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## C-6: Communicating Predictive Modeling Results

**CAS Predictive Modeling Seminar  
San Diego, October 6-7, 2008  
Louis Mak FCAS FIAA  
Watson Wyatt Worldwide**

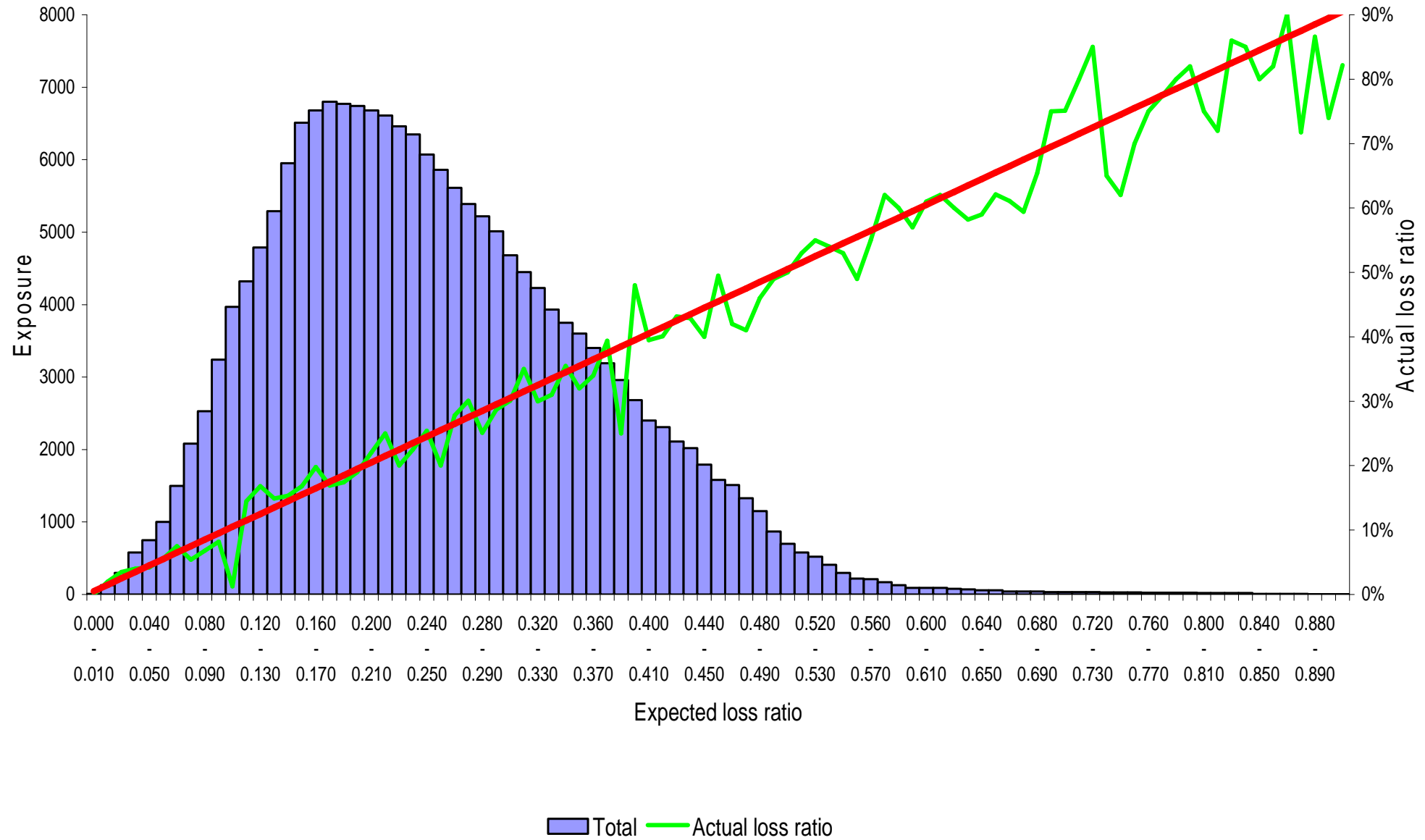


# Communicating modeling results visually

- Stakeholder approach
  - focus on the value of the results
- Technical / actuarial approach
  - tell the story of the model development in a chronological fashion



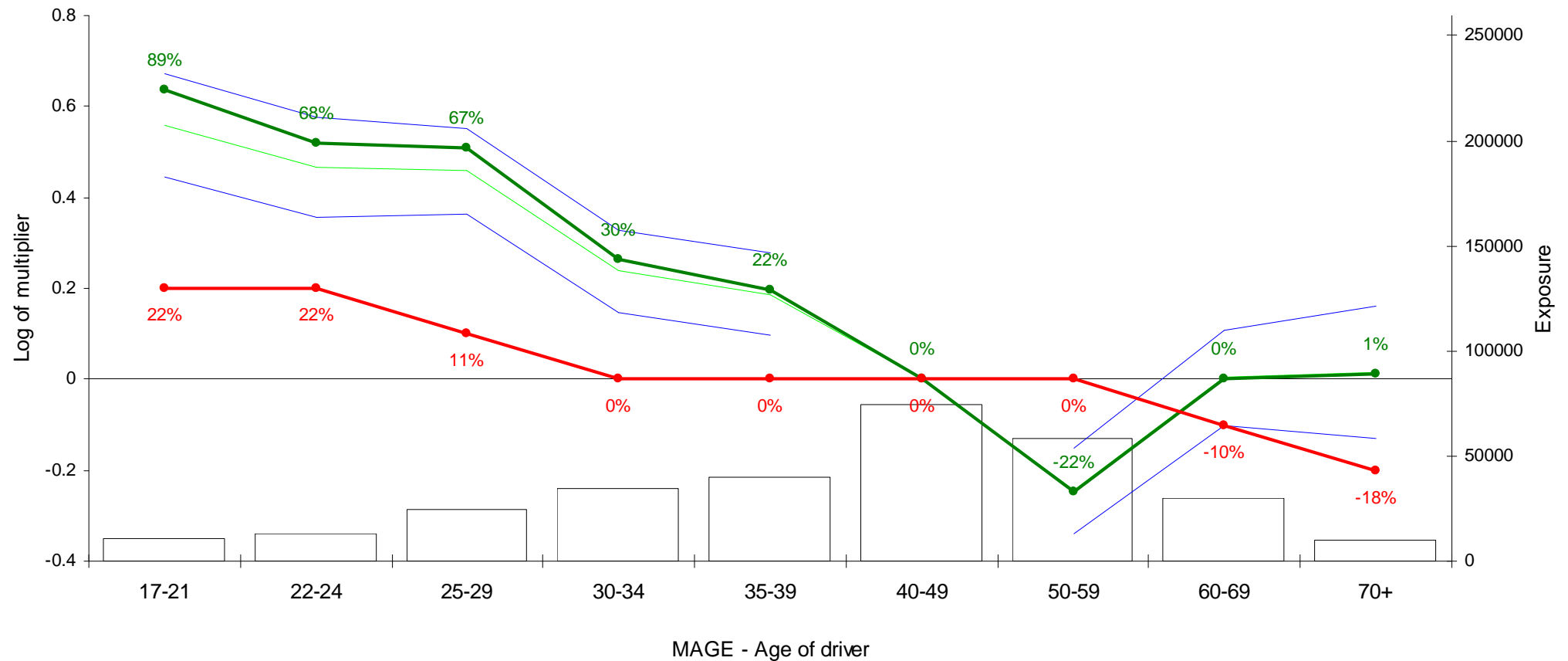
# Loss ratio impact



# Factor effect analysis

## Demonstration job

Run 10 Model 2 - Third party material, standard risk premium run - Unsmoothed standard risk premium model

