

**2005 CAS Seminar on Predictive Modeling** 

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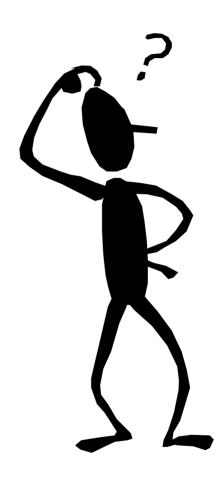
**Watson Wyatt Worldwide** 





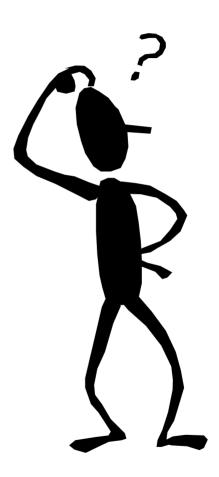
# **Retention analysis**

- What to measure
- What to consider
- Practical tips
- Why do it



# **Retention analysis**

- What to measure
- What to consider
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- Individual policy (or quote) level
- Offer & resulting accept/lapse
- Policy characteristics
- Rate change information
- Period during which rates changed



#### **Generalized linear models**

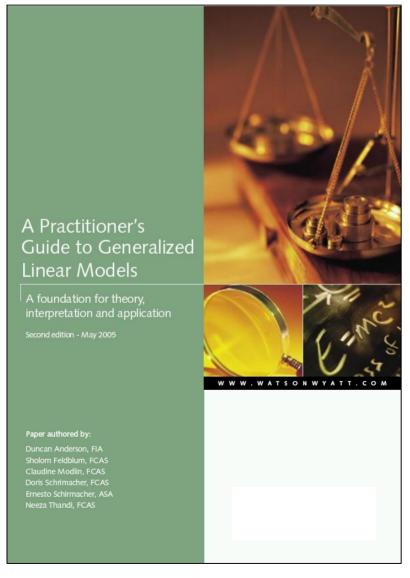
$$E[Y] = \mu = g^{-1}(X.\beta + \xi)$$

$$Var[Y] = \phi.V(\mu) / \omega$$

- Consider all factors simultaneously
- Allow for nature of random process
- Provides diagnostics
- Robust and transparent

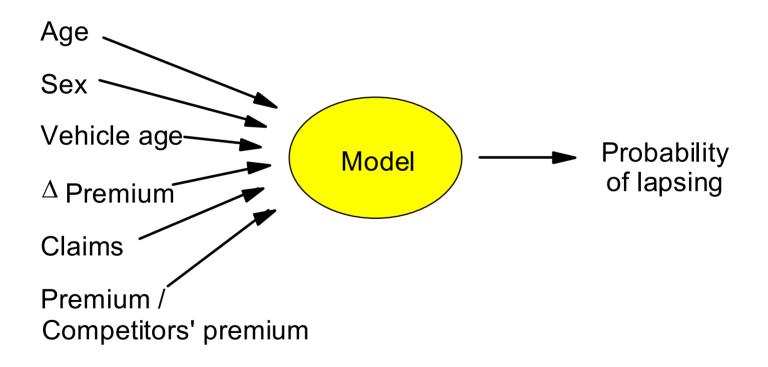


# "A Practitioner's Guide to Generalized Linear Models"



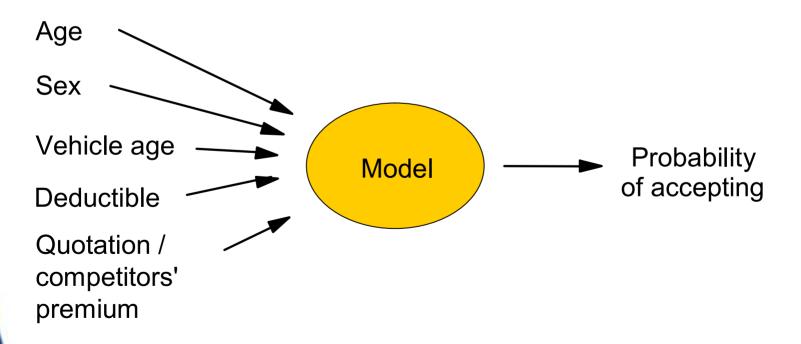
### **Modeling retention**

Most companies have data on renewal offers



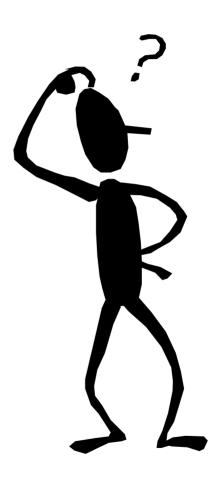
### Modeling new business rates

- If details of individual quotes known, can be modeled in similar way
- Otherwise much simpler analysis is all that can be undertaken



### **Retention analysis**

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#### What to consider

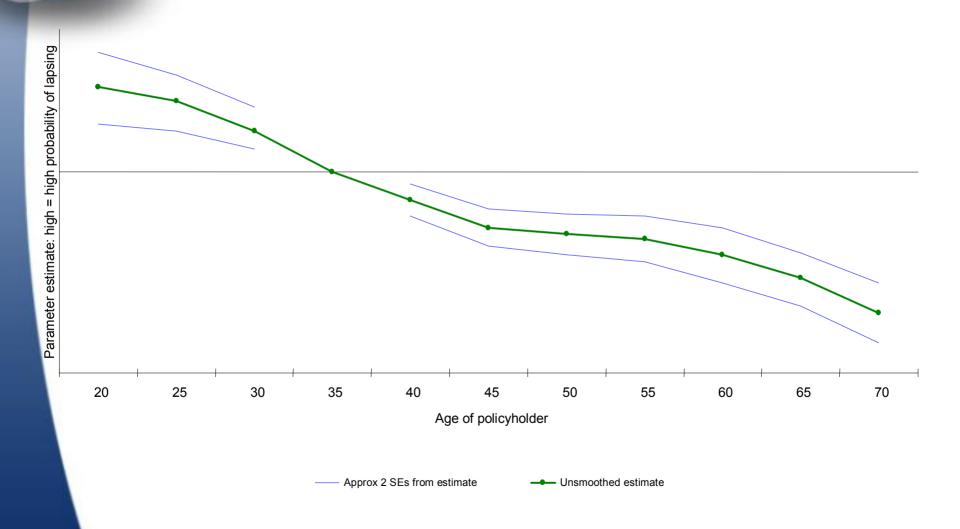
- Who are your customers
- How do you connect
- What have you done to them
- What have others done to them

