

# Stochastic Loss Reserving: A New Perspective from a Dirichlet Model

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# Outline

Introduction

Method

Statistical Inference

Data Analysis

Conclusion

# Background

Loss reserving is a classical actuarial problem:

- ▶ Balance sheet item → solvency
- ▶ Ratemaking → profitability

Two components

- ▶ To estimate the outstanding liability
- ▶ To quantify the associated variability

# Motivation

Two prominent macro-level **stochastic** loss reserving methods:

- ▶ Chain-Ladder method: development factors or age-to-age ratios
- ▶ Bornhuetter-Ferguson method: expected ultimate and unpaid quota

Connections and disconnections:

- ▶ BF can be viewed as a credibility weighted average of CL and expected ultimate loss
- ▶ Different data generating process for the same run-off triangle

## Contribution

We propose a new stochastic loss reserving method based on a Dirichlet distribution

New perspective to view the relation between CL and BF:

- ▶ Both CL and BF prediction are derived from the same stochastic model
- ▶ The choice between the two depends on the type of information available
- ▶ It becomes an inference problem rather than model selection

Nice Properties:

- ▶ Same age-to-age factors as CL
- ▶ Generalize the credibility weight in the BF

## Data Structure

Micro-level reserving: triangular aggregate data

- ▶ A triangle consists of  $m$  accident years and  $n$  development years ( $m > n$ )
- ▶ Let  $X_{ij}$  denote **incremental paid loss** in accident year  $i$  development year  $j$
- ▶ We work with  $Y_{ij}/E_i$ , where  $E_i$  is the exposure for accident year  $i$

	Accident	Development Year				
	Year	1	2	...	$n - 1$	$n$
Fully developed	1	$Y_{11}$	$Y_{12}$	...	$Y_{1n-1}$	$Y_{1n}$
	$\vdots$	$\vdots$				$\vdots$
	$m - n$	$Y_{m-n,1}$	$Y_{m-n,2}$	...	$Y_{m-n,n-1}$	$Y_{m-n,n}$
Run-off Triangle	$m - n + 1$	$Y_{m-n+1,1}$	$Y_{m-n+1,2}$	...	$Y_{m-n+1,n-1}$	$Y_{m-n+1,n}$
	$m - n + 2$	$Y_{m-n+2,1}$	$Y_{m-n+2,2}$	...	$Y_{m-n+2,n-1}$	
	$\vdots$	$\vdots$		...		
	$m - 1$	$Y_{m-1,1}$	$Y_{m-1,2}$			
	$m$	$Y_{m,1}$				



## Dirichlet Distribution

Consider an example of  $K = 3$ :

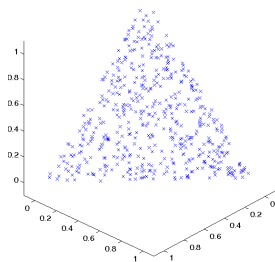
$$f(p_1, p_2, p_3) = \frac{\Gamma(p_1 + p_2 + p_3)}{\Gamma(\alpha_1)\Gamma(\alpha_2)\Gamma(\alpha_3)} p_1^{\alpha_1-1} p_2^{\alpha_2-1} p_3^{\alpha_3-1},$$

where  $p_1 + p_2 + p_3 = 1$ .

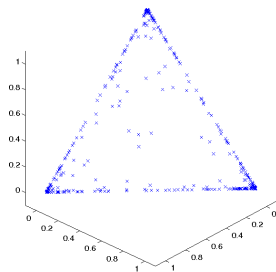
The support is the hyperplane  $p_1 + p_2 + p_3 = 1$ , and parameters  $\alpha = (\alpha_1, \alpha_2, \alpha_3)$  determines the values of  $p_1, p_2, p_3$