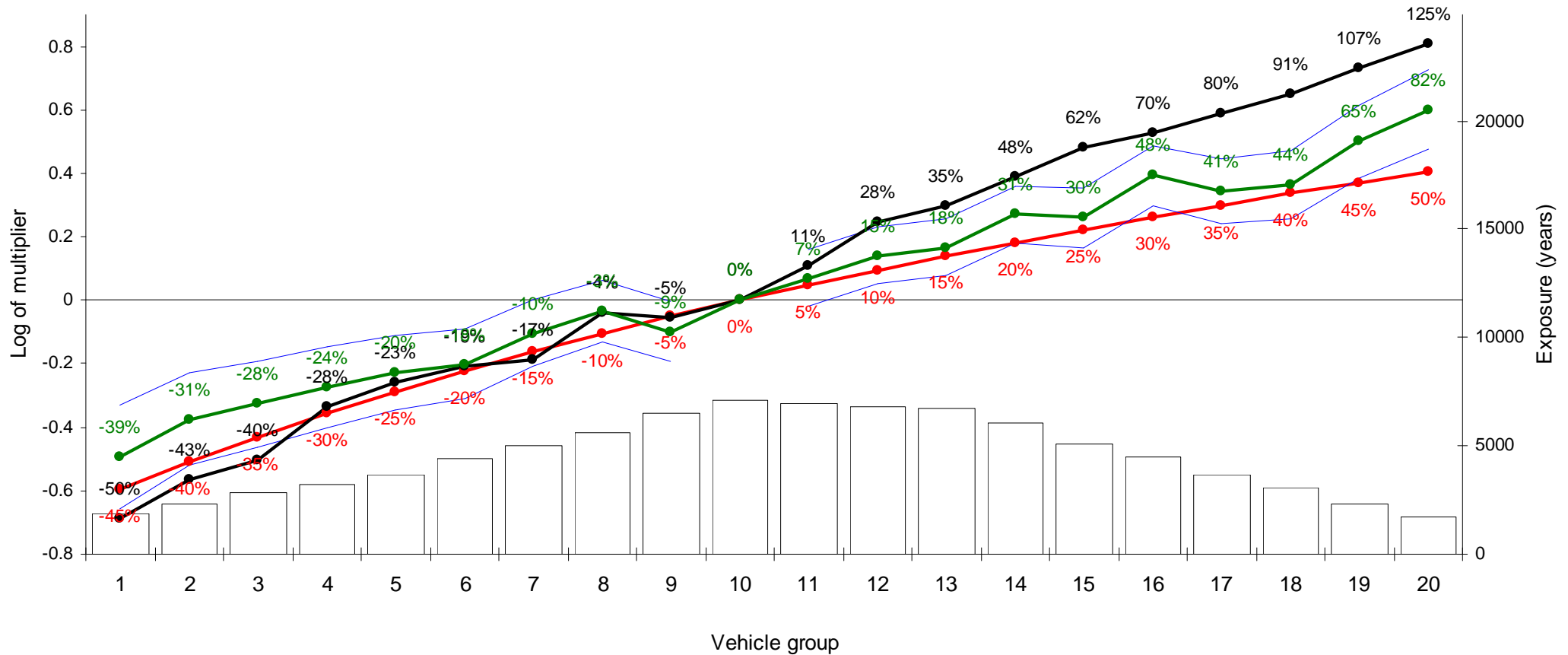


— Approx 2 SEs from unsmoothed estimate — Unsmoothed unrestricted estimate — Unsmoothed restricted estimate — Current rating structure

# Considering current rates and the competitive position

## Example of competitor analysis

Third party cover

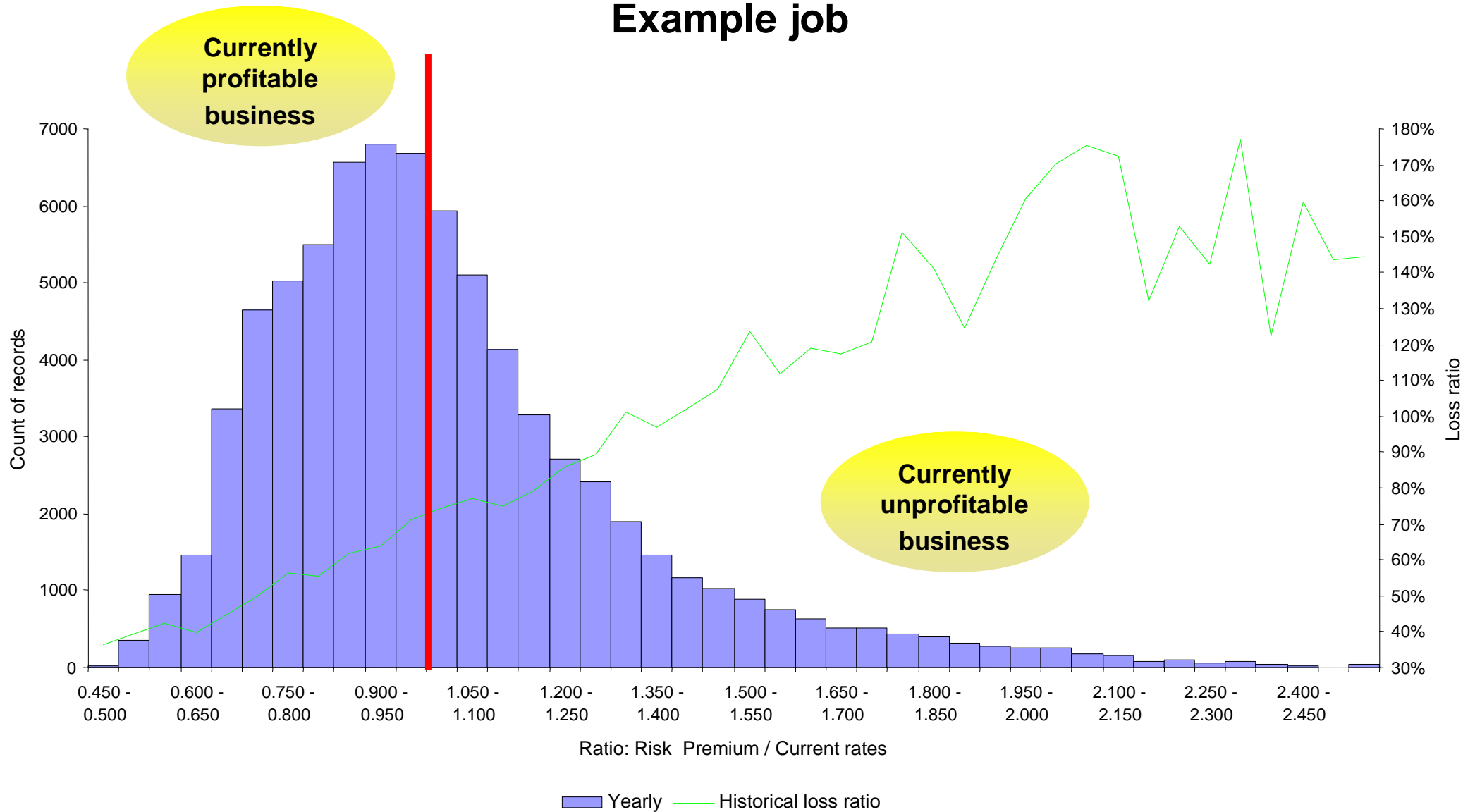


● Current rates   
 — Approx 95% confidence interval   
 ● Third cheapest market quote   
 ● Smoothed estimate