# Who are your customers?

- Age of policyholder
- Age of car
- Claims history
- Other rating factors
- Endorsement activity



#### Effect of age of policyholder on lapses



# How do you connect with them?

- Distribution channel
- Payment plan
- Other products held
- Endorsement activity
- # years with company

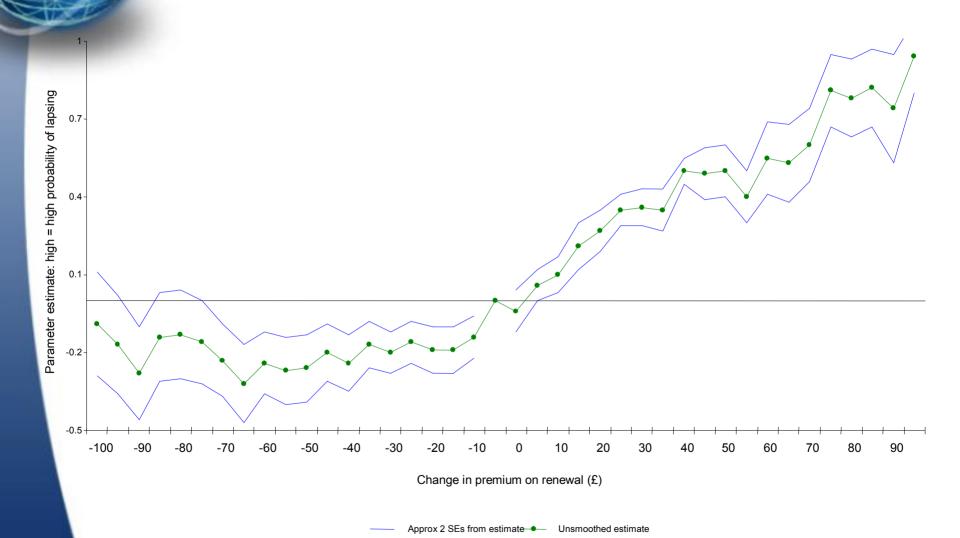


### What have you done to them?

- Rate change
- Claims service
- Agent service

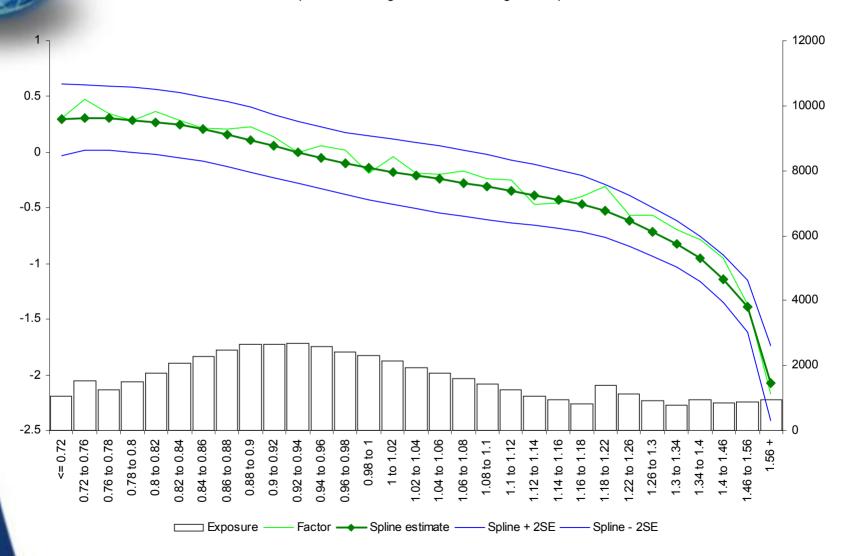


### **Effect of premium change on lapses**



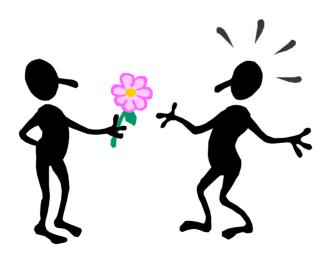
#### **Splines**

Effect of premium change on renewal using cubic splines



#### What have others done to them?

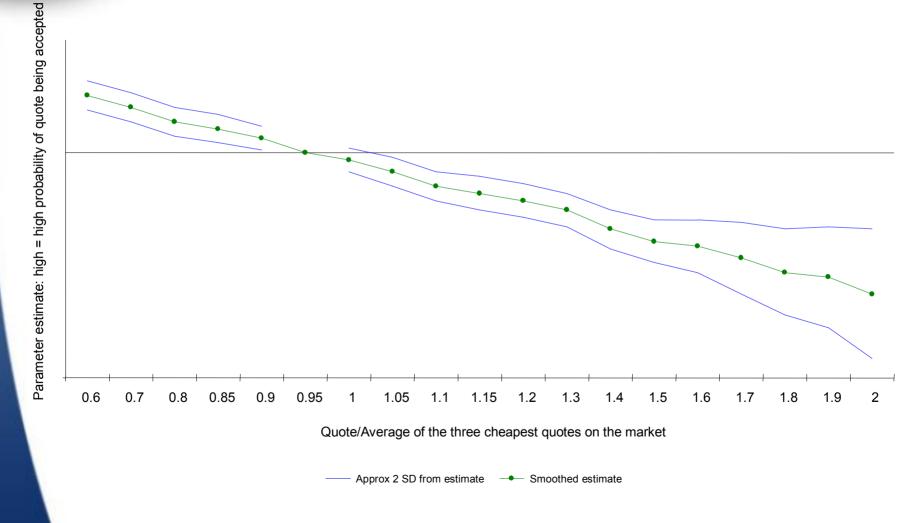
- Competitors' premium
- Product differentiation (may not be applicable to some products)



