## Catastrophe Model Blending

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# Why Blend Models

- Significant impact of cat models since 1990s.
  - Used in primary rate making (hurricane, earthquake ratings, reinsurance cost allocation, Net Cost of Reinsurance, Risk Provision, Catastrophe Tier Relativities, etc.)
  - Used in Reinsurance to calculate expected losses for pricing contracts
  - Used to calculated overall level of accumulation of risks for multiple perils for both insurers and reinsurers
  - Used for rating agency reporting, capital management, underwriting, Enterprise Risk Management, etc.

# Why Blend Models

- Significant degree of uncertainties associated with the models
  - Large range of outputs
  - Poor perception of accuracy
  - Science is still evolving, big changes from year to year

## Why Blend Models



# Why Blending Models

- Allow companies to include multiple views, reduce the model risk that results from relying on a single vendor model's opinion.
  - Complexity of the models, numerous assumptions and judgments involved in model development
  - Lack of historical records to judge which model is the best
  - Big changes are not necessarily bad
- Smooth out the large changes of individual model, mitigate the output uncertainties

#### Rating Agency Views on Model Blending

- S&P: In the wake of widespread disaster-related losses for insurers and reinsurers, ratings firm S&P has reiterated its call for the use of multiple catastrophe models. In a press release, S&P said it preferred use of models from at least two of the big three modelling firms when assessing the catastrophe risk for natural peril catastrophe bonds. S&P says its criteria still allows the use of a single model when assessing catastrophe risk, but contends that using multiple models would increase transparency in the market and lower the risk of "model shopping" where risk managers purposely select the model that gives them the most desirable results.
- AM Best: When companies provide output from multiple catastrophe models, A.M. Best's baseline approach is to take the straight average. This, however, can be adjusted to a weighted average in cases where more refined information is available that supports greater reliance being placed on a given model. In either case, A.M. Best expects a company's management to be able to explain why it has utilized the output selected to best represent its catastrophe exposure.

# Blending Methods

- Two major model outputs: AAL, PML/Tvar
- Different blending methods for different output
- Major blending methods:
  - Severity Blending (PML, TVar)
  - Frequency Blending (PML, AAL, TVar)
  - Simple or Weighted Average of Pure Premium (AAL) is consistent with both Frequency and Severity Blending
- Most of the time, the results from different blending methods won't be the same

# Severity Blending

- Model A gives \$3 Billion for the 100 Year PML, Model B gives \$4 Billion for the same return period loss, then the 50-50 severity blend for the 100 year PML is \$3.5 Billion.
- Advantages: Simple, different blending weight can be easily implemented
- Disadvantages:
  - Break the coherent and correlations of cat model events
  - Subsequent simulations (reinsurance pricing, annual aggregation, etc.) relying on the rank order of the events are impossible

# Severity Blending

| Exceedance |         |         | Severity |  |
|------------|---------|---------|----------|--|
| Prob       | Model A | Model B | Blending |  |
| 0.1%       | 3,952   | 6,345   | 5,149    |  |
| 0.2%       | 3,161   | 5,054   | 4,107    |  |
| 0.4%       | 2,559   | 3,890   | 3,224    |  |
| 0.5%       | 2,290   | 3,537   | 2,914    |  |
| 1.0%       | 1,623   | 2,529   | 2,076    |  |
| 2.0%       | 1,083   | 1,683   | 1,383    |  |
| 4.0%       | 653     | 1,018   | 836      |  |
| 5.0%       | 550     | 844     | 697      |  |
| 10.0%      | 273     | 414     | 344      |  |
| 20.0%      | 97      | 146     | 122      |  |
| 50.0%      | 5       | 3       | 4        |  |



# Frequency Blending

- Frequency is adjusted through simulations
- Sampling years from different models
  - Method 1: Sample from each of model A and B for certain percentage of years
  - Method 2: for each simulation year, sample from each model based on weight
- Broadly used for reinsurance, and risk management purposes.
- Requires the event loss table with probabilities associated with each event.