P value = 0.0%  
 Rank 9/11

# Impact analysis

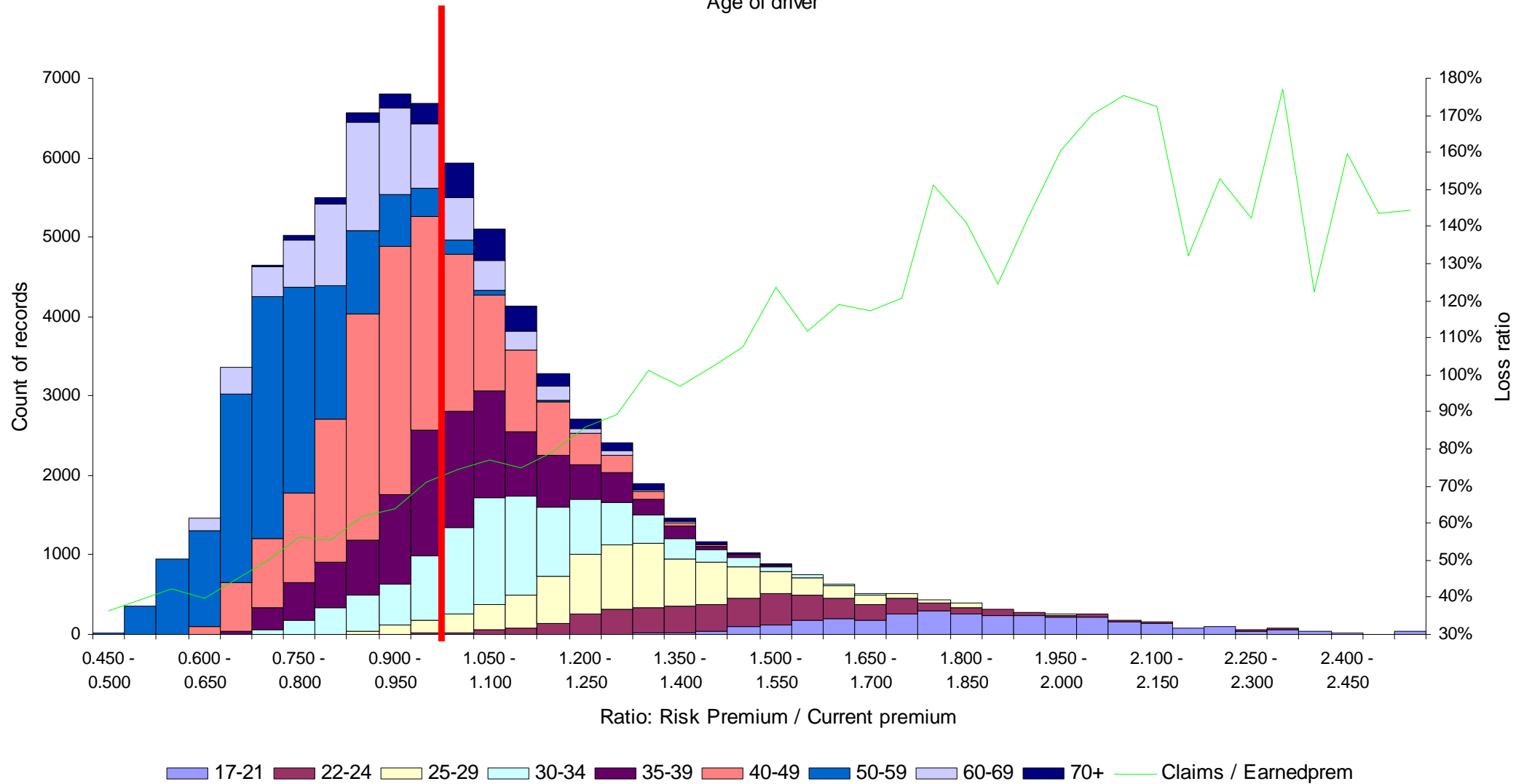
## Example job



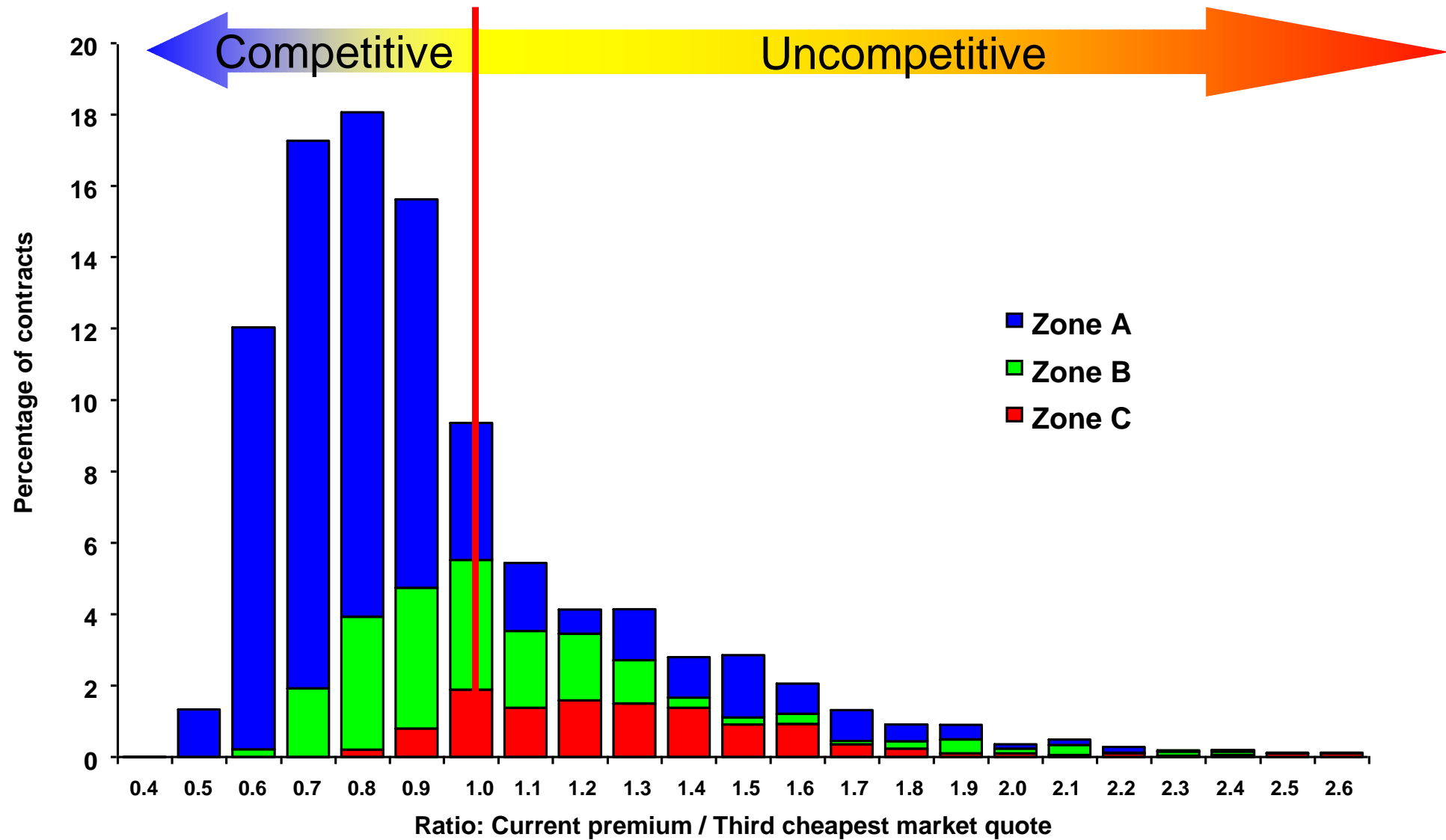
# Impact analysis

## Example job

Age of driver

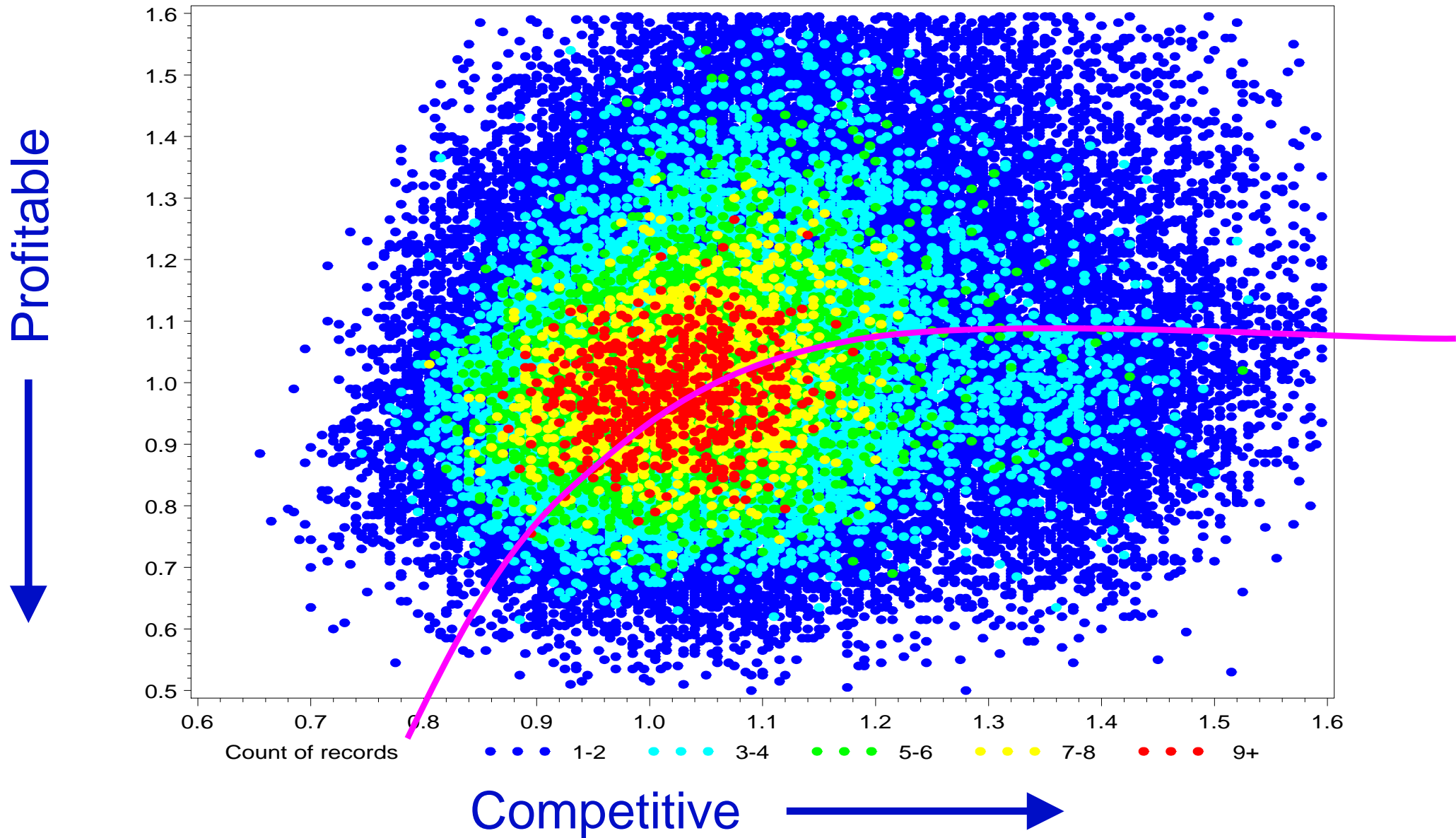


# Comparison with competitors

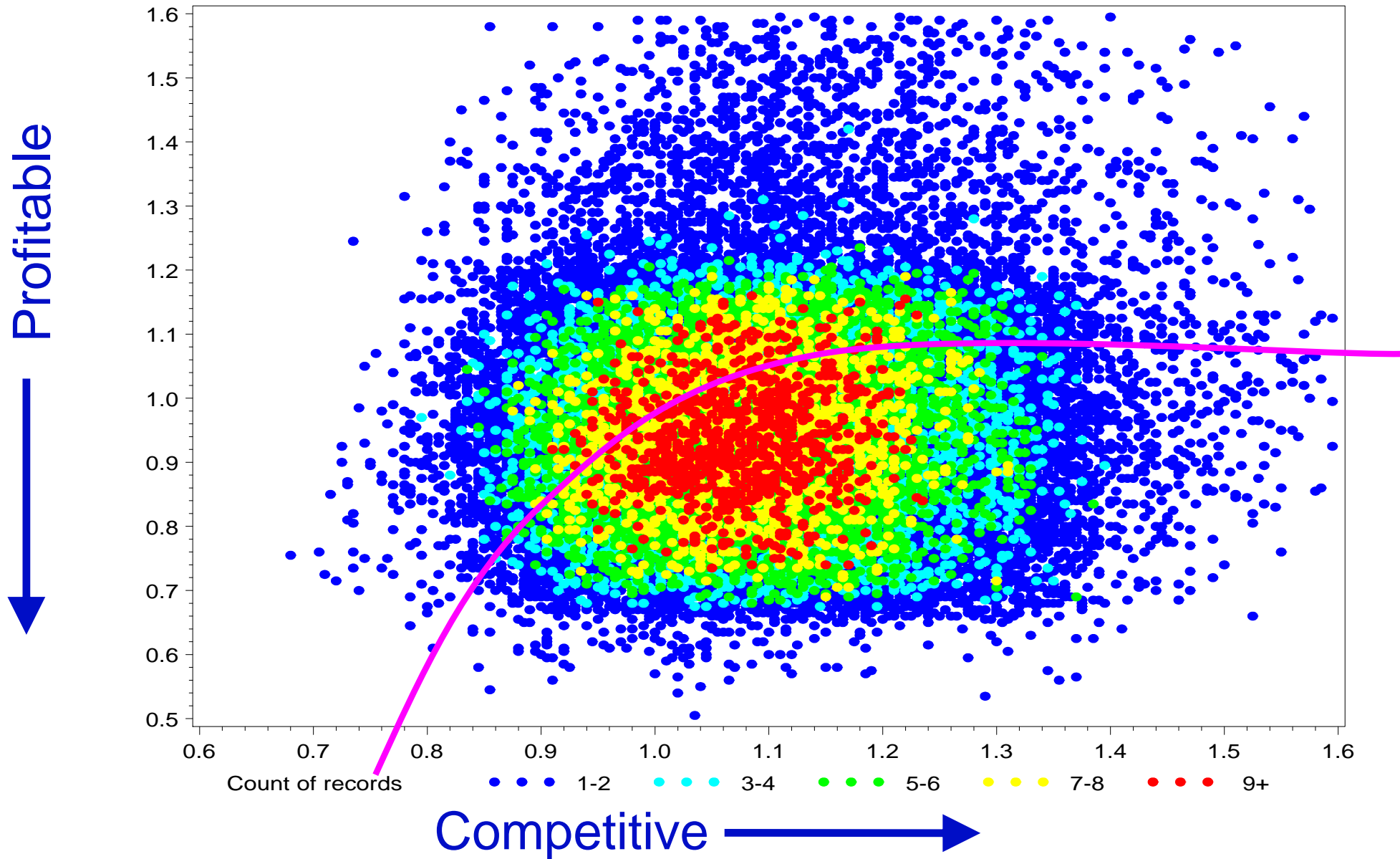




# Moving toward competitive / profitable (Before)



# Moving toward competitive / profitable (After)



# Communicating modeling results visually

- Business approach
  - lead with the value of the results
- Technical / actuarial approach
  - tell the story of the model development in a chronological fashion



# Technical stories

- Data Cleaning
- Portfolio analysis
- Deviance tests vs graphical results
- Consistency with time
- Interactions (deciding which to test & detecting significance)
- Residual diagnostics and leverage
- Testing the effectiveness of restrictions
- Validating models
- Maps
- Monitoring

# Technical stories

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# One way table

- Check data reasonable
- See obvious features
- Allows consideration of factor mapping

Level	Number of records	Exposure	Premium	Number of claims	Incurred claims	Claim frequency	Average cost per claim	Pure premium	Loss ratio
02	89	317	181,270	9	7,586	2.8%	843	24	4.2%
04	124	409	256,502	29	23,671	7.1%	816	58	9.2%