### **Competitive indices**

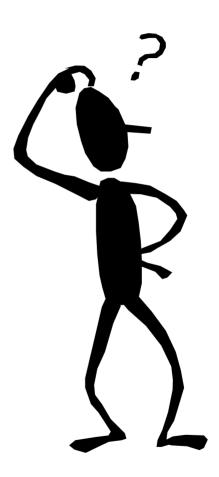
- For modeling, required at individual policy level
- Sources of competitor info
  - rate manuals
  - comparative rating software
- Measures
  - index (comparing to one competitor or averaged across several)
  - rank of quote relative to competitors
- Challenges
  - tier criteria
  - point in time
  - cost

#### **Effect of competitiveness on new business**



### **Retention analysis**

- What to measure
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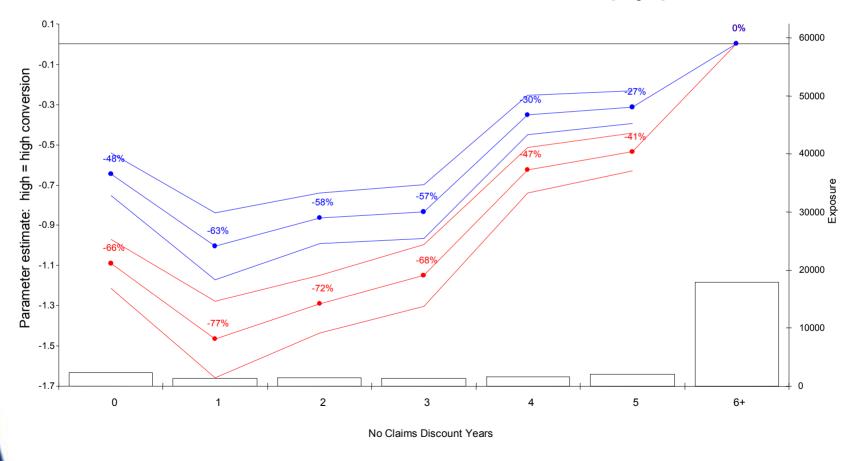


### Statistical assumptions

- A logistic model is most appropriate
  - considers log( p / [1-p] ) and binomial error
  - maps [0,1] to  $[-\infty,\infty]$
  - invariant to whether you measure lapse/renew
- If lapses are low and results not to be used directly, a Poisson multiplicative model can help
  - theoretically wrong (can predict multiple lapses), but:
  - easier to understand
  - can superimpose one-way results more easily

### Practical tip on competitiveness

Superimposing models with and without competitiveness will show extent to which effects are simply price related



Without competitiveness in model With competitiveness in model

### **Beware absolute premium**

- GLM shows effect all other factors being equal
- For varying premium all other factors are never equal
- Results, while statistically correct, can be hard to interpret, for example adding premium size can reverse the multivariate result for age of driver
- Consider fitting separate models for different premiums bands



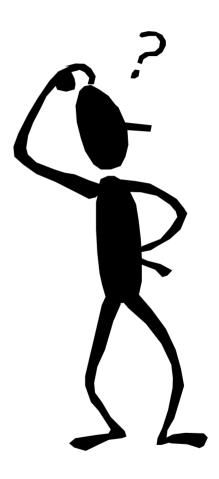
- Best to have more than one rate change in data
- Investigate % change and \$ change
- Suggest fit rate change as a categorical factor and then model with splines if appropriate
  - some results are straight lines in logistic space, some are clearly not

### **Beware expectations**

- Customer expectations of premium change
  - try to isolate rate change from risk criteria change which affects premium
  - consider premium change adjusted for change in risk criteria (ie new rates for new risk / old rates for new risk)

# **Retention analysis**

- What to measure
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### Why model lapses / new business?

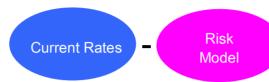
- Qualitative management decisions
  - marketing strategies
  - renewal campaigns
- Simple expense loadings
- Modeling
  - simple lifetime modeling
  - detailed impact modeling
  - detailed lifetime modeling
  - price optimization



#### **Customer value**



Low



High

High

Retention Lapse model

 $\mathsf{Low}$ 

Target marketing at these

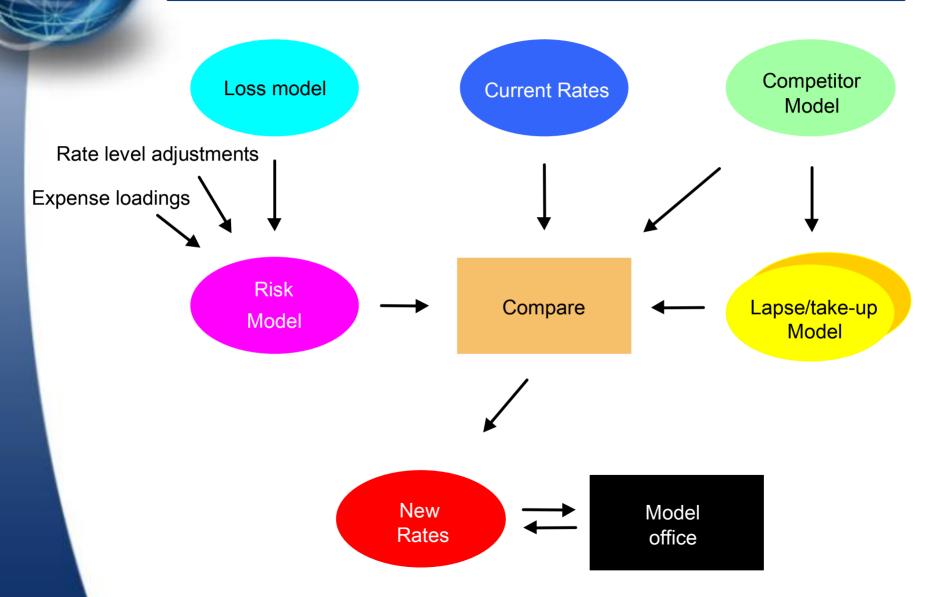
Increase premiums

Actively target at renewal (discount vouchers / phone calls)

