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Expected loss
(LEV)
$$\mathcal{E}[\mathcal{L} \wedge a] = \int_{0}^{a} \mathcal{S}(x) dx = \int_{0}^{a} x dF(x) + aS(a)$$



















Expected loss and premium by line and layer and total

$$\bar{L}_{i}(a) = E[X_{i}(a)] = \int_{0}^{a} E\left[\frac{X_{i}}{X}|X > x\right] S(x)dx = \int_{0}^{a} \alpha_{i}(x)S(x)dx$$

$$\bar{P}_{i}(a) = E_{g}[X_{i}(a)] = \int_{0}^{a} E_{g}\left[\frac{X_{i}}{X}|X > x\right] g(S(x))dx = \int_{0}^{a} \beta_{i}(x)g(S(x))dx$$

$$\bar{\beta}_{i}(x)$$

$$\alpha_{i}, \beta_{i} \text{ functions add-up: } \sum \alpha_{i}(x) = E\left[\frac{X_{1}+\dots+X_{n}}{x}|X > x\right] = 1$$

convex risk	
Expected loss and premium by	line and layer and total
Loss cost density $L_i(x) =$	$\alpha_i(x)S(x)$
Premium density $P_i(x) =$	$\beta_i(x)g(S(x))$
\Rightarrow Margin density $M_i(x) =$	$P_i(x) - L_i(x)$
=	$\beta_i(x)g(S(x)) - \alpha_i(x)S(x)$
Integrate density to get total	Assumptions
Everything you need to price!	 Price with g
 All quantities add-up 	 Equal priority in default
 Not an arbitrary allocationno choices 	Independence of X_i not required
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		_		line	Thick	Thin	total	
Moon	5000	5000	10000	stat				
cv	0 364418	0 101493	0 189144	EPD	0.001107	0.00027622	0.00069138	
Skew	2.40723	0.158277	2,1551	Loss Ratio	4994.5	4998.6	9993.1	
EmpSkew	2.4055	0.158277	2.15259	Margin	843.44	66.28	909.72	
P99.0	11645	6240	16712	Premium	5837.9	5064.9	10903	
P99.5	13212	6384	18274	P/S Ratio	0.90642	1.9066	1.1985	
P99.99	24537	7067	29578	Equity	6440.6	2656.6	9097.2	
MeanErr	-4.73138e-07	-1.22125e-15	-4.88351e-07	ROE	0.13096	0.02495	0.1	
CVErr	-2.41911e-05	2.28706e-14	-3.92099e-05					
 Exa pacl pip i Agg port CF 	mple produ kage <u>https:</u> install aggre regate port	rced using a //github.com egate folio specifi	aggregate F n/mynl/aggr ication:	 Pricin 2000 transf P + G (P - L) orm 10 cv 20 	g result) assets orm = 1090 _) / Q = mixed	s calibrate , p=0.997 (3 + 9097 (10903 - sig 0.3	ed to 10% 7, using a = 20000 9993) / 90	o return at Wang 097 = 0.1



