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CAS Ratemaking and Product Management Seminar

GLM II

March 21, 2011

A Case Study in Claims Management

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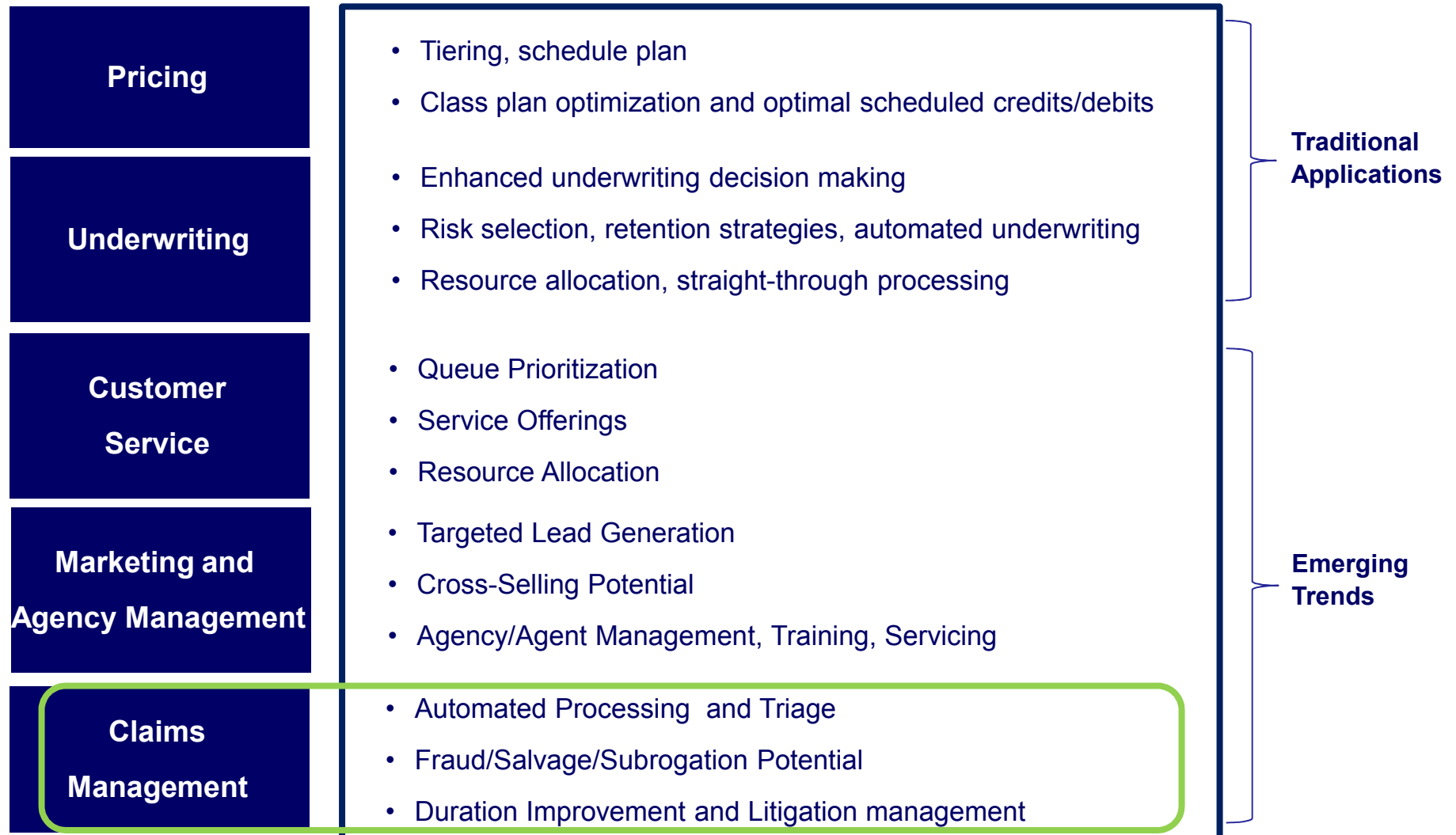
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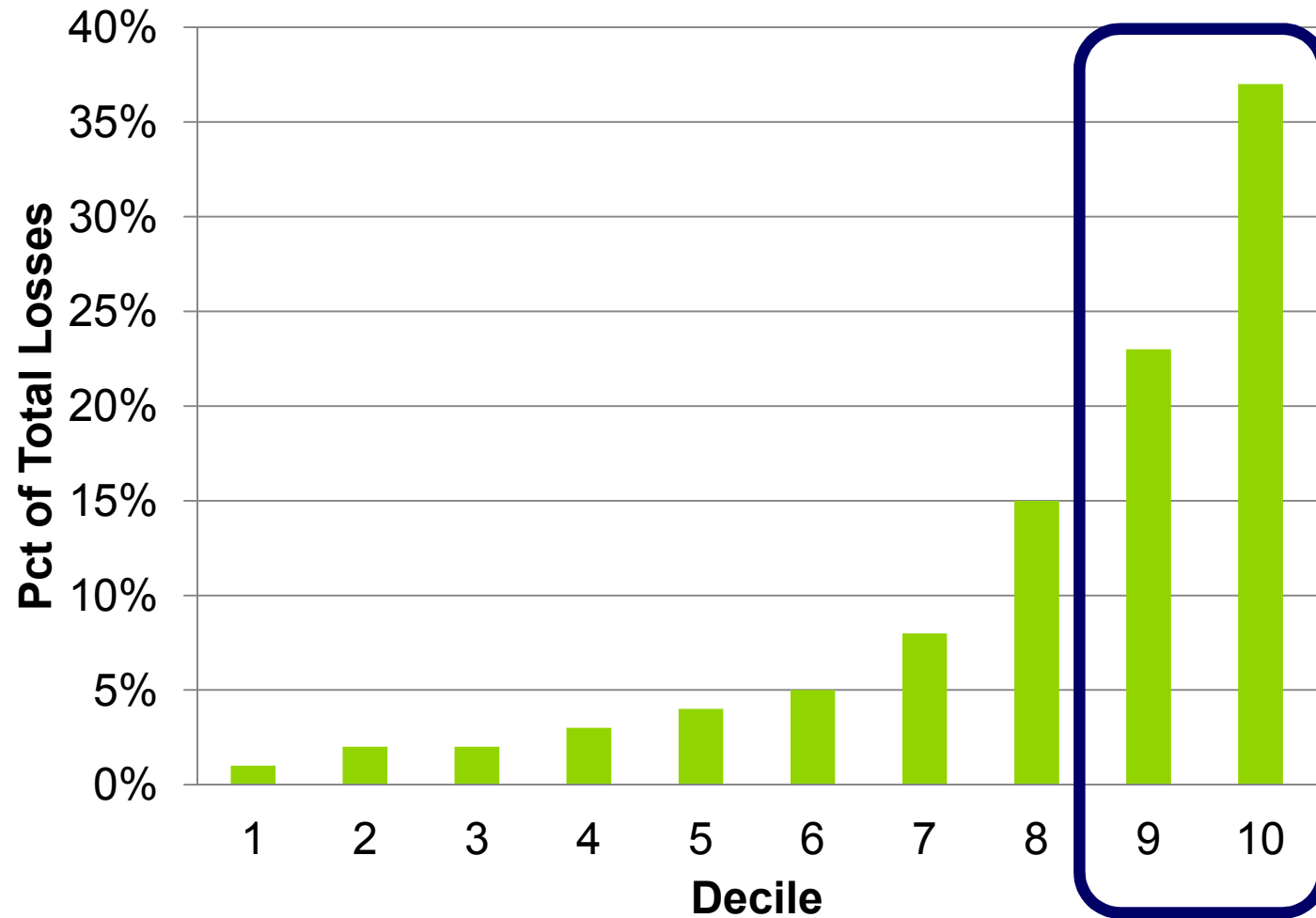
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GLMs in the insurance
industry...