# Lifetime expense loads

- Expenses per policy
  - acquisition 100
  - renewal30
- Expected lifetime
  - youngyears
  - old5 years
- Lifetime expense loadings
  - young (100 + 1 \* 30)/2 = 65
  - old (100 + 4 \* 30) / 5 = 44

# **Price optimization**





- How do we use information from retention models and claims models to change rates optimally?
- Which is more important overall rate changes or relativity changes?
- How quickly and for what types of policyholder should we move the rates to the theoretical position?
- What might happen if I do X?

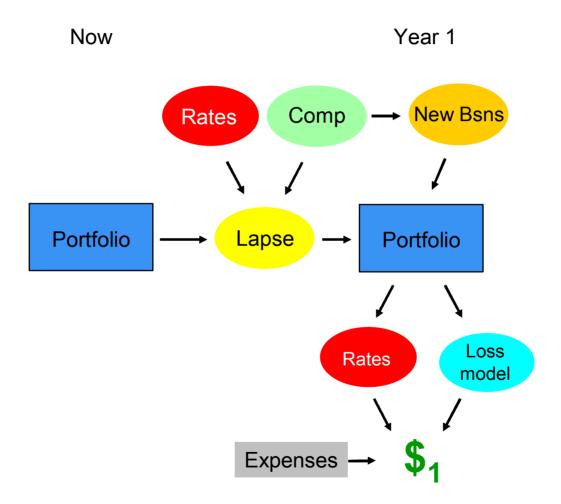


- Given all this information, what is the "best" rating action?
- Given a form of rating structure, seek the parameters which maximize a company's strategic objectives, perhaps with defined constraints

### **Ingredients**

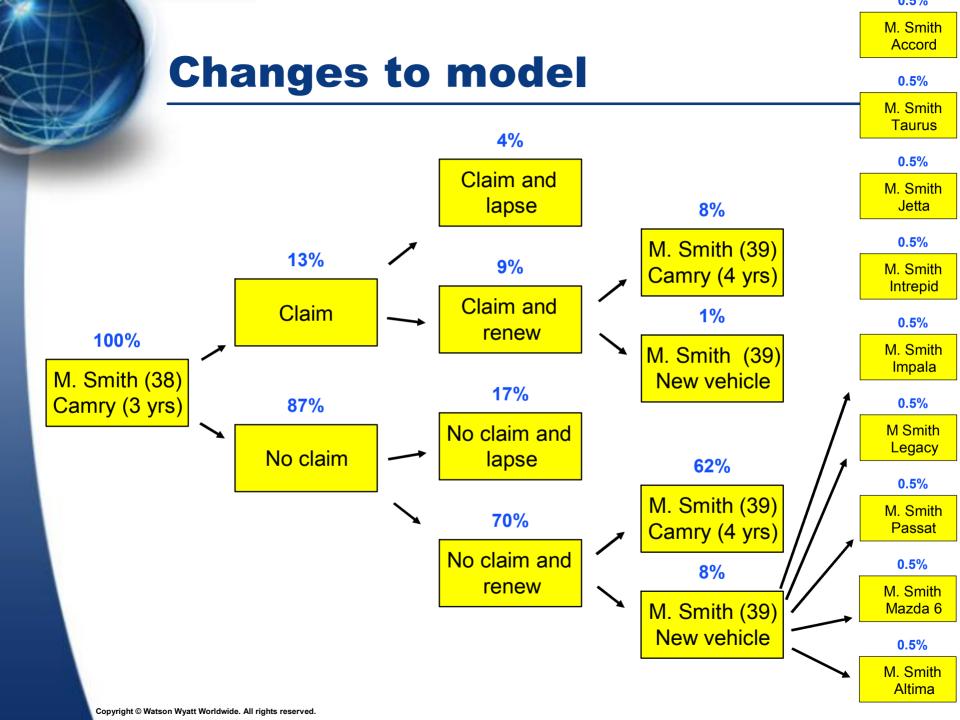
Data **Current Rates** Portfolio now Competitor **Assumptions** Expenses Model New business **GLMs** Lapse model Loss model model **Test** New Rates

### **Scenario testing**



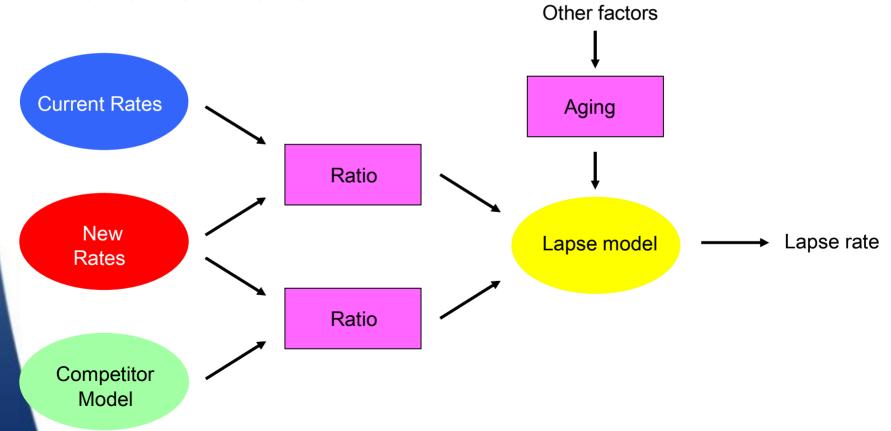
# **Problems (1)**

- What will the competition do?
- Things change
  - age of insured
  - age of vehicle (home)
  - vehicle (home)
  - address
  - claim surcharges
- What is the measure of success?
- Over what period is the projection done?