# Frequency Blending

#### **Before Blending**

|         | Model A | Model A<br>Prob. | Model B | Model B<br>Prob |
|---------|---------|------------------|---------|-----------------|
| Event 1 | 5,000   | 0.001            | 3,504   | 0.001           |
| Event 2 | 4,986   | 0.001            | 3,494   | 0.001           |
| Event 3 | 4,875   | 0.004            | 3,300   | 0.004           |
| Event 4 | 4,591   | 0.004            | 3,218   | 0.004           |
| Event 5 | 4,400   | 0.01             | 2,900   | 0.01            |
| Event 6 | 4,200   | 0.02             | 2,700   | 0.02            |
| Event 7 | 3,121   | 0.02             | 2,189   | 0.02            |



### After Blending

| Event Loss         | Prob   |
|--------------------|--------|
| 5,000              | 0.0005 |
| 4,986              | 0.0005 |
| 4,875              | 0.002  |
| 4,591              | 0.002  |
| 4,400              | 0.005  |
| 4,200              | 0.01   |
| 3,504              | 0.0005 |
| <mark>3,494</mark> | 0.0005 |
| <u>3,300</u>       | 0.002  |
| 3,218              | 0.002  |
| 3,121              | 0.01   |
| 2,900              | 0.005  |
| <mark>2,700</mark> | 0.01   |
| <mark>2,189</mark> | 0.01   |

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# Frequency Blending

- Advantages:
  - It utilizes the simulation approach
  - It outputs event sets for accumulation, helping to reflect dependencies and correlations between portfolios
  - Event sets allows calculations of reinsurance recoveries and reinstatement premiums
  - The blended outputs can be fed directly into capital models for ERM

#### Challenge of Frequency Blending

- How to vary weight by region and retain the correlations for events impacting multiple regions
- After correlation is broken, annual aggregation will also fail. The application of companywide reinsurance treaty becomes difficult
- Frequency blending requires advanced statistics and programming skills and deeper understanding of models

# Challenges of Frequency Blend



### Simple/Weighted Average of Loss Cost

- Simple or weighted average of loss cost from different models.
- It is in line with Frequency and Severity Blending
- It can be achieved directly from model output, so the re-simulations of events is not required
- Commonly used in rate making where event loss table and probability of exceedance curve information are not needed.
- Easy to implement and explain to regulators

#### Selecting Weight by Model Validation

- Review of Model Assumptions
  - Frequency, severity, vulnerability assumptions
  - Geographic relativities
  - Relying on model documentation, modelers submission in different jurisdictions
  - Using notional portfolio to conduct reasonability checks

### Selecting Weight by Model Validation

#### Understand the variations of model assumptions

|          | Northeast - Long Term Catalog |       |       |       |       |  |
|----------|-------------------------------|-------|-------|-------|-------|--|
|          | Cat 1                         | Cat 2 | Cat 3 | Cat 4 | Cat 5 |  |
| Model A  | 0.058                         | 0.033 | 0.020 | 0.003 | 0.000 |  |
| Model B. | 0.084                         | 0.039 | 0.020 | 0.003 | 0.000 |  |
| Model C  | 0.075                         | 0.040 | 0.025 | 0.001 | 0.000 |  |
| Model D  | 0.046                         | 0.046 | 0.028 | 0.003 | 0.000 |  |

|         | Florida - Long Term Catalog |       |       |       |       |  |  |
|---------|-----------------------------|-------|-------|-------|-------|--|--|
|         | Cat 1                       | Cat 2 | Cat 3 | Cat 4 | Cat 5 |  |  |
| Model A | 0.266                       | 0.157 | 0.145 | 0.066 | 0.012 |  |  |
| Model B | 0.258                       | 0.143 | 0.117 | 0.048 | 0.013 |  |  |
| Model C | 0.299                       | 0.137 | 0.149 | 0.083 | 0.008 |  |  |
| Model D | 0.313                       | 0.107 | 0.175 | 0.078 | 0.019 |  |  |

Source: ISCM 2012 RAA Cat Modeling Model Comparison ٠

### Compare model assumptions with historical





#### Selecting Weight by Model Validation

- Company Specific information
  - Historic events comparison
  - Year to year comparison
  - Comparison of results to other models
  - Reasonableness of relationship among various output results
  - Sensitivity of variations in user input
- Select weighting based on model validation and statistics matrix