05	2,186	8,772	5,076,035	381	229,390	4.3%	602	26	4.5%
06	4	17	22,886	2	764	11.5%	382	44	3.3%
07	2,883	11,451	8,101,723	560	380,803	4.9%	680	33	4.7%
08	9,420	36,571	37,021,314	2,310	1,652,938	6.3%	716	45	4.5%
09	12,852	49,515	50,639,518	3,030	2,098,998	6.1%	693	42	4.1%
10	16,758	64,407	73,509,639	4,401	3,114,671	6.8%	708	48	4.2%
11	13,702	53,372	63,136,308	3,608	2,602,046	6.8%	721	49	4.1%
12	10,302	40,512	51,408,113	2,715	1,928,351	6.7%	710	48	3.8%
13	5,682	22,108	28,594,451	1,658	1,177,545	7.5%	710	53	4.1%
14	1,829	6,990	11,039,929	466	336,051	6.7%	721	48	3.0%
15	480	1,797	3,091,657	119	81,852	6.6%	688	46	2.6%
16	195	744	1,387,007	73	54,593	9.8%	748	73	3.9%
	<b>76,506</b>	<b>296,980</b>	<b>333,466,350</b>	<b>19,361</b>	<b>13,689,260</b>	<b>6.5%</b>	<b>707</b>	<b>46.09</b>	<b>4.1%</b>

# Data Problem Identification / Cleaning

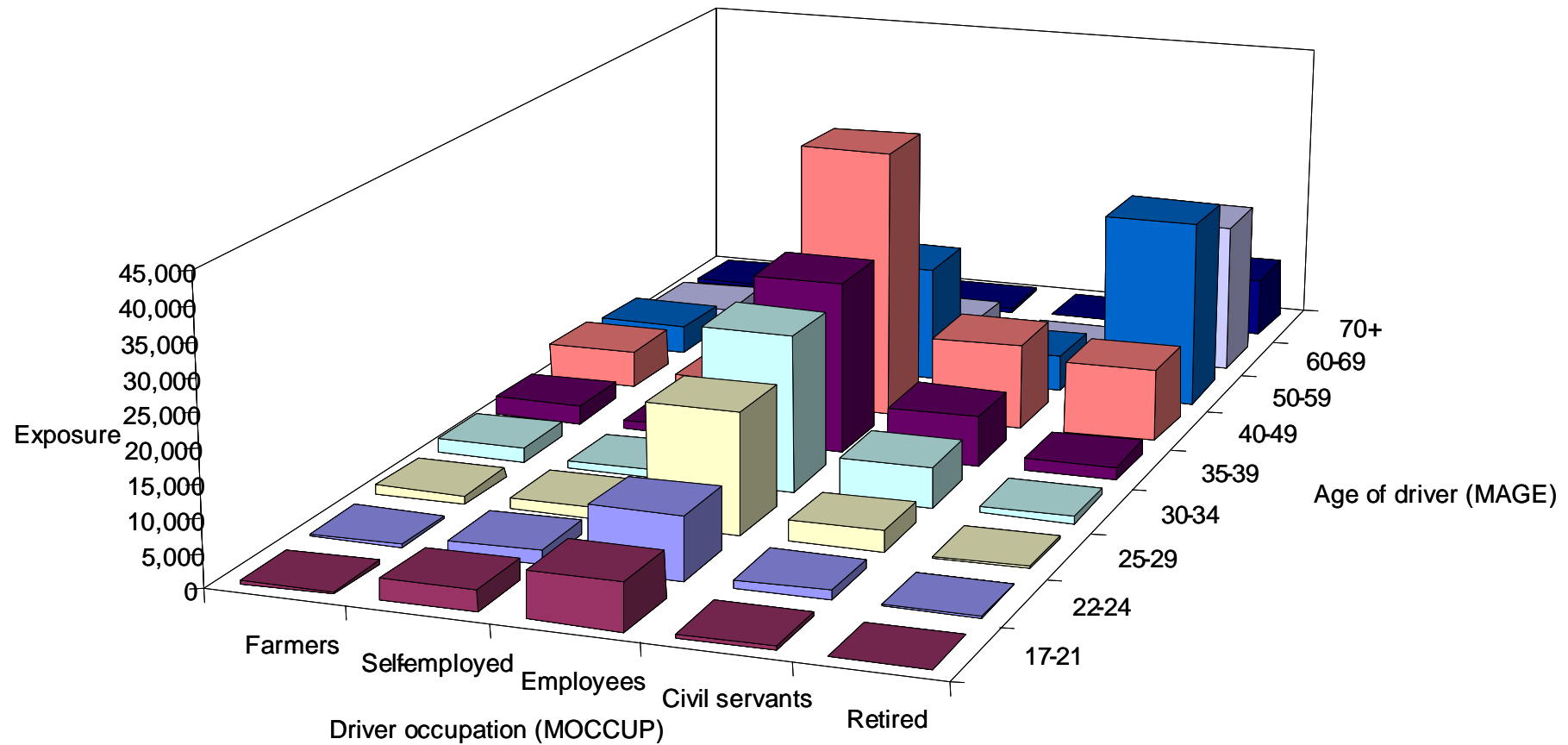
Data exception report  
Record count = 150100

Variable	Missing (Claim fields)	Missing (Other)	Negative (Claim fields)	Negative (Other)	Zero	Numbers > 0 and Incurred = 0	Incurred ^= 0 and Numbers = 0	Exposure = 0 and Numbers > 0	-1 < Incurred < 1 and Numbers > 0
Numad	0		0		144541	0			
Numtppd	0		0		131884	21			
Numtpbi	0		0		143404	0			
Incad	0		0		144541		0		0
Inctppd	0		0		131905		0		33
Inctpbi	0		0		143404		0		71
Expy	0		22		57			0	
Expyad	0		7		73005			0	
Eprem	0		22		57				
Epremad	0		7		73005				