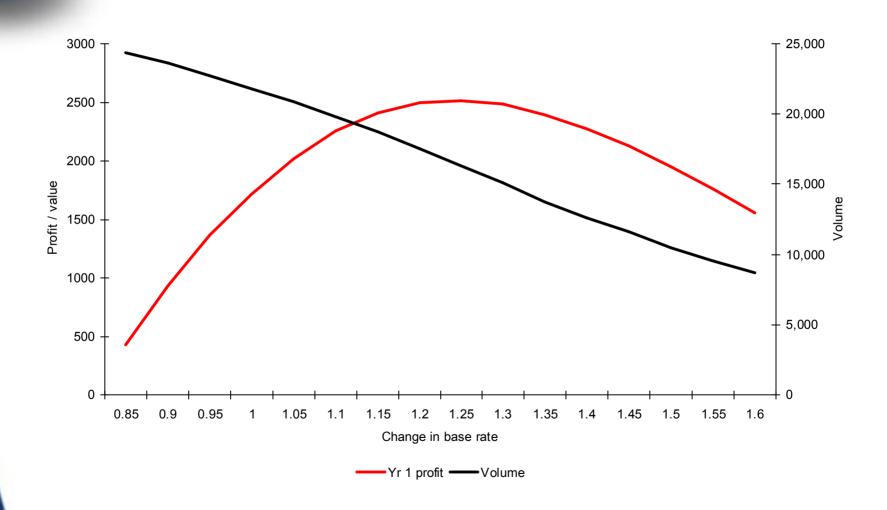


# Inputs to some models are outputs from others

Sometimes model output needs to be processed and/or recategorized before being input to another model



# **Example - effect of different base rate changes**

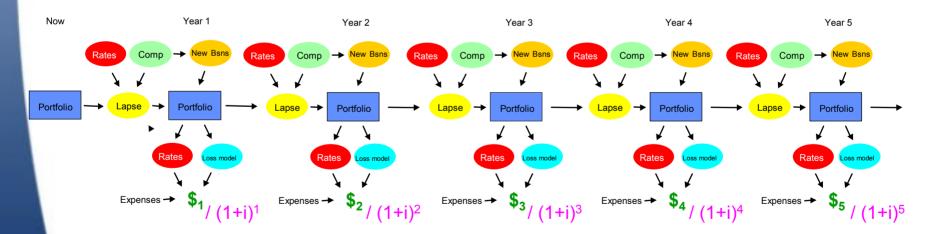


### **Problems (2)**

- What are we optimizing?
  - Year 1 profit will not consider value business in the future
  - Putting on a life actuary's hat ...
- Seek "a<sub>x</sub>"
  - two big drivers of retention are age and tenure => people get stickier
  - expected life higher than 1/(1-r)
  - but multiply by what profit measure?
  - and account for future rating actions how?

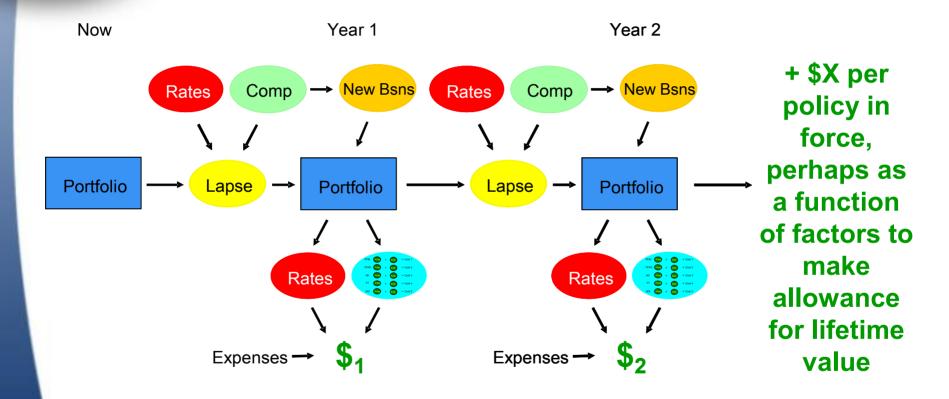
#### Problems (2)

- What are we optimizing?
  - Year 1 profit will not consider value business in the future
  - Putting on a modern life actuary's hat...



Too many assumptions - (things change)<sup>5</sup>

### A pragmatic compromise?



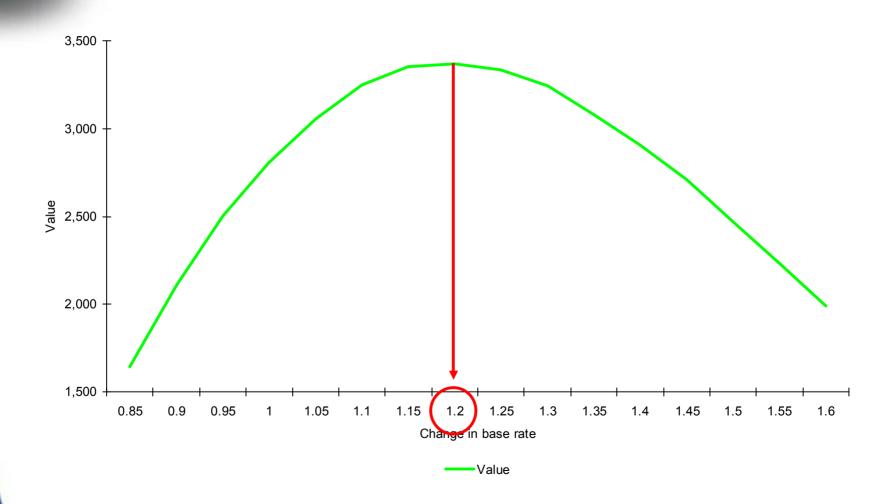


- Constrained optimization
- Seek to maximize profit over short period, subject to constraints such as minimum required business volumes

