



**CAS Ratemaking & Product Mgmt Seminar**  
**Severe Weather Workshop:**  
*Using Cat Bonds to Develop Risk Loads*

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**Using Cat Bonds to Develop Risk Loads**

**Discussion Topics:**

- § History of Homeowners Ratemaking
- § Introduction of the Profit Multiple
- § Background of New Risk Load Methodology
- § Overview of Catastrophe Bonds
- § Catastrophe Bond Data – The Profit Multiple
- § Application of the Profit Multiple

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**History of Homeowners Ratemaking**

- § Hurricane Andrew made landfall in South Florida on August 24, 1992
- § The amount of devastation & insured loss was a dramatic wake-up call for property insurers and actuaries

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### Audience Participation – Question 1

In comparing Homeowners and Auto insurance, which of the following statements do you agree with most?

- A. The amount of Profit / Risk Load should be similar
- B. The amount of Profit / Risk Load for Auto should be more than Homeowners
- C. The amount of Profit / Risk Load for Auto should be significantly more than Homeowners
- D. The amount of Profit / Risk Load for Homeowners should be more than Auto
- E. The amount of Profit / Risk Load for Homeowners should be significantly more than Auto

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### History of Homeowners Ratemaking

- § Homeowners Insurance has large variation in Loss Ratio from year to year
- § Existence of potential mega-catastrophes significantly increases variation
- § Potential losses in a single year are many times a single year's premium
- § Significant amounts of capital are exposed to mega-catastrophe events
- § We have developed a method for quantifying a risk load to account for the large amount of capital required to cover potential insured losses in catastrophe prone areas

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### The Profit Multiple

#### In catastrophe bond data:

- §  $YS = \text{Yield Spread} = \text{Bond Yield} - \text{LIBOR}$
- §  $EL = \text{Expected Loss (based on catastrophe models)}$
- §  $EER = \text{Expected Excess Return} = YS - EL$
- §  $\text{Profit Multiple} = EER/EL$

#### In a reinsurance contract:

- §  $\text{Profit Multiple} = (\text{Reinsurance Premium} - EL) / EL$

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### Audience Participation – Question 2

§ Assume you're reviewing a reinsurance contract with a Profit Multiple of 2.0

§ What is the expected loss ratio of the reinsurer?

- A. Greater than 80%
- B. 60%-80%
- C. 40%-60%
- D. 20%-40%
- E. Less than 20%

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### Answer (Q2)

Expected Loss Ratio (ELR) =  $1 / (PM + 1)$

$$\begin{aligned} \text{ELR} &= 1 / (2 + 1) \\ &= 1 / 3 \\ &= 33.3\% \end{aligned}$$

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### Audience Participation – Question 3

Given the following:

- Cat Reinsurance Cover for hurricane losses in Texas
- Reinsurance Layer is 100% of \$636 Million excess of \$1,600 Million
- Expected Covered Losses = \$19.5 Million
- Attachment Probability = 3.5%
- Exhaustion Probability = 2.5%

What is the expected loss ratio for the reinsurers issuing this reinsurance?

- A. Greater than 80%
- B. 60%-80%
- C. 40%-60%
- D. 20%-40%
- E. Less than 20%

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### Audience Participation – Question 4

- Assume further that the Rate-on-Line is 17%

**What is the expected loss ratio for the reinsurers issuing this reinsurance?**

- A. Greater than 80%
- B. 60%-80%
- C. 40%-60%
- D. 20%-40%
- E. Less than 20%

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### Answer (Q4)

$$\begin{aligned} \text{Reinsurance Premium} &= \text{Reinsured Layer} \times \text{ROL} \\ &= \$636 \text{ M} \times 17\% = \$108.12 \text{ M} \end{aligned}$$

$$\begin{aligned} \text{ELR} &= \text{EL} / \text{Reinsurance Premium} \\ &= \$19.5 \text{ M} / \$108.12 \text{ M} = 18.0\% \end{aligned}$$