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# Two way analyses

- Hint where interactions may lie





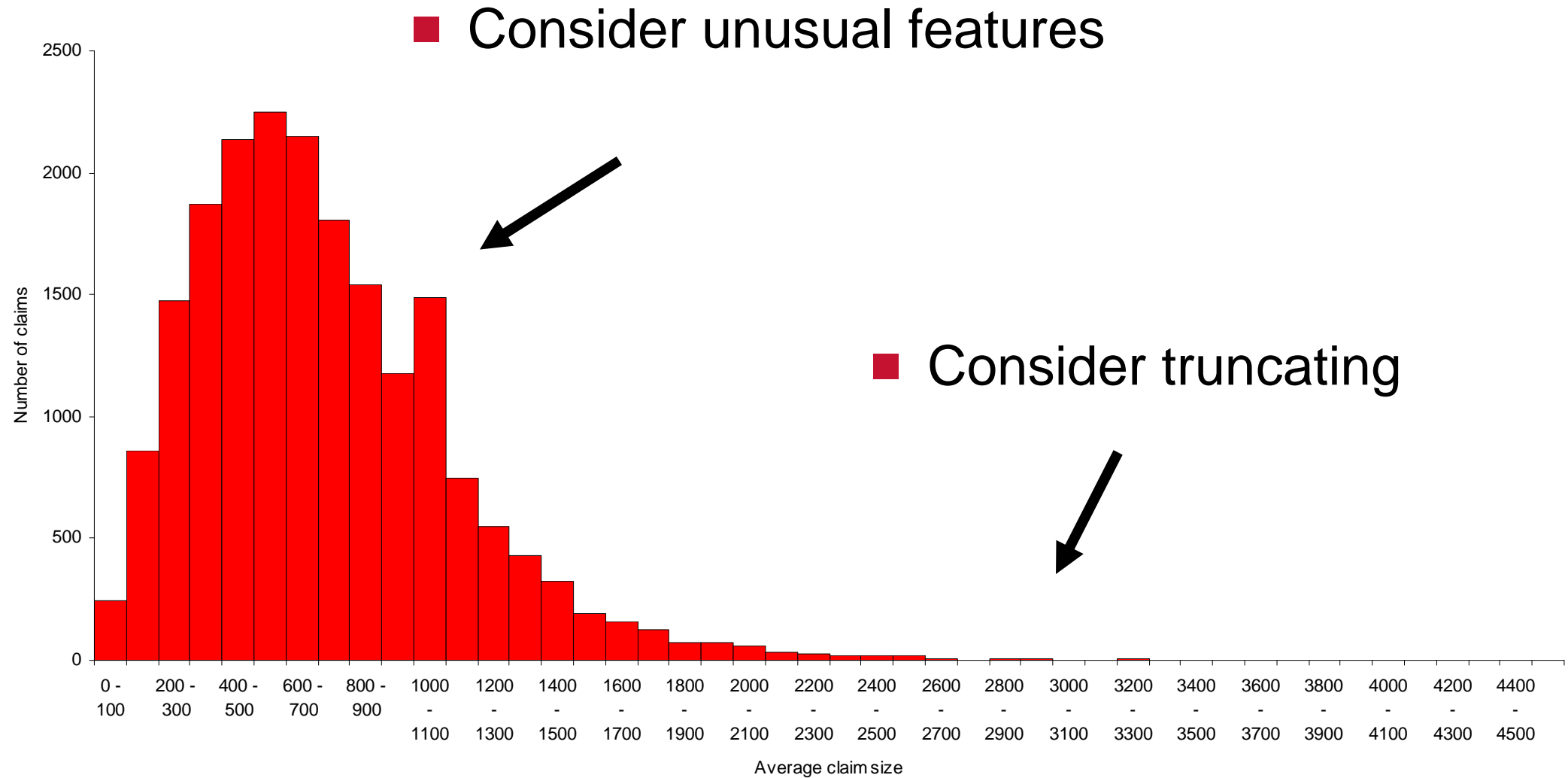
# Correlation

- Identified key correlations
- Not used directly, but helps with interpretation later

## Cramer's V

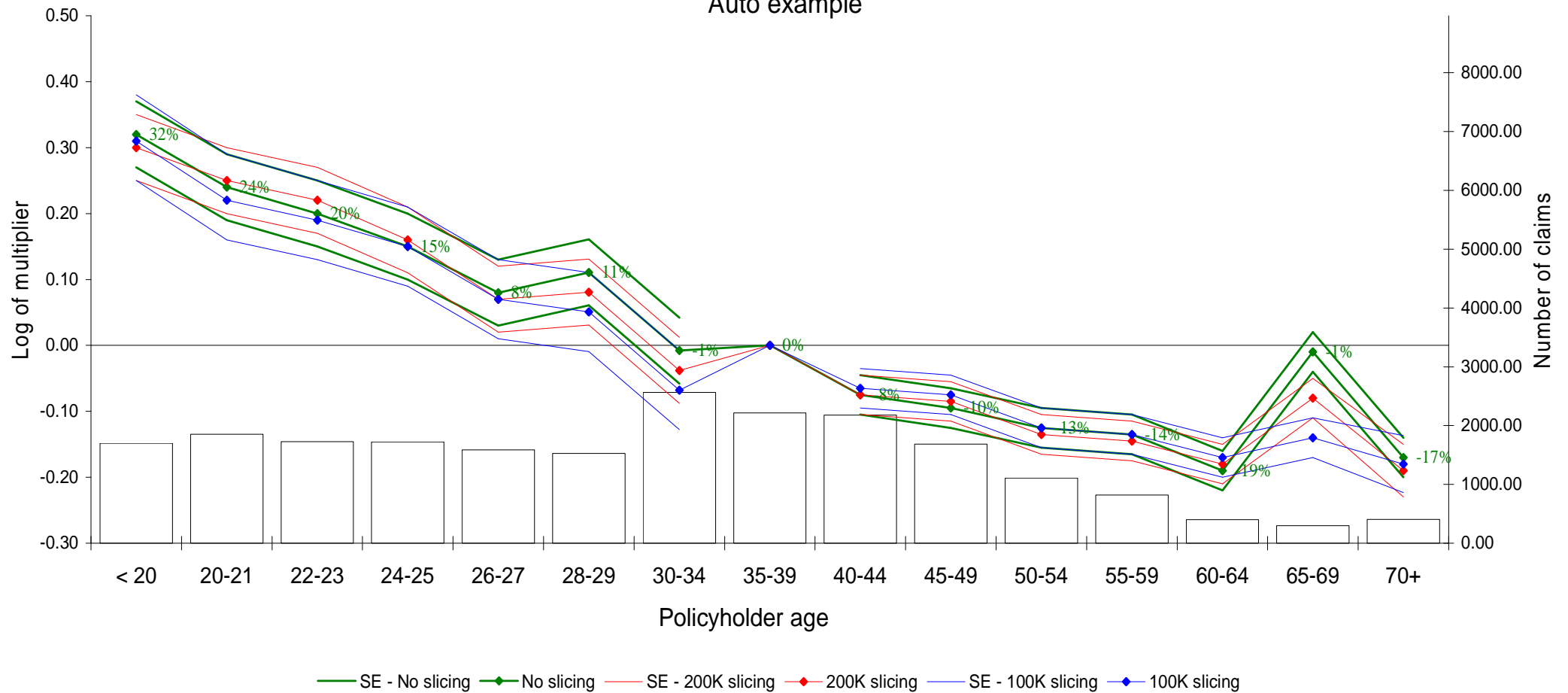
	Age of driver	Area of garage	Calendar year	Class of vehicle	Type of fuel	Group of vehicle	Married driver	No claim discount	Driver occupn	Payment freq	No of secndry drivers	Sex of driver
Age of driver												
Area of garage	3%											
Calendar year	1%	1%										
Class of vehicle	6%	2%	1%									
Type of fuel	10%	4%	1%	<b>39%</b>								
Group of vehicle	6%	2%	1%	<b>51%</b>	<b>46%</b>							
Married driver	<b>32%</b>	3%	1%	3%	1%	4%						
No claim discount	<b>28%</b>	5%	2%	6%	6%	6%	<b>23%</b>					
Driver occupn	<b>35%</b>	7%	1%	5%	13%	6%	18%	<b>19%</b>				
Payment freq	<b>26%</b>	10%	1%	6%	5%	8%	12%	<b>30%</b>	<b>22%</b>			
No of secndry drivers	12%	3%	1%	6%	2%	7%	2%	8%	8%	2%		
Sex of driver	<b>22%</b>	4%	0%	16%	11%	<b>19%</b>	2%	6%	16%	3%	6%	
Age of vehicle	4%	2%	1%	10%	<b>27%</b>	16%	3%	4%	5%	5%	2%	4%