#### **Examples**

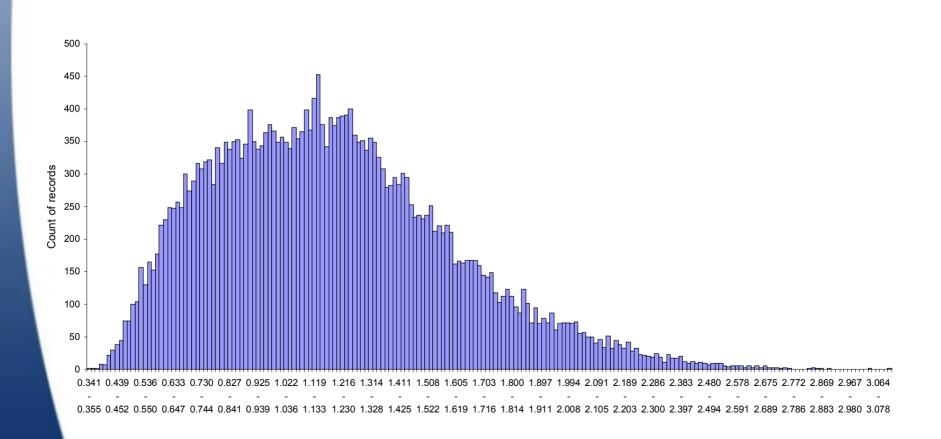
- Base rate change
- Base rate change with relativity change
- Premium moderators
- Full optimization