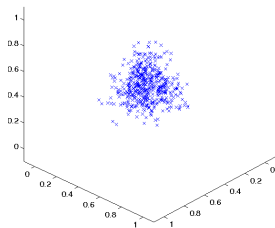
# Dirichlet Distribution



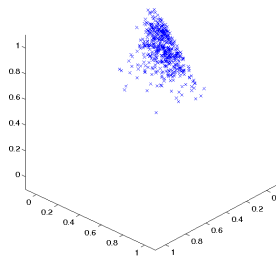
$$\alpha = [1, 1, 1]$$



$$\alpha = [.1, .1, .1]$$



$$\alpha = [10, 10, 10]$$



$$\alpha = [2, 5, 15]$$

## Dirichlet Distribution

The Dirichlet distribution can be thought of as a **distribution over probability mass functions** of length  $K$ :

Let  $P = (P_1, \dots, P_K)$  be a random vector with  $K \geq 2$  components. Then  $P$  is said to follow the Dirichlet distribution of order  $K \geq 2$ , which we denote by  $P = (P_1, \dots, P_K) \sim \text{Dir}(\alpha_1, \dots, \alpha_K)$ , if its density is given by:

$$f(p; \alpha_1, \dots, \alpha_K) = \frac{\Gamma(\sum_{k=1}^K \alpha_k)}{\prod_{k=1}^K \Gamma(\alpha_k)} \prod_{k=1}^K p_k^{\alpha_k - 1},$$

where  $\alpha_1, \dots, \alpha_K$  are parameters of the distribution with  $\alpha_k > 0$  for each  $k$ , and  $p = (p_1, \dots, p_K)$  is on the  $(K - 1)$ -dimensional probability simplex, i.e.  $\sum_{k=1}^K p_k = 1$  and  $p_k \geq 0$  for  $k = 1, \dots, K$ .

## Reserving Model

We propose to model the incremental loss ratios ( $Y_{ij} = X_{ij}/E_i$ ) using a **scaled Dirichlet distribution**.

For accident year  $i$ , we assume:

$$\left( \frac{Y_{i1}}{\phi_i}, \dots, \frac{Y_{in}}{\phi_i}, 1 - \frac{\sum_{j=1}^n Y_{ij}}{\phi_i} \right) \sim \text{Dir}(a_1, \dots, a_n, b_n), \text{ with } 0 < \sum_{j=1}^n Y_{ij} < \phi_i,$$

where  $\phi_i$ ,  $a_1, \dots, a_n$ , and  $b_n$  are parameters to be estimated.

## Reserving Model

Define cumulative paid loss  $S_{i,1:n} = Y_{i1} + \dots + Y_{in}$  and  $a_0 = a_1 + \dots + a_n$ . For interpretation, we show an equivalent of representation of model as:

$$\left\{ \begin{array}{l} \left( \frac{Y_{i1}}{S_{i,1:n}}, \frac{Y_{i2}}{S_{i,1:n}}, \dots, \frac{Y_{in}}{S_{i,1:n}} \right) \Big| S_{i,1:n} \sim \text{Dir}(a_1, \dots, a_n) \\ \frac{S_{i,1:n}}{\phi_i} \sim \text{Beta}(a_0, b_n) \end{array} \right.$$

The Dirichlet model is about **allocation** given  $S_{i,1:n}$ :

$$x_1 = \frac{Y_{i1}}{S_{i,1:n}}, x_2 = \frac{Y_{i2}}{S_{i,1:n}}, \dots, x_{n-1} = \frac{Y_{i,n-1}}{S_{i,1:n}}$$
$$x_n = \frac{Y_{in}}{S_{i,1:n}} = 1 - \sum_{j=1}^{n-1} x_j$$

Mathematical properties of Dirichlet distribution implies that past allocation does not inform future allocation.