*Ø Is there any reason that primary insurers should charge less than reinsurers for the risk of losing large amounts of capital to losses caused by catastrophic events?*

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### Background – New Risk Load Methodology

#### Objective

- *To describe a new methodology for quantifying the cost of exposing capital to large catastrophic events*

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## Background – Profit Provision in Ratemaking

§ Traditional Ratemaking for Property Insurance

$$\hat{u} P = (L + FE) / (1 - VER - Pr)$$

§ Essentially the same level of profit is generated for each dollar of expected loss and expense

§ Alternative Methodology

$$\hat{u} P = (L_{nc} + FE) / (1 - VER - Pr) + L_c / (1 - VER) + \text{Risk Load}$$

Note:  $L_{nc}$  = Non-cat & non-modeled cat losses

$L_c$  = Modeled cat losses above 1-in-5 year event

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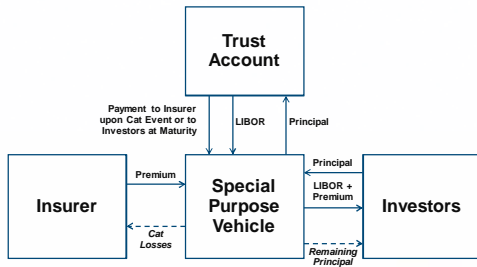
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## Overview of Cat Bonds – How They Work



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## Overview of Cat Bonds – Important Concepts

Included in Cat Bond data:

- **Probability of First Loss (PFL)**
- **Yield Spread** (Risk Premium) = Bond Yield – LIBOR
- **Expected Value of Loss (EL)**
- **Expected Excess Return (EER)** = Yield Spread – EL

Calculated by Milliman:

- **Profit Multiple** = EER / EL

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## Overview of Cat Bonds – Sample Data

| Year | Month | Amount (in \$ Mil) | Probability of First Loss | Yield Spread | Expected Loss | Expected Excess Return | Profit Multiple |
|------|-------|--------------------|---------------------------|--------------|---------------|------------------------|-----------------|
| 2010 | Dec   | 80                 | 8.74%                     | 16.63%       | 6.24%         | 10.39%                 | 1.67            |
| 2010 | May   | 90                 | 7.35%                     | 14.19%       | 4.97%         | 9.22%                  | 1.86            |
| 2010 | Dec   | 65                 | 5.84%                     | 12.93%       | 4.77%         | 8.16%                  | 1.71            |
| 2010 | Nov   | 100                | 2.56%                     | 6.34%        | 1.67%         | 4.67%                  | 2.80            |
| 2010 | Dec   | 50                 | 2.12%                     | 7.35%        | 1.48%         | 5.87%                  | 3.97            |
| 2010 | May   | 250                | 1.99%                     | 8.36%        | 1.66%         | 6.70%                  | 4.04            |
| 2010 | Jul   | 96                 | 1.76%                     | 7.10%        | 1.47%         | 5.63%                  | 3.83            |
| 2010 | May   | 185                | 1.07%                     | 6.59%        | 0.97%         | 5.62%                  | 5.79            |
| 2010 | Dec   | 100                | 0.88%                     | 5.07%        | 0.55%         | 4.52%                  | 8.22            |
| 2010 | Oct   | 100                | 0.69%                     | 3.80%        | 0.52%         | 3.28%                  | 6.31            |

Source: Lane Financial LLC, Annual Securitization Reviews



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## The Profit Multiple – What is it?

