

**CLRS 2013
CLFM Estimates**

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Agenda

- CLFM and the R ChainLadder package
 - Finding the selection-consistent model
 - Graphing the link ratio function
 - A look at two diagnostic plots
 - Calculating IBNR and standard errors
 - Visualizing the estimated distribution of the predicted IBNR outcomes
- California Workers Comp data
- Questions for discussion

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Users are demanding something be done! 😊

- Apr 8, 2009
I am using the latest version of Chainladder in R 2.8.1 and have found it to be an excellent package indeed.
There are occasions when the development factor may need to be selected as different from the output of the linear model. Is there a place in the MackChainLadder code where different development factors may be used?
Thanks and Regards.
- Feb 27, 2013
I agree with this proposal. We often have to choose specific coefficients. Could it be an option in the input of the functions bootchainladder and MackChainLadder?
Thank you in advance.

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CLFM in the ChainLadder Package

- ChainLadder (<https://code.google.com/p/chainladder/>)
 - A library of functions (a "package") for the R statistical environment (www.r-project.org)
 - Primarily targeted toward stochastic reserving
 - Originated and maintained by Markus Gesmann of Lloyds
 - Other contributing authors: Wayne Zhang and yours truly
 - Distributed under the GPL (General Public License)
 - Therefore, open-source, free to download, use, copy, modify, etc.
- Markus programmed the Mack method using linear regression models on the development periods
 - He used Barnett & Zehnwirth's ("Best Estimates for Reserves") delta (δ) notation for weighting the observations
 - So CLFM's α = Barnett & Zehnwirth's δ
 - He used Mack's recursive formula (1999 paper) to chain the standard error statistics together
 - Mack's formulas use alpha ($2-\delta$) for weighting the observations

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Finding a selection-consistent model: CLFMdelta

- As explained by Manolis, a selection-consistent member of CLFM is a model whose expected value of the regression slope equals the actuary's selected RTR
- Use CLFMdelta(Triangle, selected, tolerance = .0005)
 - Triangle = loss data
 - selected = actuary's selected age-to-age factors
 - tolerance = proximity of found parameter to selected RTR
- selected = c(8.206, 1.624, 1.275, 1.175, 1.115, 1.042, 1.035, 1.018, 1.009)
- CLFMdelta(RAA, selected)

ChainLadder

| | | | | | | | | |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| 2.000000 | 1.000000 | 1.158150 | 1.305441 | 1.116562 | 1.000000 | 3.000000 | 2.000000 | 1.000000 |
| 2.000 | 1.000 | 1.158 | 1.305 | 1.117 | 1.000 | 2.565 | 2.005 | 2.005 |

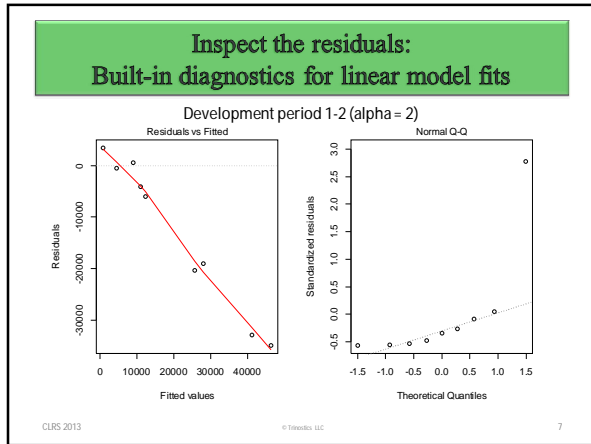
Paper

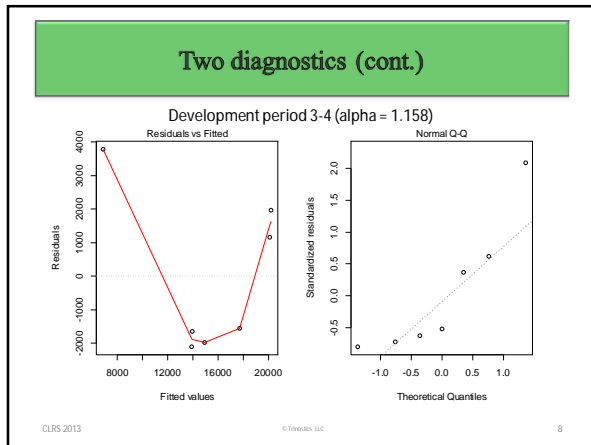
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Visualizing the search for α : ChainLadder's LRfunction

- LRfunction(x, y, delta) *B&Z's δ notation
 - x = beginning value of loss during a development period
 - y = ending value of loss during a development period
 - delta = a real number or a vector of real numbers
- Here, x & y are the column 7 & 8 losses for development period 7-8

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Running ChainLadder's MackChainLadder function with alpha = 2-delta gets close to a full CLFM implementation

```

> MackChainLadder(RAA, alpha = 2 - CLFMSdelta(RAA, selected))
MackChainLadder(Triangle = RAA, alpha = 2 - CLFMSdelta(RAA, selected))
  Latest Dev.To.Date Ultimate INBR Mack.S.E CV(INBR)
1991 19,834 1.0000 19,834 0 0.00e+00 NA
1992 16,704 0.9909 16,858 154 4.21e-01 0.50273
1993 23,466 0.9734 24,108 642 4.19e+02 0.96367
1994 27,007 0.9400 29,729 1,726 2.50e+02 0.46670
1995 26,180 0.9022 29,018 2,838 1.50e+03 0.53034
1996 19,802 0.8092 19,891 3,739 1.98e+03 0.52218
1997 12,314 0.6856 17,881 5,987 2.18e+03 0.25144
1998 13,112 0.5401 24,276 11,164 5.40e+03 0.50196
1999 5,393 0.3327 16,227 32,822 4.42e+03 0.59279
1990 2,063 0.0405 50,887 49,824 8.17e+04 1.67315

      Totals
Latest: 160,987.00
Dev: 0.65
Ultimate: 246,463.48
INBR: 89,476.48
Mack S.E.: 82,651.02
CV (INBR): 0.97
    
```

ChainLadder

| Age | Estimated Ultimate | Current Diagonal | Estimated Inpaid | Total Risk | CV |
|-----|--------------------|------------------|------------------|------------|-------|
| 48 | 246,387 | 160,987 | 85,400 | 82,838 | 97.0% |

Paper

✓ Although the MackChainLadder function does not provide for the psi-function process risk adjustment, the bottom line CVs are virtually identical

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Possible questions for discussion


1. Under what circumstances might it be reasonable to expect the standard error of cumulative developed losses to be inversely proportional to the beginning value of loss ($\alpha < 0$)?
2. What is the difference between the Chain Ladder method and the Loss Development method?
3. [per 2nd post on slide 1]
Is it appropriate to carry out the England and Verrall bootstrap method given a triangle and an arbitrary set of selected link ratios? Why or why not?

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Thanks

- To my co-authors Manolis and Ali Majidi for being the brains behind our paper
- To the many reviewers for their time, patience, and constructive comments, and their dedication to the 



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