## Reserving Model

The model implies both past and future allocations given cumulative payments:

$$\left( \frac{Y_{i1}}{S_{i,1:k}}, \dots, \frac{Y_{ik}}{S_{i,1:k}} \right) | S_{i,1:k} \sim \text{Dir}(a_1, \dots, a_k)$$
$$\left( \frac{Y_{ik+1}}{\phi_i - S_{i,1:k}}, \dots, \frac{Y_{in}}{\phi_i - S_{i,1:k}}, \frac{\phi_i - S_{i,1:n}}{\phi_i - S_{i,1:k}} \right) | S_{i,1:k} \sim \text{Dir}(a_{k+1}, \dots, a_n, b_n).$$

## Properties

Age-to-age factor and unpaid percentage:

In CL and BF:

$$\gamma_{k:k+1} = \frac{E(S_{i,1:k+1})}{E(S_{i,1:k})}, \quad \text{and} \quad \eta_k = \frac{E(S_{i,1:k})}{E(S_{i,1:n})}.$$

Dirichlet model:

$$\gamma_{k:k+1} = \frac{a_1 + \cdots + a_{k+1}}{a_1 + \cdots + a_k}$$
$$\eta_k = \frac{a_1 + \cdots + a_k}{a_1 + \cdots + a_n}$$

## Properties

Reserve prediction at development year  $k$  is

$$\widehat{R}_i = \widehat{S}_{i,1:n} - S_{i,1:k} = E(S_{i,1:n} | S_{i,1:k}) - S_{i,1:k}$$

Recall the well-known results:

$$\widehat{R}_i^{EX} = E(S_{i,1:n}) - S_{i,1:k}$$

$$\widehat{R}_i^{CL} = \left( \prod_{j=k}^{n-1} \gamma_{j,j+1} - 1 \right) S_{i,1:k}$$

$$\widehat{R}_i^{BF} = \eta_k \widehat{R}_i^{CL} + (1 - \eta_k) \widehat{R}_i^{EX}$$

## Properties

At development year  $k$ , the Dirichlet model predicts:

$$\widehat{R}_i^D = v_k \widehat{R}_i^{CL} + (1 - v_k) \widehat{R}_i^{EX},$$

where

$$v_k = \left\{ \frac{\text{CV}(S_{i,1:n})}{\text{CV}(S_{i,1:k})} \right\}^2 = \frac{\text{Var}(S_{i,1:n})}{\text{Var}(S_{i,1:k})} \left\{ \frac{\text{E}(S_{i,1:k})}{\text{E}(S_{i,1:n})} \right\}^2$$

Compare with BF prediction:

$$\widehat{R}_i^{BF} = \eta_k \widehat{R}_i^{CL} + (1 - \eta_k) \widehat{R}_i^{EX}$$

where

$$\eta_k = \frac{\text{E}(S_{i,1:k})}{\text{E}(S_{i,1:n})}$$

We note the limiting case:  $v_k \rightarrow \eta_k$  when  $\frac{\sum_{j=k+1}^n a_j}{b_n} \rightarrow 0$



## Estimation

To predict the outstanding payments, one needs the unknowns

$$\theta = (a_1, a_2, \dots, a_n, b_n, \phi_1, \phi_2, \dots, \phi_m).$$

Two types of data:

- Fully developed accident year: for  $1 \leq i \leq m - n$ ,

$$\left( \frac{Y_{i1}}{\phi_i}, \dots, \frac{Y_{in}}{\phi_i}, 1 - \frac{S_{i,1:n}}{\phi_i} \right) \sim \text{Dir}(a_1, \dots, a_n, b_n)$$

- Not fully developed accident year: for  $m - n + 1 \leq i \leq m$ ,

$$\left( \frac{Y_{i1}}{\phi_i}, \dots, \frac{Y_{im+1-i}}{\phi_i}, 1 - \frac{S_{i,1:m+1-i}}{\phi_i} \right) \sim \text{Dir} \left( a_1, \dots, a_n, a_0 + b_n - \sum_{j=1}^{m+1-i} a_j \right)$$

# Estimation

Frequentist estimation:

- ▶ Likelihood-based estimation
- ▶ When  $a_0/(a_0 + 1) \approx 1$ , we obtain CL estimates

Bayesian estimation:

- ▶ It allows for a hierarchical extension:  $\phi_1, \phi_2, \dots, \phi_n \stackrel{iid}{\sim} \text{uniform}(0, \phi)$  with a flat hyper prior  $p(\phi) \propto 1$  for  $\phi \in (0, \infty)$
- ▶ Expert knowledge on development pattern could be incorporated into inference via informative priors
- ▶ It is straightforward to blend in collateral information in the model inference