# Claim size distribution analysis



# Large loss sensitivity testing

Third Party Liability - Severity  
Auto example



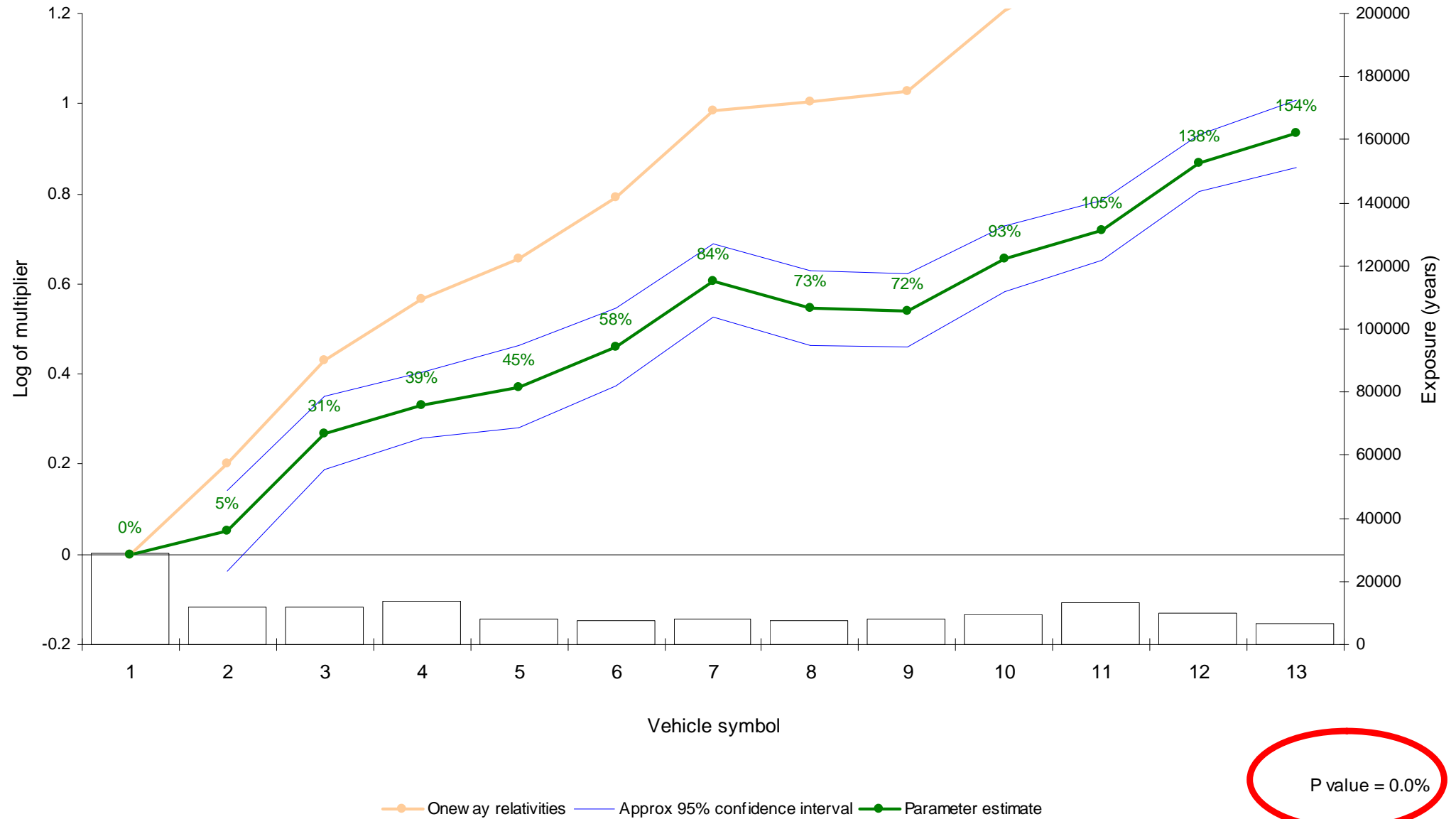
# Technical stories

- Data Cleaning
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- **Deviance tests vs graphical results**
- Consistency with time
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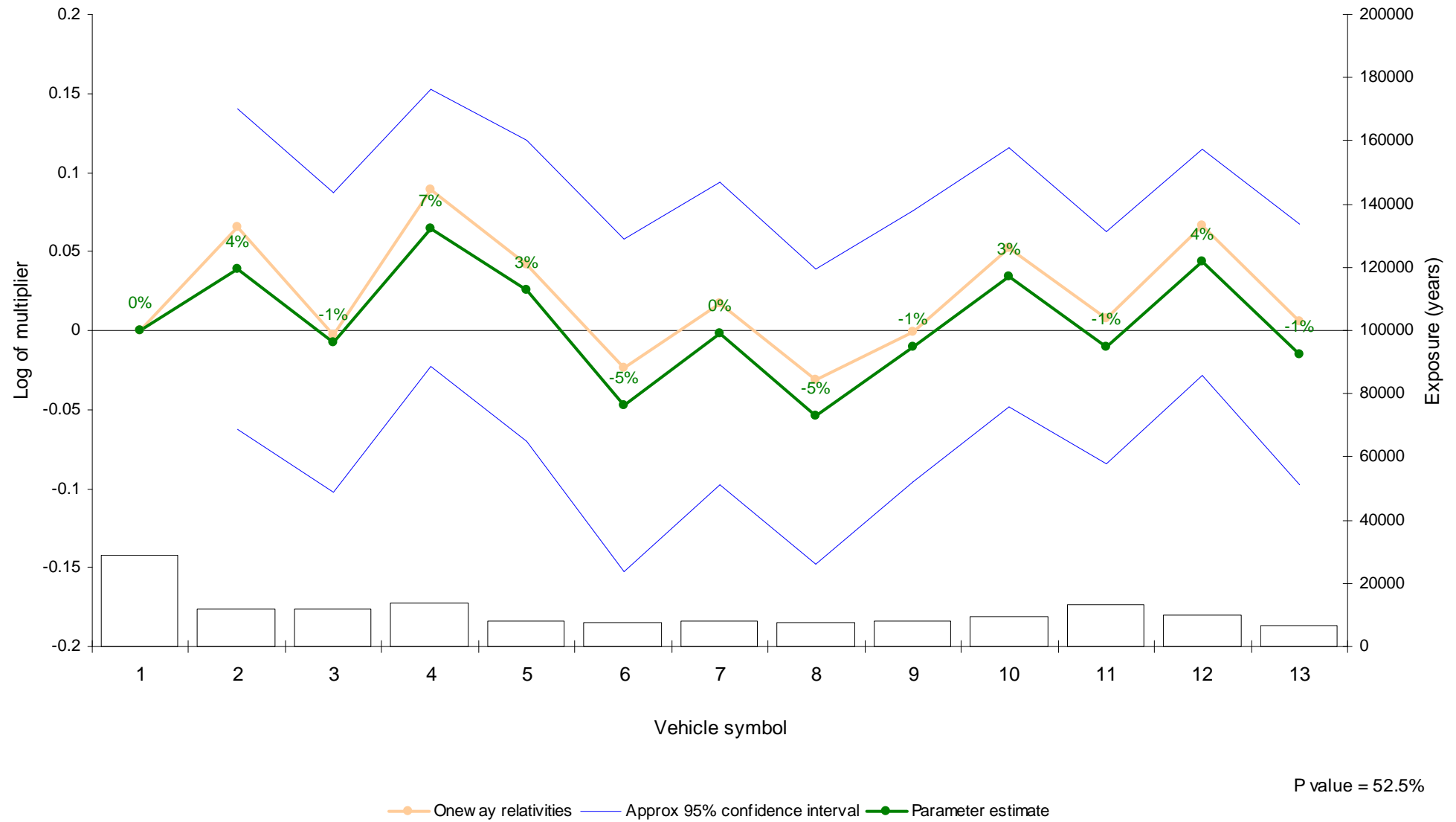
# Deviance tests

- Single figure measure of goodness of fit
- Try model with & without a factor
- Statistical tests show the theoretical significance given the extra parameters

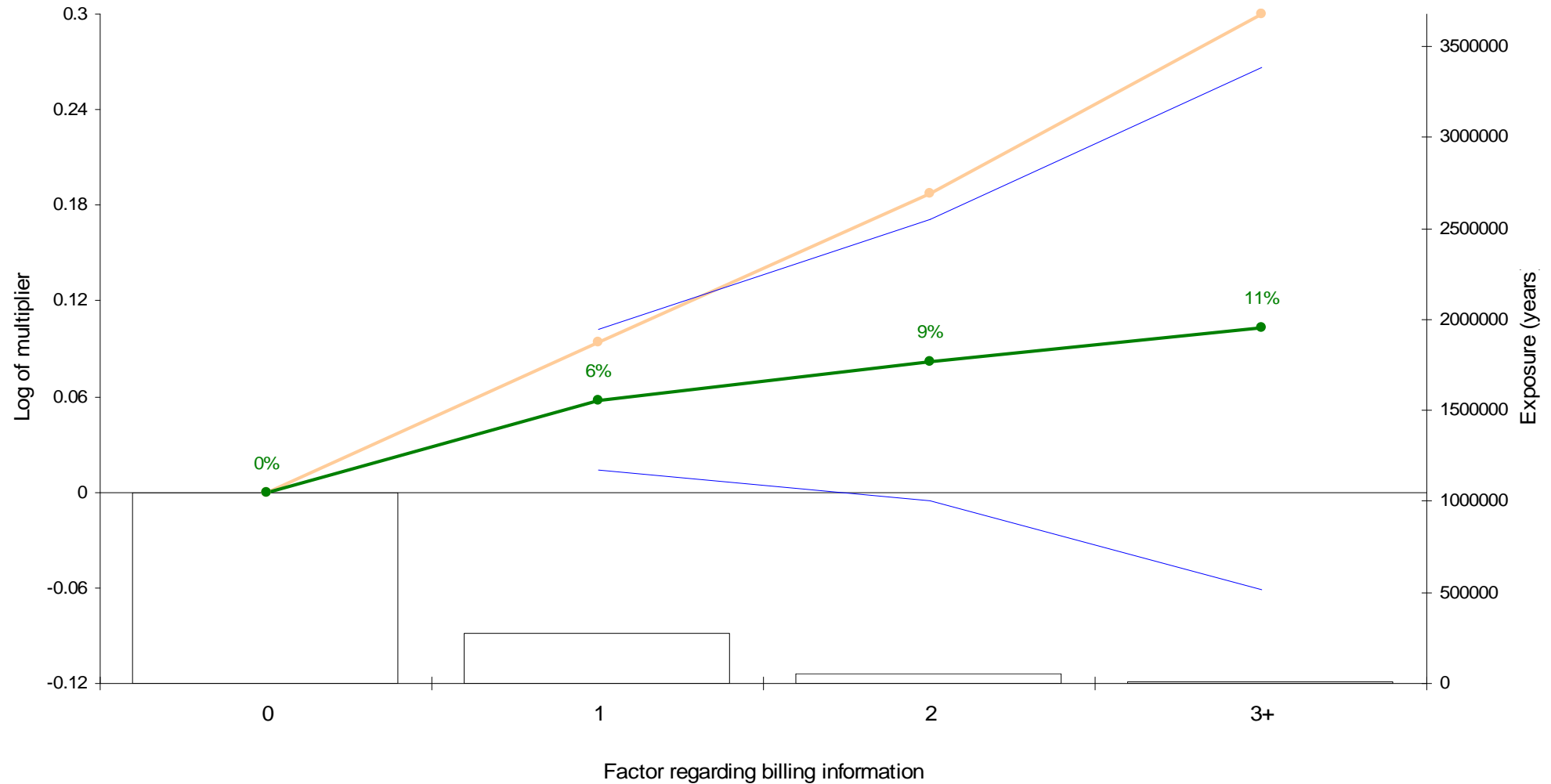
# GLM output (significant factor)