The structure of a GLM...

The general structure of a Generalized Linear Model is:

$$\mu_i = E [Y_i] = g^{-1} (\sum X_{ij} \beta_j + \xi_i)$$

$$\text{Var} [Y_i] = \Phi V(\mu_i) / \omega_i$$

What is typically being modeled in claims management?

$$\mu_i = E [Y_i] = g^{-1} (\sum X_{ij} \beta_j + \xi_i)$$

$$\text{Var} [Y_i] = \Phi V(\mu_i) / \omega_i$$

- Ultimate severity
- Closing duration
- Propensity for fraud
- Propensity for litigation
- Propensity for salvage/subrogation recovery
- Litigation expenses
- Propensity to explode
- ...and more

The link function:

$$\mu_i = E [Y_i] = g^{-1} (\sum X_{ij} \beta_j + \xi_i)$$

$$\text{Var} [Y_i] = \Phi V(\mu_i) / \omega_i$$

- The link function “g” is differentiable and monotonic
- Typically, log link functions ($g(x) = \ln(x)$ or $g^{-1}(x) = e^x$) are used for severity, expense, duration to allow for a multiplicative effect
- Logit link function ($g(x) = \ln(x/1-x)$ or $g^{-1}(x) = e^x / 1 + e^x$) for propensity to litigation, fraud, or recovery

Predictive variables:

$$\mu_i = E [Y_i] = g^{-1} (\sum X_{ij} \beta_j + \xi_i)$$

$$\text{Var} [Y_i] = \Phi V(\mu_i) / \omega_i$$

- Predictors will eventually determine how good a model is
- Internal data across many departments can be predictive (claimant, policy information, etc.)
- A wide range of external 3rd party data is also available (geo-demographic, financial, etc.)

The Offset:

$$\mu_i = E [Y_i] = g^{-1} (\sum X_{ij} \beta_j + \xi_i)$$

$$\text{Var} [Y_i] = \Phi V(\mu_i) / \omega_i$$

If the effect of a predictive variable is known \rightarrow don't estimate its β and introduce the offset term.

General examples of offset in the claims space include:

- None
- State effect
- Etc...

The variance function:

$$\mu_i = E [Y_i] = g^{-1} (\sum X_{ij} \beta_j + \xi_i)$$

$$\text{Var} [Y_i] = \Phi V(\mu_i) / \omega_i$$

Target	Link	Error
Ultimate severity	Log	Gamma/Tweedie
Closing duration	Log	Gamma
Propensity for fraud	Logit	Binomial

Prior weights:

$$\mu_i = E [Y_i] = g^{-1} (\sum X_{ij} \beta_j + \xi_i)$$

$$\text{Var} [Y_i] = \Phi V(\mu_i) / \omega_i$$

Prior weight are used to assign known credibility to each data point:

- Typically 1
- Can vary by loss year, claim class, etc.
- Can be very creative but be wary of results (validate by cross-sections)

The modeling dataset...

