand reserving process may need to adjust benchmark loss development patterns – bordereau vs. individual reporting

 - early closing
- How to handle new lines of business with no history? benchmarks, underwriting files, actuarial pricing analysis
- Difficult Coverage (Agg XS, deductibles, reinstatements) requires modeling of underlying exposures

Other Approaches

Asbestos, Pollution, Construction Defect, Other Health Hazards

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Other Cor

- · need to handle separately
 - cedent information, industry data, benchmarks results of exposure based modeling techniques
- · consider a survival ratio analysis
- Large Events / Market Losses
- · seek input from claims department
- utilize market information / knowledge
- Property Catastrophes
- results of models (may need to adjust)
- underwriter estimates
- traditional top-down techniques
- · Ground-up analysis
- other industry sources such as ISO's PCS

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