## Estimation

Estimation with a variance constraint:  $b_n > a_0 (= a_1 + \dots + a_n)$

This constraint ensures  $\text{Var}(S_{i,1:k})$  increases in  $k$ :

$$\text{Var}(S_{i,1:k}) = \frac{\left(\sum_{j=1}^k a_j\right) \left(a_0 + b_n - \sum_{j=1}^k a_j\right)}{(a_0 + b_n)^2 (a_0 + b_n + 1)} \phi_i^2.$$

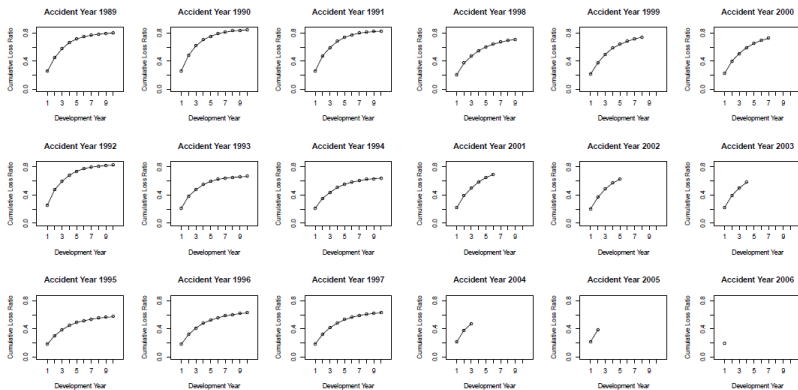
This constraint mimics a condition implied by the Chain-Ladder method: the variance in the cumulative paid loss ratio is increasing by development age.

# Data

Data from the NAIC schedule P:

- ▶ We examine the paid losses for worker's compensation
- ▶ The data of each individual company contain incremental paid losses for 18 accident years ( $m = 18$ ) from to 1989 to 2006, and for each accident year, losses are developed for the period of 10 years ( $n = 10$ ).
- ▶ Data are split into two parts
  - ▶ Upper triangle is used to develop model
  - ▶ Lower triangle is for validation

# Case Study Using One Insurer



(a) Fully developed claims

(b) Partially developed claims

## Case Study Using One Insurer

Frequentist approach: MLE Dirichlet  $\hat{a}_0/(\hat{a}_0 + 1) \approx 1$

Development Factor	10 accident years				18 accident years			
	Dirichlet Model		Mack Chain-Ladder		Dirichlet Model		Mack Chain-Ladder	
	Estimate	SE	Estimate	SE	Estimate	SE	Estimate	SE
$\gamma_{1:2}$	1.778	0.0138	1.779	0.0087	1.775	0.0175	1.781	0.013
$\gamma_{2:3}$	1.280	0.0055	1.281	0.0082	1.269	0.0072	1.269	0.006
$\gamma_{3:4}$	1.169	0.0040	1.169	0.0039	1.161	0.0049	1.160	0.003
$\gamma_{4:5}$	1.098	0.0029	1.098	0.0024	1.091	0.0034	1.090	0.003
$\gamma_{5:6}$	1.066	0.0025	1.066	0.0012	1.057	0.0026	1.057	0.002
$\gamma_{6:7}$	1.046	0.0023	1.046	0.0019	1.037	0.0020	1.037	0.003
$\gamma_{7:8}$	1.033	0.0021	1.033	0.0026	1.025	0.0017	1.025	0.002
$\gamma_{8:9}$	1.021	0.0020	1.022	0.0013	1.016	0.0014	1.016	0.002
$\gamma_{9:10}$	1.014	0.0023	1.014	0.0008	1.011	0.0012	1.010	0.001

## Case Study Using One Insurer

Comparison of reserve prediction:

		MLE Dirichlet Model (18 accident years data)				Hierarchical Bayes Dirichlet Model (18 accident years data)			
Acc Year	Actual Loss Ratio	95% Inter-val	Actual-Predicted	Interval contains actual	Interval Length	95% Inter-val	Actual-Predicted	Interval contains actual	Interval Length
1997	0.629	[0.629,0.629]	0.000	1	0.000	[0.629,0.629]	0.000	1	0.000
1998	0.719	[0.709,0.720]	0.004	1	0.011	[0.718,0.719]	0.000	1	0.001
1999	0.763	[0.749,0.765]	0.005	1	0.016	[0.763,0.765]	0.001	1	0.002
2000	0.767	[0.747,0.772]	0.006	1	0.025	[0.764,0.768]	0.001	1	0.004
2001	0.765	[0.736,0.767]	0.012	1	0.031	[0.757,0.763]	0.005	0	0.006
2002	0.741	[0.698,0.739]	0.022	0	0.041	[0.722,0.730]	0.015	0	0.008
2003	0.722	[0.699,0.752]	0.005	1	0.053	[0.723,0.735]	0.007	0	0.012
2004	0.705	[0.657,0.723]	0.014	1	0.066	[0.682,0.699]	0.014	0	0.017
2005	0.729	[0.676,0.771]	0.006	1	0.095	[0.715,0.743]	0.001	1	0.028
2006	0.629	[0.576,0.708]	0.013	1	0.132	[0.624,0.667]	0.016	1	0.043
Average			0.009	0.900	0.047		0.006	0.600	0.012

## Case Study Using One Insurer

Reserve prediction with variance constraints:

		MLE Dirichlet Model (18 accident years data)					Hierarchical Bayes Dirichlet Model (18 accident years data)				
Acc Year	Actual Loss Ratio	95% Inter-val	Actual-Predicted	Interval contains actual	Interval Length	95% Inter-val	Actual-Predicted	Interval contains actual	Interval Length		
1997	0.629	[0.629,0.629]	0.000	1	0.000	[0.629,0.629]	0.000	1	0.000		
1998	0.719	[0.712,0.722]	0.003	1	0.010	[0.713,0.722]	0.002	1	0.009		
1999	0.763	[0.752,0.768]	0.004	1	0.016	[0.754,0.769]	0.002	1	0.015		
2000	0.767	[0.751,0.774]	0.006	1	0.023	[0.754,0.774]	0.004	1	0.020		
2001	0.765	[0.740,0.768]	0.012	1	0.028	[0.745,0.771]	0.008	1	0.026		
2002	0.741	[0.702,0.739]	0.021	0	0.037	[0.710,0.740]	0.016	0	0.030		
2003	0.722	[0.705,0.754]	0.006	1	0.049	[0.712,0.751]	0.009	1	0.039		
2004	0.705	[0.661,0.724]	0.013	1	0.063	[0.671,0.721]	0.010	1	0.050		
2005	0.729	[0.682,0.770]	0.005	1	0.088	[0.698,0.776]	0.006	1	0.078		
2006	0.629	[0.577,0.716]	0.014	1	0.139	[0.603,0.718]	0.027	1	0.115		
Average			0.008	0.900	0.047		0.008	0.900	0.038		



## Case Study Using One Insurer

Some observations for this specific insurer:

- ▶ Both point and interval predictions are comparable between the CL and MLE Dirichlet model. Recall that  $\hat{\alpha}_0/(\hat{\alpha}_0 + 1) \approx 1$ .
- ▶ Additional 8 years fully developed claims data help improve prediction in terms of coverage probability. It is not true in general.
  - ▶ The insurer has stable underwriting criterion and business mix.
  - ▶ It focuses on assigned risk market.
- ▶ Prediction interval from the MLE is wider than the Bayesian approach, and variance constraint further improves the hierarchical model performance.

## Comparative Study Using Many Insurers

We focus on large insurers. Limit to earned premium  $\geq 10$  million dollars. This leaves us 139 insurers in the analysis.