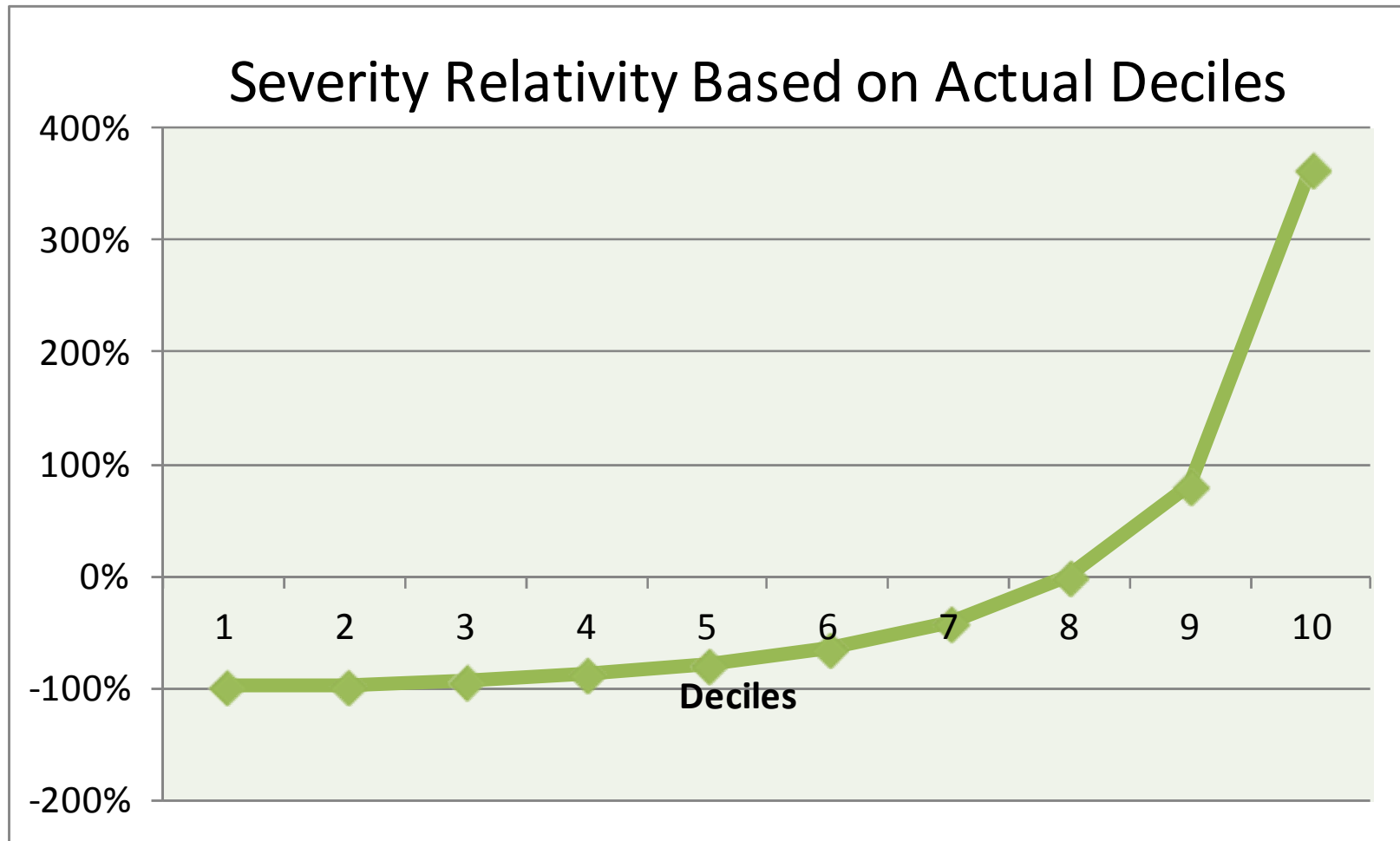
Modeling dataset:

1. Workers' compensation – Lost time indemnity severity
2. Severity was trended and appropriately adjusted
3. Year used 2002-2007
4. Data points used 30,000 closed claims
5. CWOP pay claims were excluded
6. Predictive variables include:
 1. Claims data
 2. Claimant information
 3. Injury details
 4. Employment data
 5. External data

Get to know your response
variable...

Distribution of the observed response variable: WC LTI severity

Quartile 4	\$1,000,000	←	Consider capping
Quartile 3	\$23,000		
Quartile 2	\$3,500		
Quartile 1	\$700		
10%	\$400		
5%	\$100		
1%	\$0	←	Consider Zeroing-out / excluding
0% Min	\$-20		
Mean	16,000		



Get to know *your* predictors...

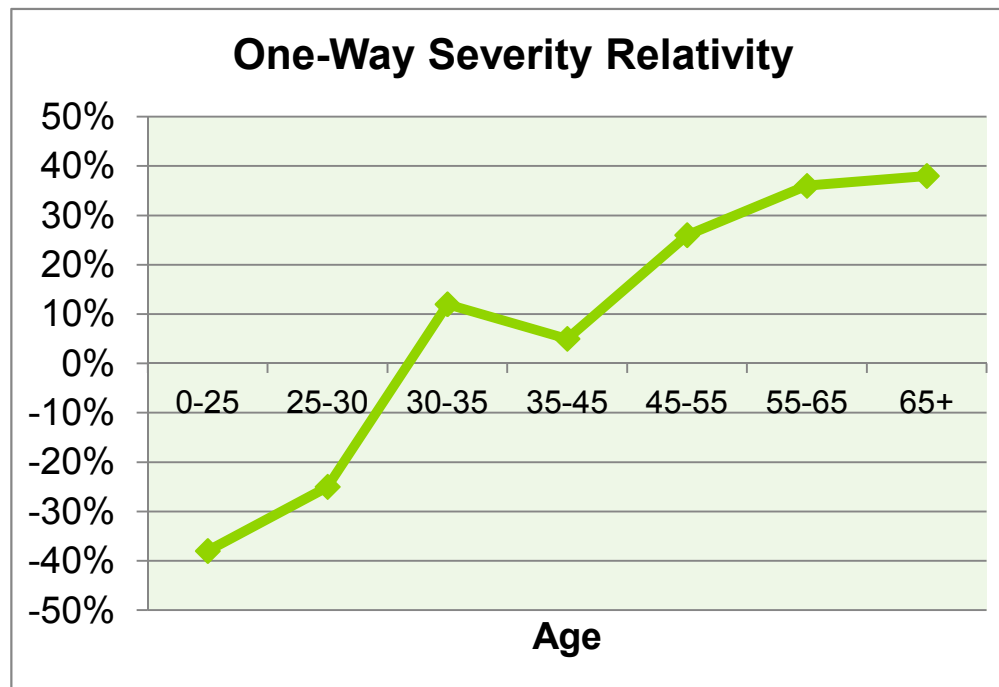
In general, predictors should be tested on the following prior to modeling:

- Variable distribution
- Level of missing values and their meaning
- Variable transformation (grouping, cap max, etc.)

Age	Claim Count
0-25	4,234
25-30	4,266
30-35	5,498
35-45	6,411
45-55	4,514
55-65	3,217
65+	1,748
Missing	112

In general, predictors should be tested on the following prior to modeling:

- Correlation with the response variable
- Correlation with predictors and principal components



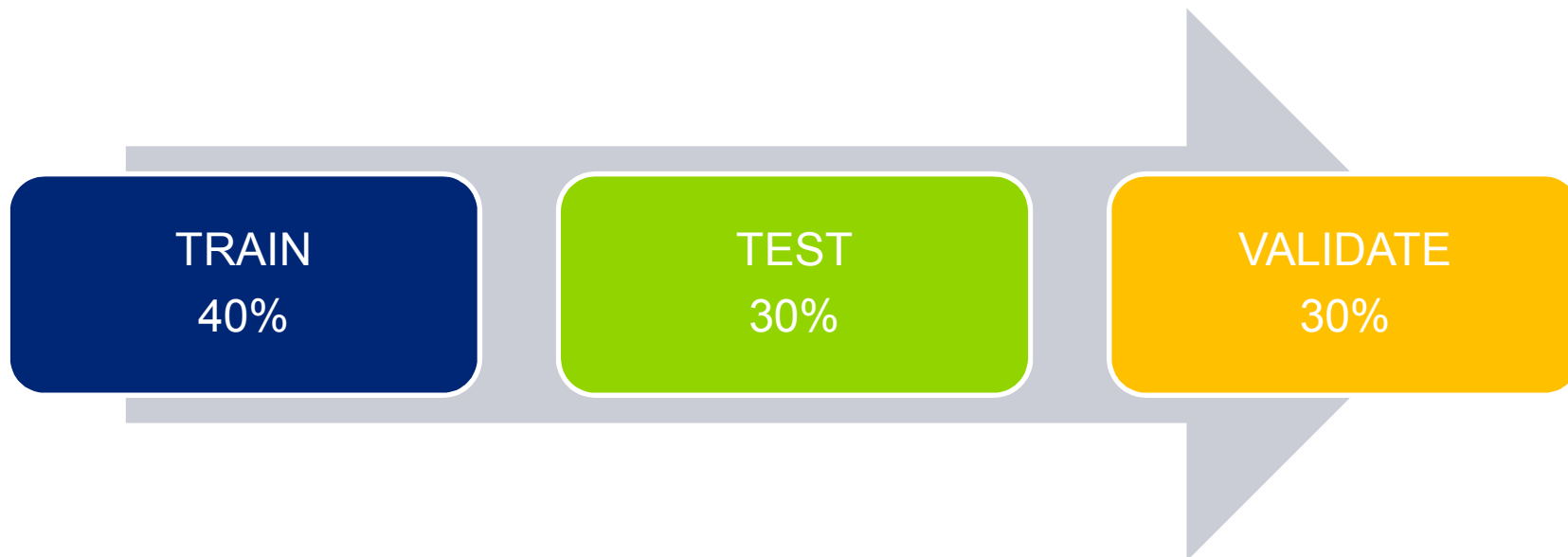
In general, predictors should be tested on the following prior to modeling:

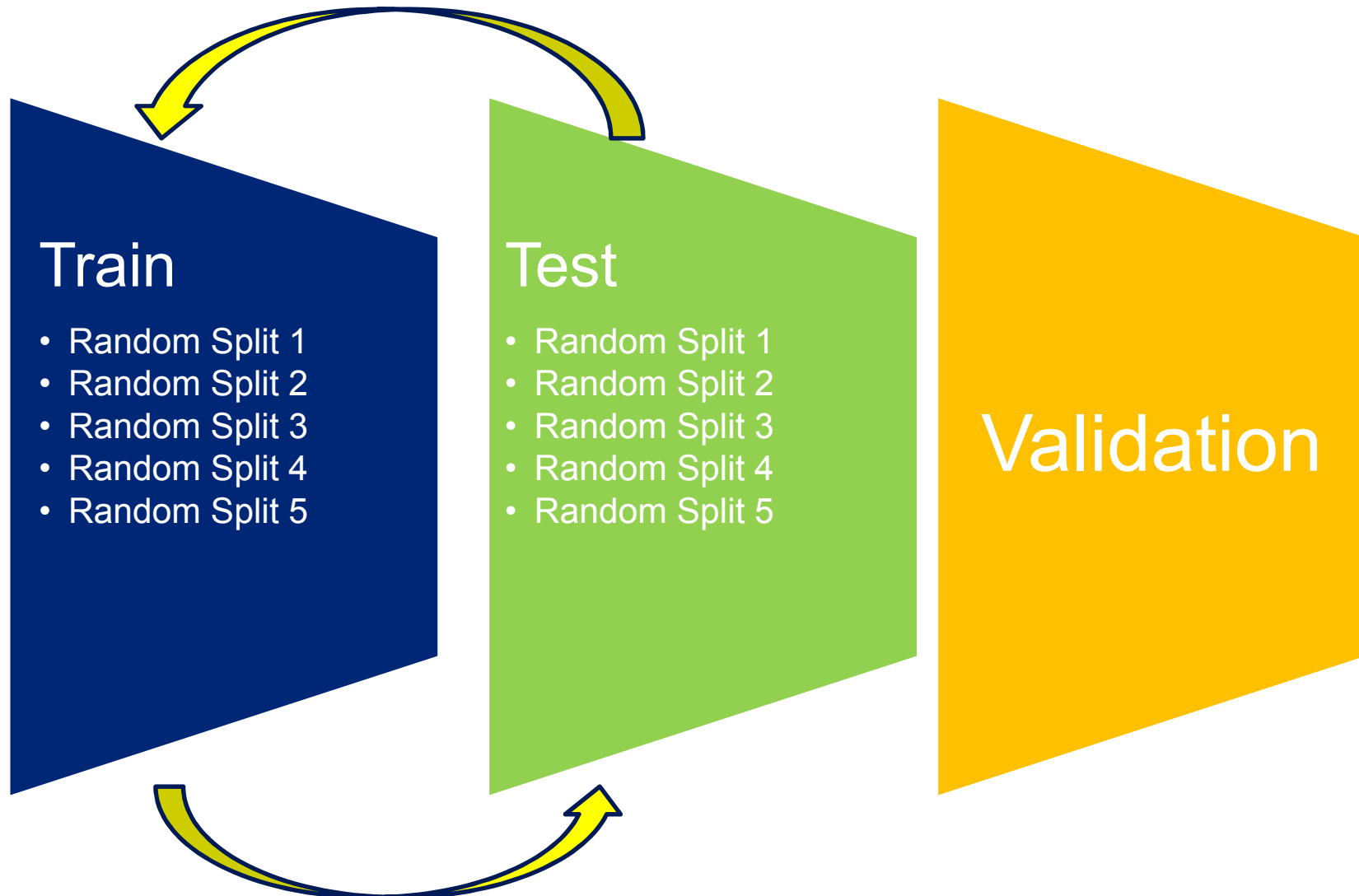
- Business meaning and usability
- Legal and regulatory limitations
- Availability and limitation in production
- Changes over time

Begin the modeling
exercise...