**Profit Multiple** = Expected XS Return / Expected Loss

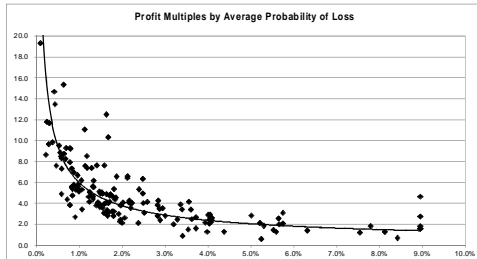
- The compensation the investor requires to expose their capital to catastrophe losses
  - ↳ *This is exactly the same risk faced by direct writers for the retained portion of catastrophe risk*
- Instead of relating reinsurance costs to the layer of coverage (ROL), the Profit Multiple uses a risk-related value in the denominator (expected losses in the layer)
- Increases as the layer of catastrophe cover increases (i.e. probability of loss decreases)



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## Profit Multiple – Relation to Loss Probability

*All Cat Bonds Issued on U.S. Exposures: 2006 - 2012*



Source: Lane Financial LLC, Annual Securitization Reviews



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## Profit Multiple – Application #1

### 1. Develop Risk Load for Catastrophe Exposure

- ü Define the layers (Reinsurance Layers, PMLs, etc.)
- ü Allocate the gross losses from each event into the layers
- ü Gross Risk Load = Expected Loss in Layer x Profit Multiple
- ü Risk Load on Retained Losses:
  - Split the gross losses into ceded and retained by applying reinsurance contracts to each event
  - Risk Load for Retained Catastrophe Exposure = Net Loss in Layer x Profit Multiple

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## Profit Multiple – Application #2

### 2. Estimate Reinsurance Premiums

- ü Can quickly calculate estimated reinsurance premiums for any potential reinsurance contract
- ü Indicated Rate-on-Line =  
 $(\text{Indicated Risk Load} + \text{Expected Loss}) / \text{Size of Layer}$
- ü Can be easily compared to actual Rate-on-Line in quoted or purchased reinsurance contracts

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*Spreadsheet Demonstration*

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### Audience Participation – Question 5

Going back to Question 3, given the following:

- Reinsurance Layer is 100% of \$636 Million excess of \$1,600 Million
- Expected Covered Losses = \$19.5 Million
- Attachment Probability = 3.5%
- Exhaustion Probability = 2.5%

If a primary insurer elected to retain the exposure described above, what would be the indicated Risk Load required by that company based on the Cat Bond methodology?

- A. Greater than \$60 million
- B. \$40-60 million
- C. \$30-40 million
- D. \$20-30 million
- E. Less than \$20 million

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### Answer (Q5)

**Risk Load** = Expected Loss in Layer x Profit Multiple  
= \$19.5 M x  $\int_a^b 0.45364 y^{-0.52591} dy / (b-a)$   
(where a = 3.5% and b = 2.5%)  
= \$19.5 M x 2.88  
= \$56.14 M  
(compared to traditional profit provisions of 5-10%,  
which result in only \$1-2 M of profit)

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### Audience Participation – Question 6

Using the same information ...

- Reinsurance Layer is 100% of \$636 Million excess of \$1,600 Million
- Expected Covered Losses = \$19.5 Million
- Attachment Probability = 3.5%
- Exhaustion Probability = 2.5%

What is the indicated Rate-on-Line for the reinsurance layer described above?

- A. Greater than 20%
- B. 16-20%
- C. 13-16%
- D. 10-13%
- E. Less than 10%

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### Answer (Q6)

**Indicated Rate-on-Line =**

(Indicated Risk Load + Expected Loss) / Size of Layer

= (\$56.14 M + \$19.5 M) / \$636 M

= \$75.64 M / \$636 M

= 11.9%

(compared to the quoted Rate-on-Line of 17.0%)

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### Audience Participation – Bonus Question

**Using similar information ...**

- Reinsurance Layer is **80%** of \$636 Million excess of \$1,600 Million
- Expected Covered Losses = \$19.5 Million
- Attachment Probability = 3.5%
- Exhaustion Probability = 2.5%

**What is the indicated Risk Load on the primary insurer's *retained* exposure based on the Cat Bond methodology?**

- A. Greater than \$15 million
- B. \$12-15 million
- C. \$10-12 million
- D. \$8-10 million
- E. Less than \$8 million

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### Answer (Bonus)

**Retained Risk Load =**

Net Loss in Layer x Profit Multiple

= (\$19.5 M x 20%) x 2.88

= \$11.23 M

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## Questions?

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