Performance of prediction is assessed using out-of-sample validation, and we compute three metrics:

- ▶ Root mean squared error (RMSE)
- ▶ Coverage probability of the 95% prediction interval (Coverage)
- ▶ Average length of the 95% prediction interval (Length)

## Comparative Study Using Many Insurers

MLE Dirichlet Model:

- ▶ The usage of additional 8 years of claims data provide worse prediction
- ▶ Variance constraint improves coverage at the price of RMSE and interval length

AY	10-year Triangle					
	Unconstrained			Constrained		
	Coverage	Length	RMSE	Coverage	Length	RMSE
1998	0.950	0.037	0.007	0.942	0.061	0.015
1999	0.871	0.084	0.052	0.914	0.111	0.067
2000	0.871	0.102	0.059	0.892	0.130	0.083
2001	0.813	0.109	0.053	0.784	0.149	0.068
2002	0.763	0.114	0.057	0.799	0.152	0.080
2003	0.791	0.118	0.050	0.784	0.157	0.075
2004	0.791	0.135	0.059	0.849	0.182	0.081
2005	0.806	0.203	0.120	0.856	0.260	0.146
2006	0.871	0.417	0.219	0.849	0.464	0.225
Overall	0.836	0.147	0.075	0.852	0.185	0.093

## Comparative Study Using Many Insurers

Bayesian Inference with informative priors:

We employ prior knowledge on the expected unpaid loss ratio for the  $i$ th accident year:

$$\begin{aligned} & E(S_{i,m+2-i:n} | S_{i,1:m+1-i} = s_{i,1:m+1-i}) \\ &= \frac{\sum_{j=m+2-i}^n a_j}{\sum_{j=m+2-i}^n a_j + b_n} (\phi_i - s_{i,1:m+1-i}), \quad i = m - n + 2, \dots, m. \end{aligned}$$

Consider two different levels of uncertainty on the information:

(a)

$$E(S_{i,m+2-i:n} | S_{i,1:m+1-i}) \in [0.5(CLR_i - S_{i,m+2-i:n}), 1.5(CLR_i - S_{i,m+2-i:n})]$$

(b)

$$E(S_{i,m+2-i:n} | S_{i,1:m+1-i}) \in [0.9(CLR_i - S_{i,m+2-i:n}), 1.1(CLR_i - S_{i,m+2-i:n})]$$

## Comparative Study Using Many Insurers

Scenario #1: *CLR* is the actual cumulative loss ratio

AY	Scenario #1(a)			Scenario #1(b)		
	Coverage	Length	RMSE	Coverage	Length	RMSE
1998	1.000	0.045	0.005	1.000	0.035	0.001
1999	1.000	0.089	0.013	1.000	0.070	0.002
2000	1.000	0.116	0.019	1.000	0.088	0.003
2001	1.000	0.145	0.028	1.000	0.110	0.004
2002	1.000	0.172	0.036	1.000	0.129	0.005
2003	1.000	0.186	0.045	1.000	0.138	0.006
2004	1.000	0.247	0.062	1.000	0.182	0.007
2005	1.000	0.317	0.075	1.000	0.232	0.007
2006	1.000	0.543	0.069	1.000	0.374	0.004
Overall	1.000	0.207	0.039	1.000	0.151	0.004

## Comparative Study Using Many Insurers

Scenario #2: *CLR* is estimated from industry-level loss development factor Sherman and Diss (2005).

AY	Scenario #2(a)			Scenario #2(b)		
	Coverage	Length	RMSE	Coverage	Length	RMSE
1998	0.964	0.060	0.011	0.971	0.051	0.009
1999	0.942	0.105	0.024	0.950	0.087	0.018
2000	0.871	0.135	0.036	0.878	0.111	0.026
2001	0.863	0.165	0.064	0.906	0.133	0.054
2002	0.827	0.175	0.067	0.835	0.142	0.055
2003	0.842	0.182	0.062	0.914	0.147	0.043
2004	0.914	0.205	0.057	0.899	0.165	0.048
2005	0.906	0.226	0.069	0.655	0.181	0.081
2006	0.942	0.375	0.140	0.719	0.293	0.161
Overall	0.897	0.181	0.059	0.859	0.146	0.055

## Comparative Study Using Many Insurers

Scenario #3: *CLR* is estimated using growth curve model Clark (2003).