# GLM output (insignificant factor)



# Deviance tests vs graphical results

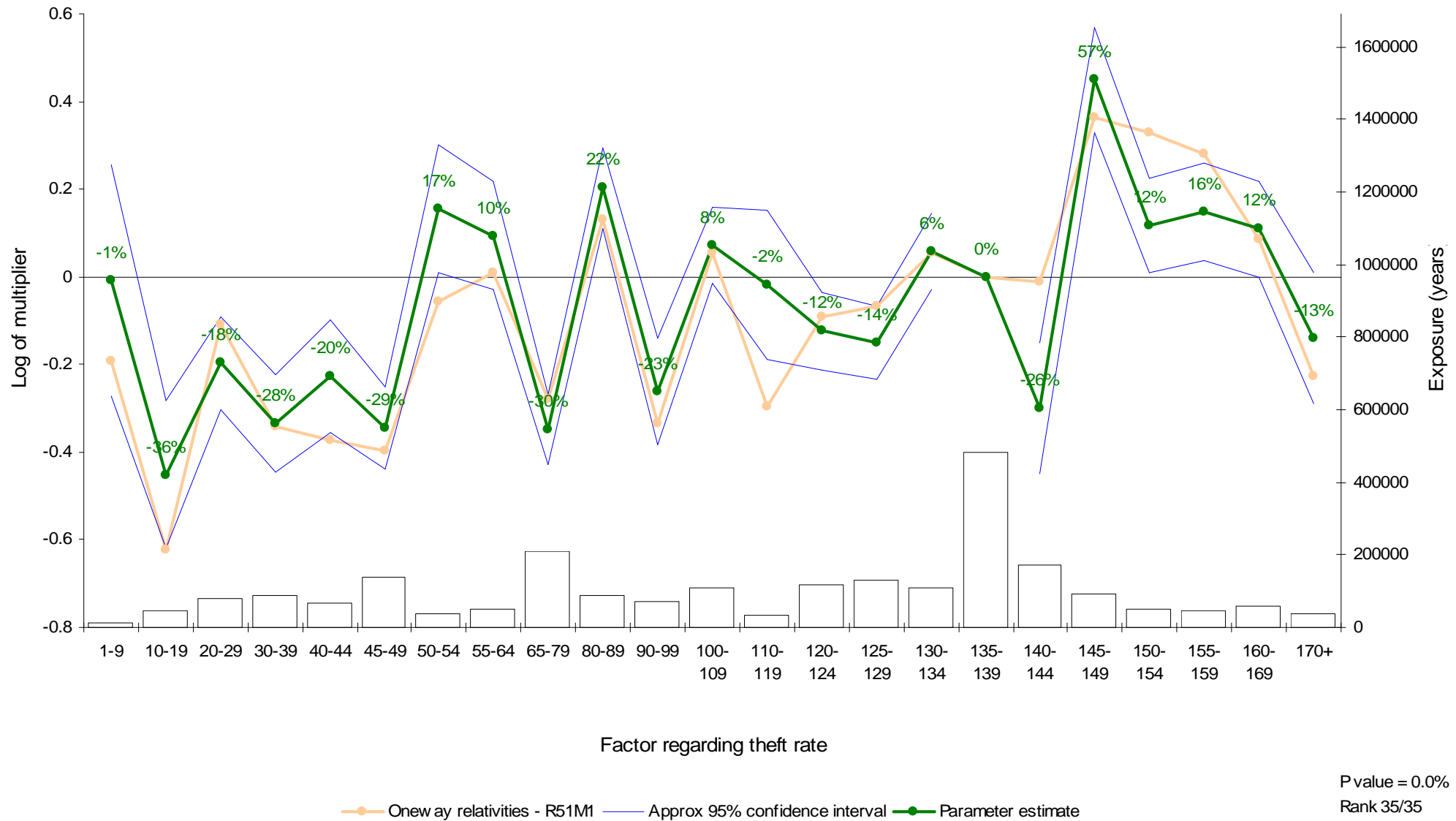


P value = 0.8%  
Rank 14/34

—●— Oneway relativities — Approx 95% confidence interval —●— Unsmoothed estimate —●— Smoothed estimate



# Deviance tests vs graphical results



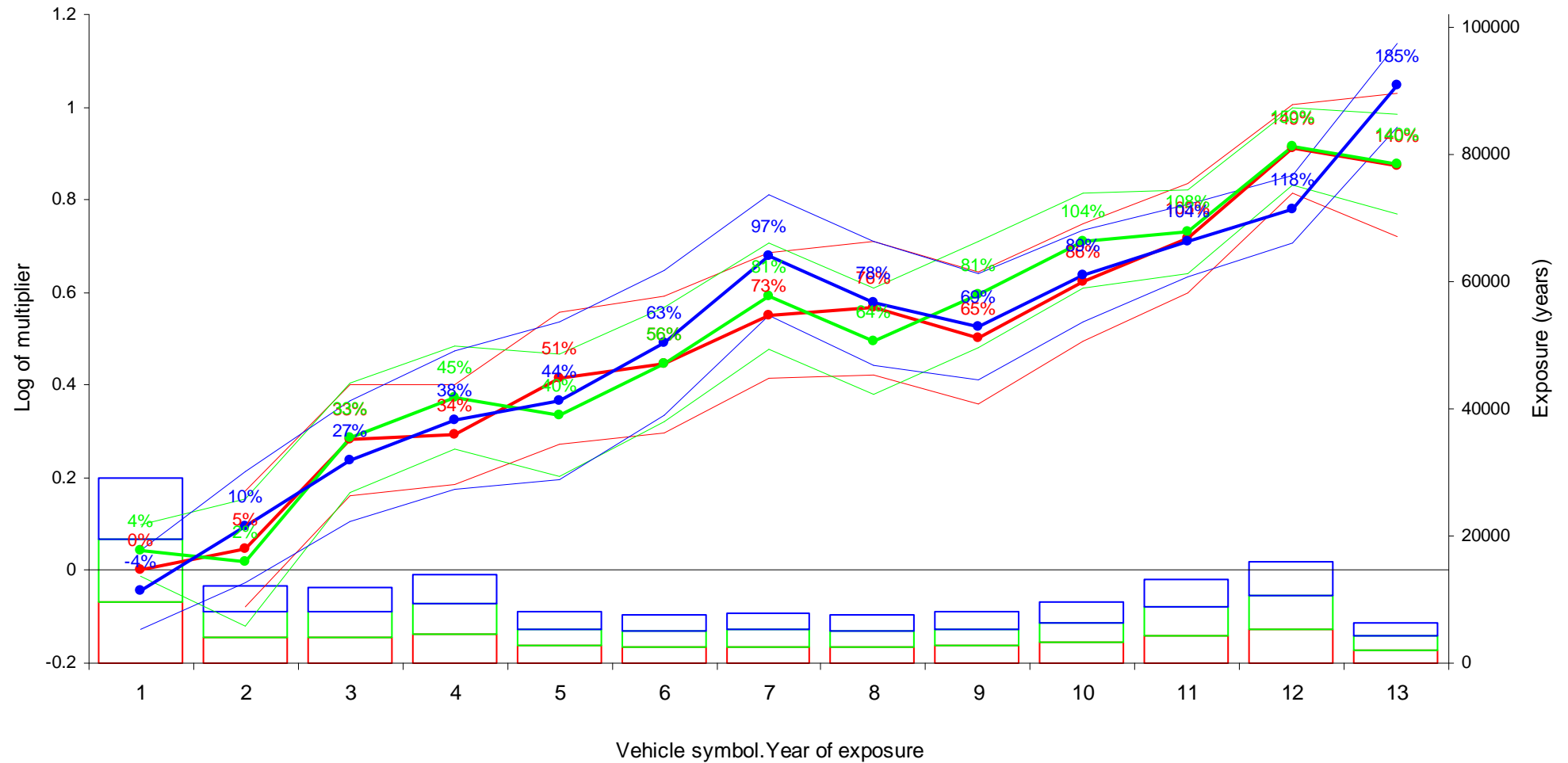
# Deviance tests vs graphical results

- Consider deviance test alongside parameter estimate graph
- In general
  - p-value  $>5\%$  rejection
  - not automatic inclusion for p-value  $\leq 5\%$
- Consider other diagnostics
  - consistency with time
  - examining results on other claim types, other statistics