#### **Base rate change**

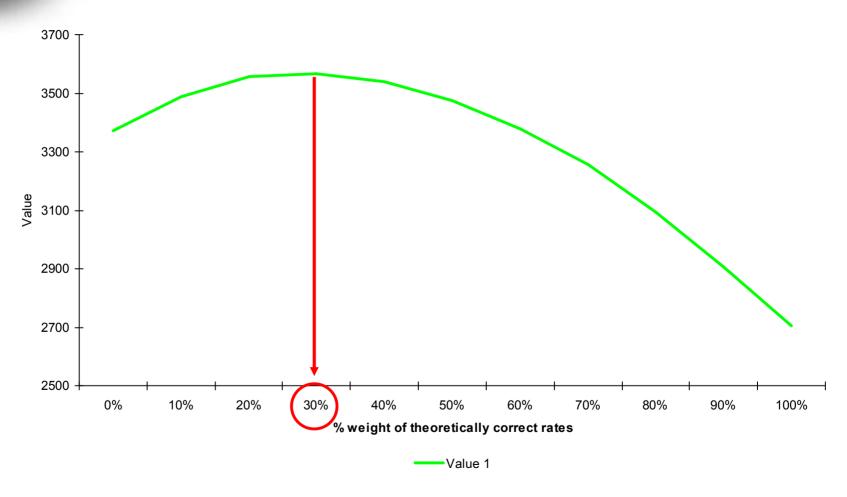




Impact from current relativities to correct relativities

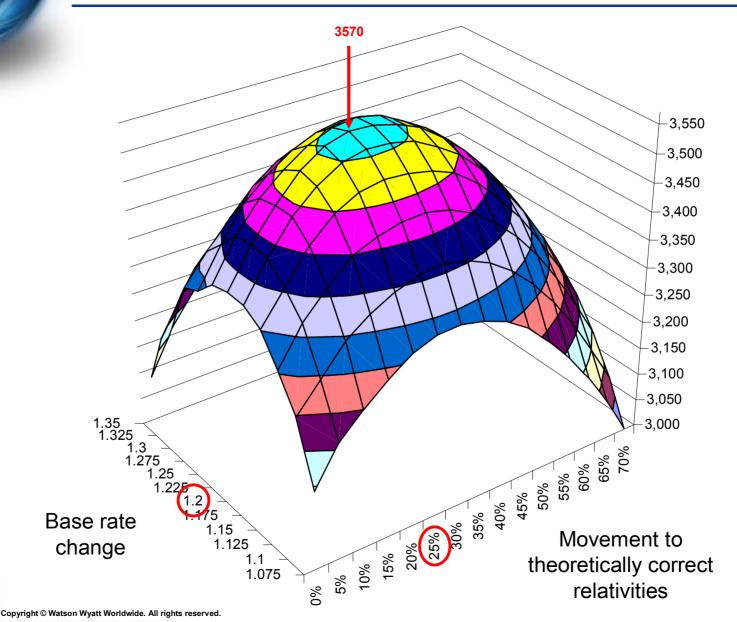


# Base rate change with relativity change



Blend of current and theoretically correct relativities

# Base rate change with relativity change



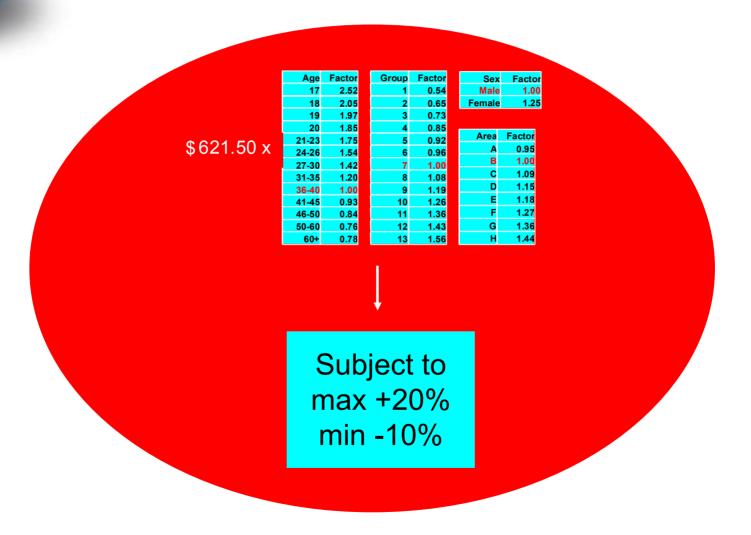


## **Moderators**Types of rating structures - simple multiplicative

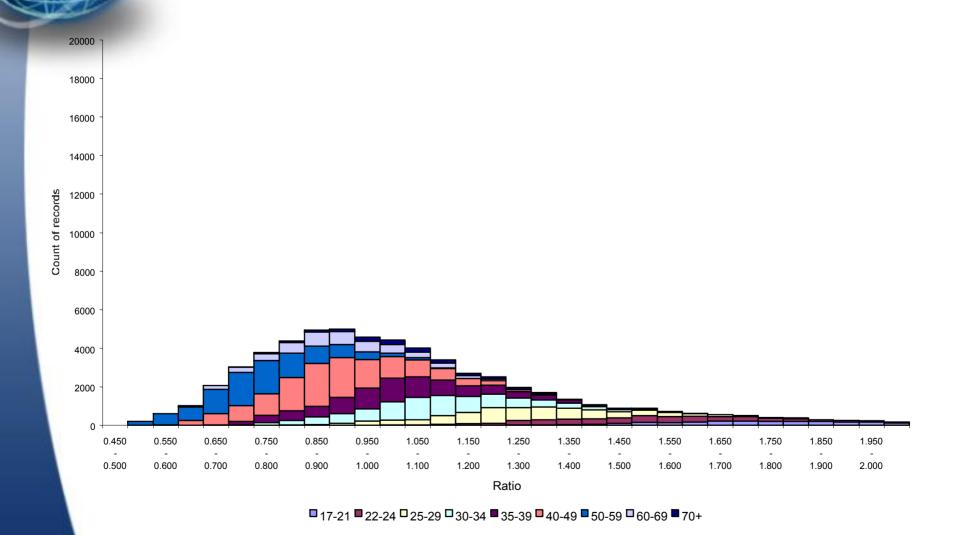
	Age	Factor	Group	Factor	Sex	Factor	
\$621.50 x	17	2.52	1	0.54	Male	1.00	
	18	2.05	2	0.65	<b>Female</b>	1.25	
	19	1.97	3	0.73			
	20	1.85	4	0.85	Anas	Footo	
	21-23	1.75	5	0.92	Area	Factor	
	24-26	1.54	6	0.96	A	0.95	
	27-30	1.42	7	1.00	В	1.00	
	31-35	1.20	8	1.08	С	1.09	
	36-40	1.00	9	1.19	D	1.15	
	41-45	0.93	10	1.26	E	1.18	
	46-50	0.84	11	1.36	F	1.27	
	50-60	0.76	12	1.43	G	1.36	
	60+	0.78	13	1.56	Н	1.44	