# Historical Comparison

| Hurricane | Exposure           | Actual Loss | Modeled loss |  |
|-----------|--------------------|-------------|--------------|--|
| Charley   | 22,275,499,438     | 63,929,684  | 105,175,085  |  |
| Frances   | 8,964,552,161      | 56,919,397  | 31,591,909   |  |
| Ivan      | Ivan 7,352,146,112 |             | 33,776,550   |  |
| Jeanne    | 10,715,233,657     | 11,622,619  | 24,153,389   |  |
| Wilma     | 43,154,867,167     | 127,121,023 | 122,399,529  |  |
| Katrina   | 7,674,691,708      | 5,968,809   | 13,379,694   |  |
| Total     | 100,136,990,243    | 286,688,528 | 330,476,156  |  |

Note: All the exposures and losses have been multiplied by a single constant to disguise the identity of clients.

• Source: AIR Florida 2013 Submission

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## Model Testing

Comparison # 3 Hurricane = Wilma Exposure = total (Personal Residential)

| Company M   | Actual         |            |               | Modeled        |            |               |
|-------------|----------------|------------|---------------|----------------|------------|---------------|
| Company M E | Exposure       | Loss       | Loss/Exposure | Exposure       | Loss       | Loss/Exposure |
| Frame       | 3,760,549,046  | 868,620    | 0.000231      | 3,760,549,046  | 718,275    | 0.000191      |
| Masonry     | 14,965,517,560 | 12,629,237 | 0.000844      | 14,965,517,560 | 11,261,073 | 0.000752      |
| Total       | 18,726,066,606 | 13,497,857 | 0.000721      | 18,726,066,606 | 11,979,348 | 0.000640      |

Note: All the exposures and losses have been multiplied by a single constant to disguise the identity of the client.

#### Comparison # 4 Hurricane = Charley Exposure = total (Personal Residential)

| Common 1   | Actual        |                          |               | Modeled       |                          |               |
|------------|---------------|--------------------------|---------------|---------------|--------------------------|---------------|
| Company J  | Exposure      | Loss                     | Loss/Exposure | Exposure      | Loss                     | Loss/Exposure |
| Coverage A | 5,974,756,996 | 55,998,569               | 0.009373      | 5,974,756,996 | 40,842,729               | 0.006836      |
| Coverage C | 2,119,645,760 | 3,897,835                | 0.001839      | 2,119,645,760 | 4,781,987                | 0.002256      |
| Coverage D | 584,167,359   | 1,388, <mark>1</mark> 13 | 0.002376      | 584,167,359   | 1,8 <mark>44,0</mark> 20 | 0.003157      |
| Total      | 8,678,570,114 | 61,284,517               | 0.007062      | 8,678,570,114 | 47,468,736               | 0.005470      |

Note: All the exposures and losses have been multiplied by a single constant to disguise the identity of the client.

#### • Source: AIR Florida 2013 Submission

# **Blending Beyond Basics**

- Model morphing means changing shape. In model morphing, one wants to change some aspect of model A to resemble that of model B, typically, because of implementation difficulties in using both models.
- Model fusion is akin to building one's own model based on own experience and expertise.

# **Blending Beyond Basics**

- Blending with own loss experience
  - Determine if there is bias by a specific model
  - If there is a bias, then develop a model miss factor
  - Historical information is not enough to calibrate tail distribution
  - Cautions
    - Don't over fit
    - Does the historical information truly reflect the tail? Consider combining multiple distributions.
    - Not recommended for developing loss cost in rate filings

# Challenges of Blending

- It is subjective
- The limitations of statistics stability vs. state of the art science
- False sense of security Blending doesn't eliminate the model uncertainty
- Resource and expertise

#### Model Blending Reduce Uncertainty



Source: Guy Carpenter & Company, LLC

## Summary

- Blending models allow companies to include multiple views of the model.
- Blending will mitigate the model uncertainties but will not eliminate the uncertainties.
  Blending may introduce new uncertainties into the process.
- Blending models requires deep understanding and extensive testing of models.