Modeling parameters used:

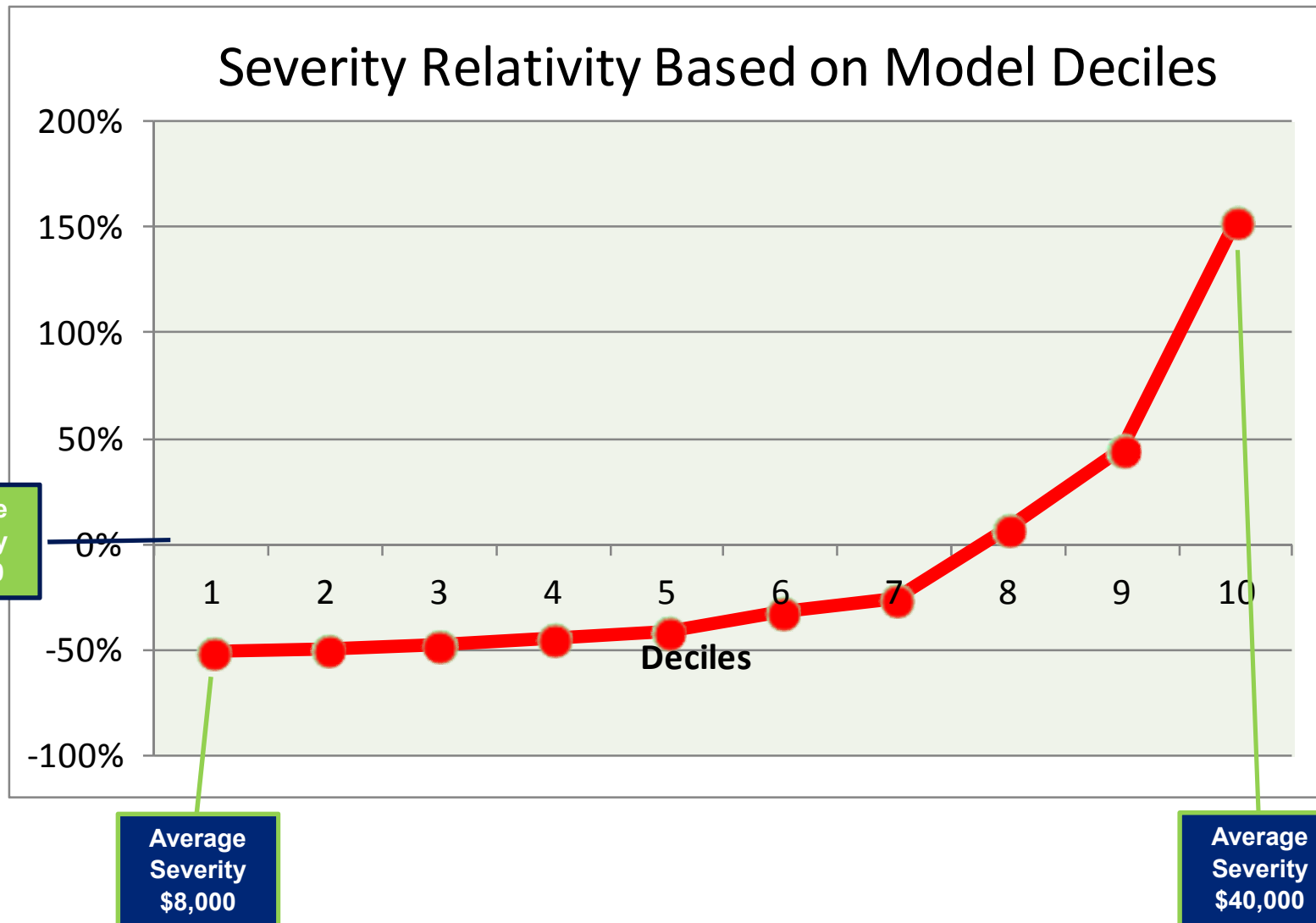
Response Variable	Link	Error	Weight	Offset
Ultimate LTI Severity	Log	Gamma	1	N/A