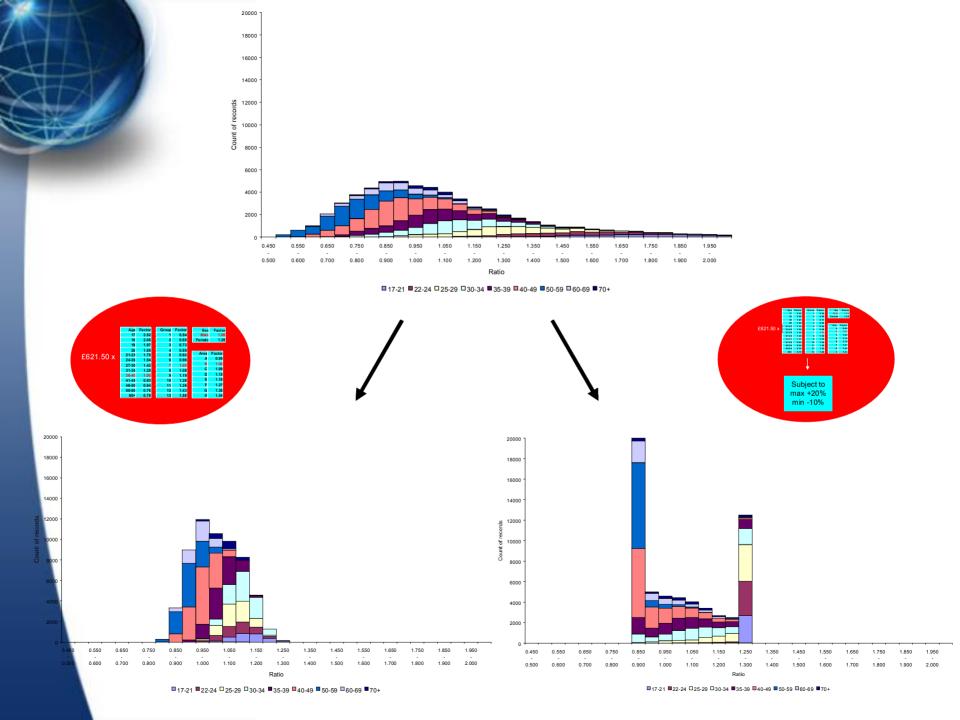
#### **Moderators**

Types of rating structures - multiplicative with moderator



#### **Example of use of moderator**

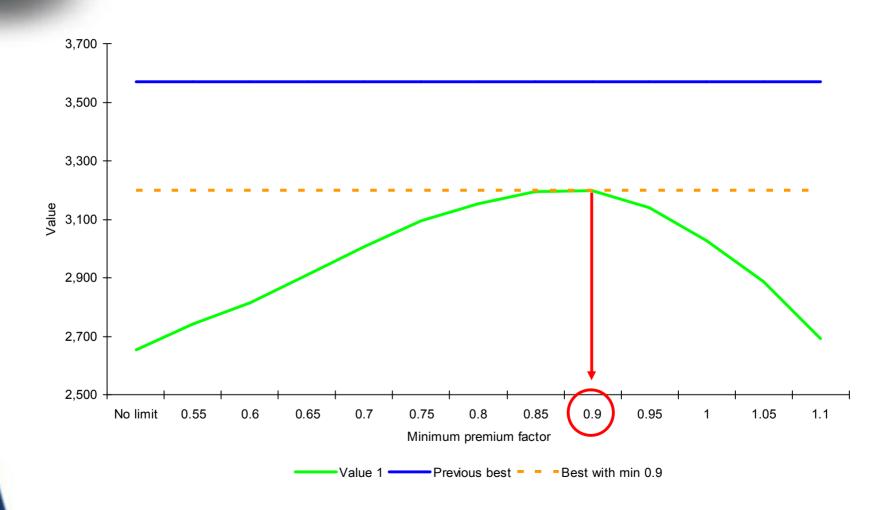




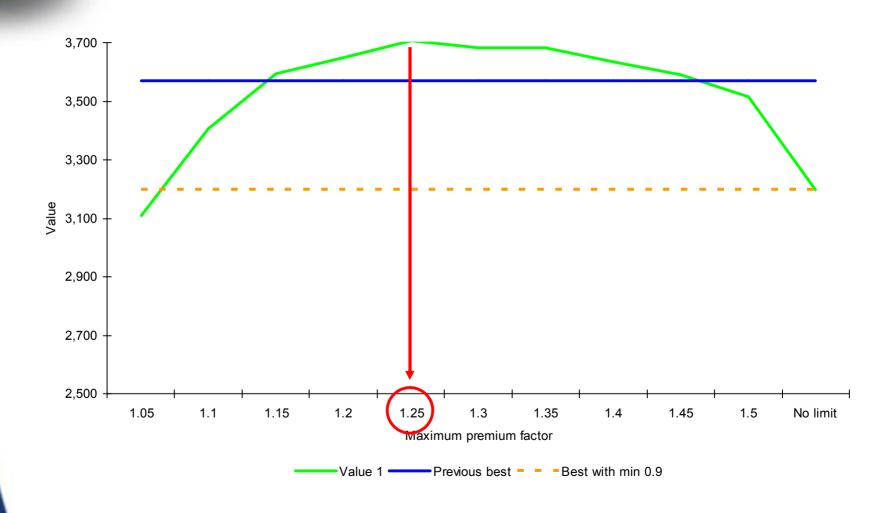
#### **Moderators:** pros/cons

- Advantages of moderators include:
  - moves everyone to optimal position (subject to acceptable premium increases) more quickly
  - can take into account elasticity for the type of person in question
  - can be less detailed work required regarding underlying parameterization
  - less work required to parameterize in future
- Disadvantages
  - more onerous system requirements
  - harder to understand rating structure
  - likely to result in different quotes for renewals and new business for an identical risk
  - may not be too popular with some regulators?

## Parameterizing the moderator Investigation of limiting premium decreases



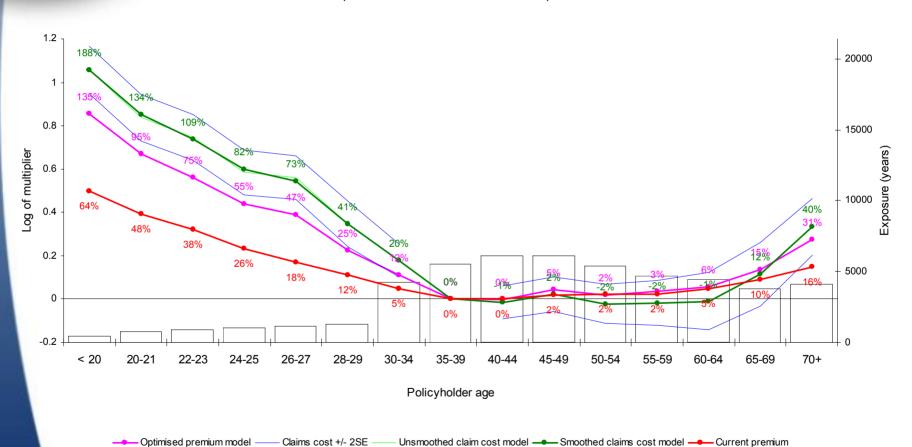
# Parameterizing the moderator Investigation of limiting premium increases given 10% limit on decreases



### **Full optimization**

#### **Optimized premium**

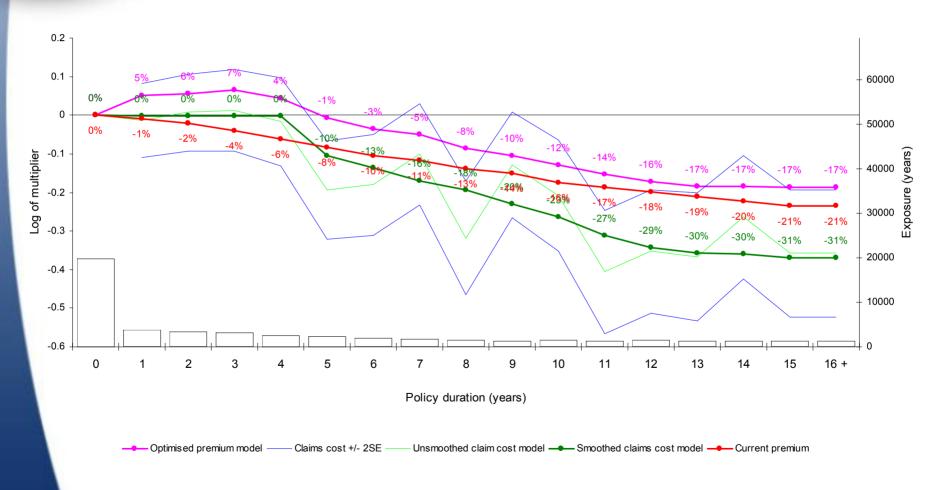
Comparison with claims model and current premium



#### **Full optimization**

#### **Optimized premium**

Comparison with claims model and current premium





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