AY	Scenario #3(a)			Scenario #3(b)		
	Coverage	Length	RMSE	Coverage	Length	RMSE
1998	1.000	0.051	0.009	0.993	0.042	0.007
1999	0.957	0.092	0.021	0.950	0.076	0.017
2000	0.957	0.122	0.033	0.935	0.100	0.026
2001	0.914	0.146	0.054	0.892	0.119	0.048
2002	0.906	0.165	0.055	0.878	0.134	0.046
2003	0.957	0.186	0.059	0.986	0.151	0.038
2004	0.928	0.235	0.070	0.928	0.189	0.045
2005	0.914	0.314	0.115	0.935	0.250	0.091
2006	0.957	0.549	0.204	0.906	0.413	0.195
Overall	0.943	0.207	0.069	0.934	0.164	0.057

# Comparative Study Using Many Insurers

Comparison with existing methods:

- ▶ Mack Chain-Ladder
- ▶ Bootstrap Chain-Ladder
- ▶ Clark's growth curve
- ▶ GLM: Poisson, gamma, and Tweedie



# Comparative Study Using Many Insurers

AY	Mack Chain-Ladder			Bootstrap Chain-Ladder			Clark		
	Coverage	Length	RMSE	Coverage	Length	RMSE	Coverage	Length	RMSE
1998	0.446	0.011	0.007	0.971	0.042	0.014	0.921	0.032	0.007
1999	0.496	0.029	0.062	0.899	0.081	0.088	0.835	0.049	0.016
2000	0.619	0.045	0.068	0.885	0.092	0.097	0.799	0.063	0.024
2001	0.712	0.061	0.056	0.799	0.091	0.064	0.770	0.075	0.047
2002	0.691	0.074	0.056	0.827	0.098	0.071	0.885	0.087	0.045
2003	0.770	0.092	0.042	0.849	0.109	0.053	0.899	0.101	0.034
2004	0.856	0.134	0.061	0.878	0.133	0.074	0.906	0.125	0.044
2005	0.871	0.186	0.116	0.871	0.196	0.144	0.871	0.174	0.090
2006	0.835	0.582	0.219	0.856	0.398	0.267	0.899	0.353	0.196
Overall	0.699	0.135	0.076	0.871	0.138	0.097	0.865	0.118	0.056
AY	Tweedie $p = 1$			Tweedie $p = 2$			Tweedie $1 < p < 2$		
	Coverage	Length	RMSE	Coverage	Length	RMSE	Coverage	Length	RMSE
1998	0.871	0.036	0.007	0.604	0.019	0.009	0.777	0.025	0.008
1999	0.813	0.066	0.062	0.511	0.042	0.056	0.669	0.049	0.053
2000	0.899	0.077	0.068	0.633	0.056	0.081	0.705	0.060	0.071
2001	0.806	0.083	0.056	0.633	0.061	0.066	0.727	0.065	0.060
2002	0.784	0.092	0.056	0.734	0.075	0.066	0.727	0.072	0.060
2003	0.885	0.102	0.042	0.806	0.093	0.060	0.784	0.084	0.050
2004	0.849	0.128	0.061	0.871	0.137	0.085	0.799	0.112	0.071
2005	0.878	0.183	0.116	0.957	0.239	0.158	0.863	0.180	0.136
2006	0.871	0.361	0.219	0.935	0.524	0.248	0.863	0.378	0.229
Overall	0.851	0.125	0.076	0.743	0.138	0.092	0.768	0.114	0.082

## Conclusion

We proposed a stochastic loss reserving method based on Dirichlet distribution

- ▶ A new perspective to view CL and BF as inference issue
- ▶ Prediction from the Dirichlet model is a credibility weighted average of CL and expected payments
- ▶ Good performance was supported by comparison with existing methods using out-of-sample validation

For more details, check out our paper:

Sriram, K. and Shi, P. (2020+) Stochastic loss reserving: A new perspective from a Dirichlet model, *Journal of Risk and Insurance*.

## Conclusion

Thank you for your attention!!!

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