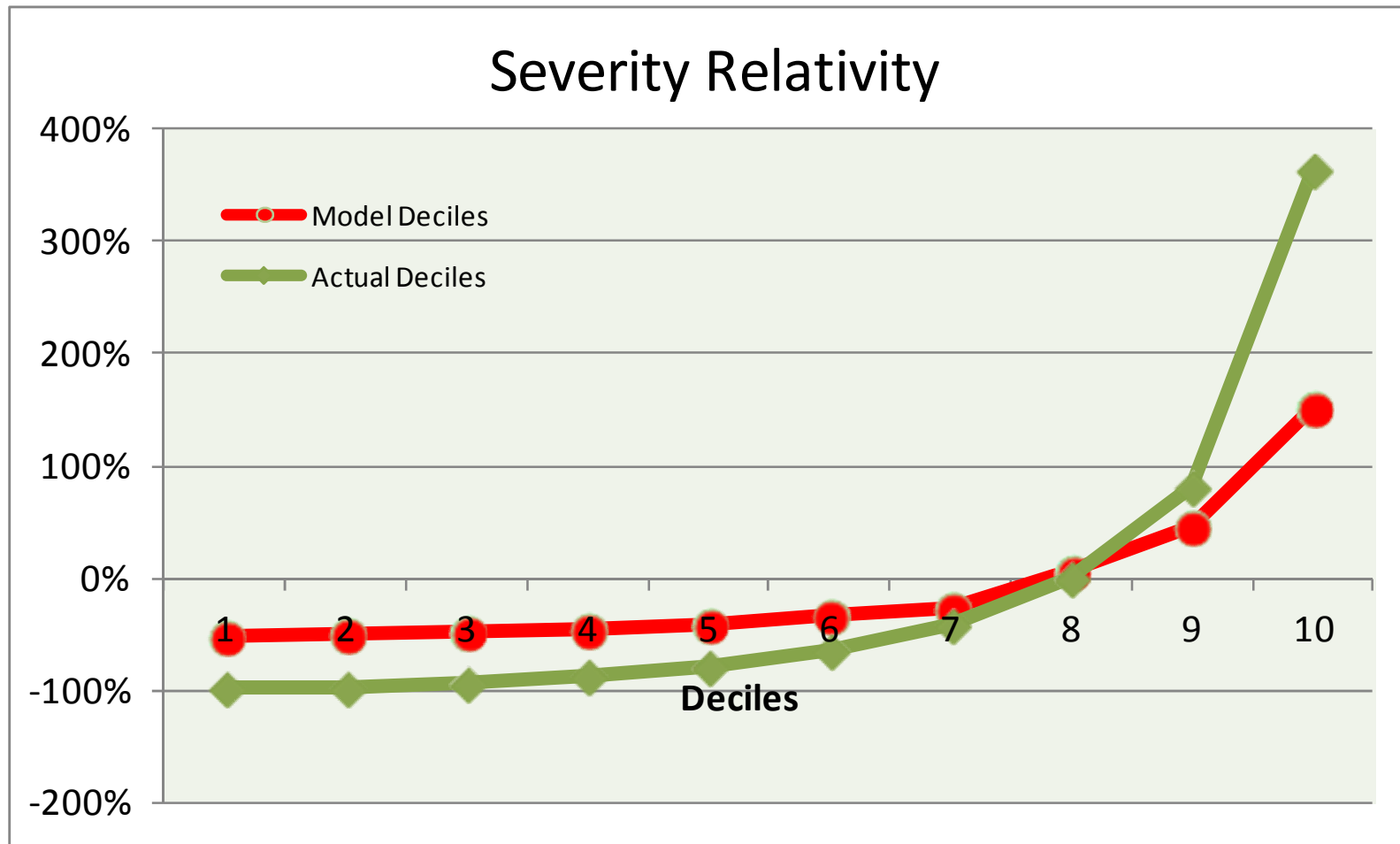




A sample modeling output:

Variable	PE RS 1	ChiSq RS 1		PE RS 5	ChiSq RS 5
$X_1 = \text{Age}$	1.20	74	...	1.19	77
$X_2 = \text{Lower Back Injury}$	0.75	53	...	0.69	53
$X_3 = \text{Afternoon Injury}$	-0.63	48	...	-0.61	47
X_4	0.54	3355	32
X_5	-0.41	21	...	-0.46	21
...			...		
$X_{40} = \text{Missing Indicator for Census Data}$	0.11	1	...	0.09	2





Post Modeling...

After modeling is complete:

- Implement
- Monitor
- Enhance
- Expand



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