# Technical stories

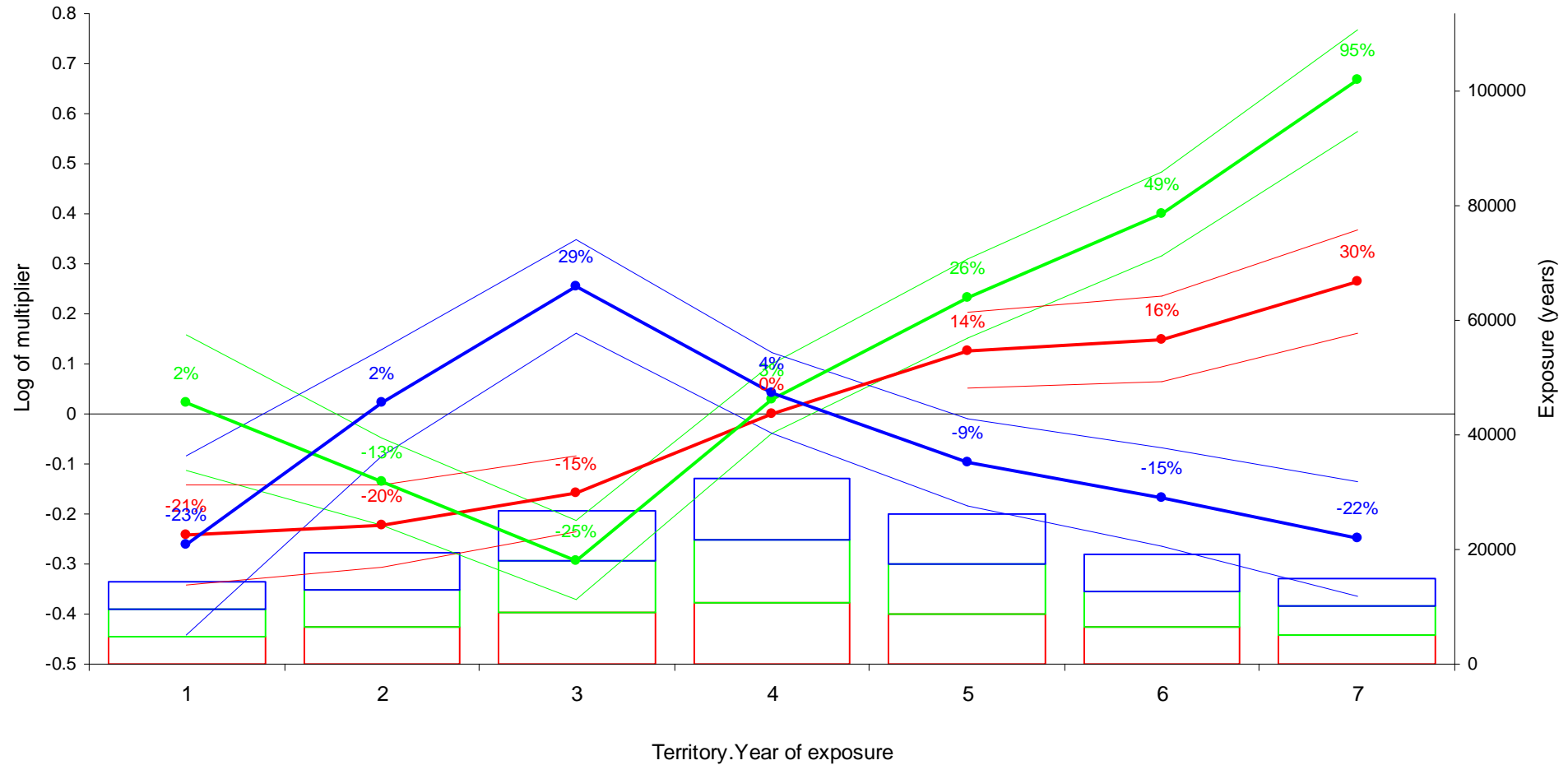
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# Consistency over time



— Approx 95% confidence interval, Year of exposure: 2000   
 — Approx 95% confidence interval, Year of exposure: 2001   
 — Approx 95% confidence interval, Year of exposure: 2002  
● Parameter estimate, Year of exposure: 2000   
 ● Parameter estimate, Year of exposure: 2001   
 ● Parameter estimate, Year of exposure: 2002

# Consistency over time



— Approx 95% confidence interval, Year of exposure: 2000   
 — Approx 95% confidence interval, Year of exposure: 2001   
 — Approx 95% confidence interval, Year of exposure: 2002  
● Smoothed estimate, Year of exposure: 2000   
 ● Smoothed estimate, Year of exposure: 2001   
 ● Smoothed estimate, Year of exposure: 2002

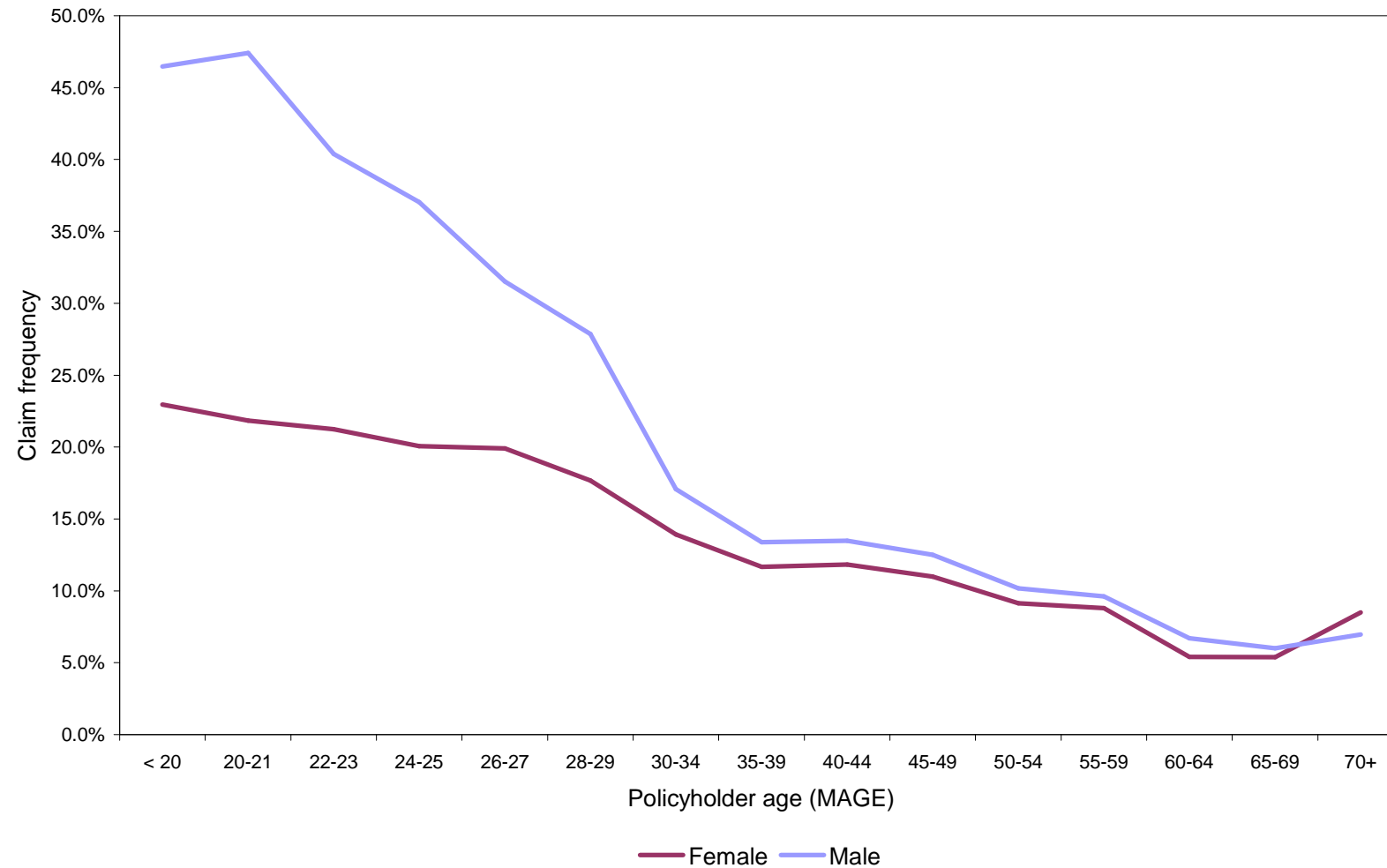
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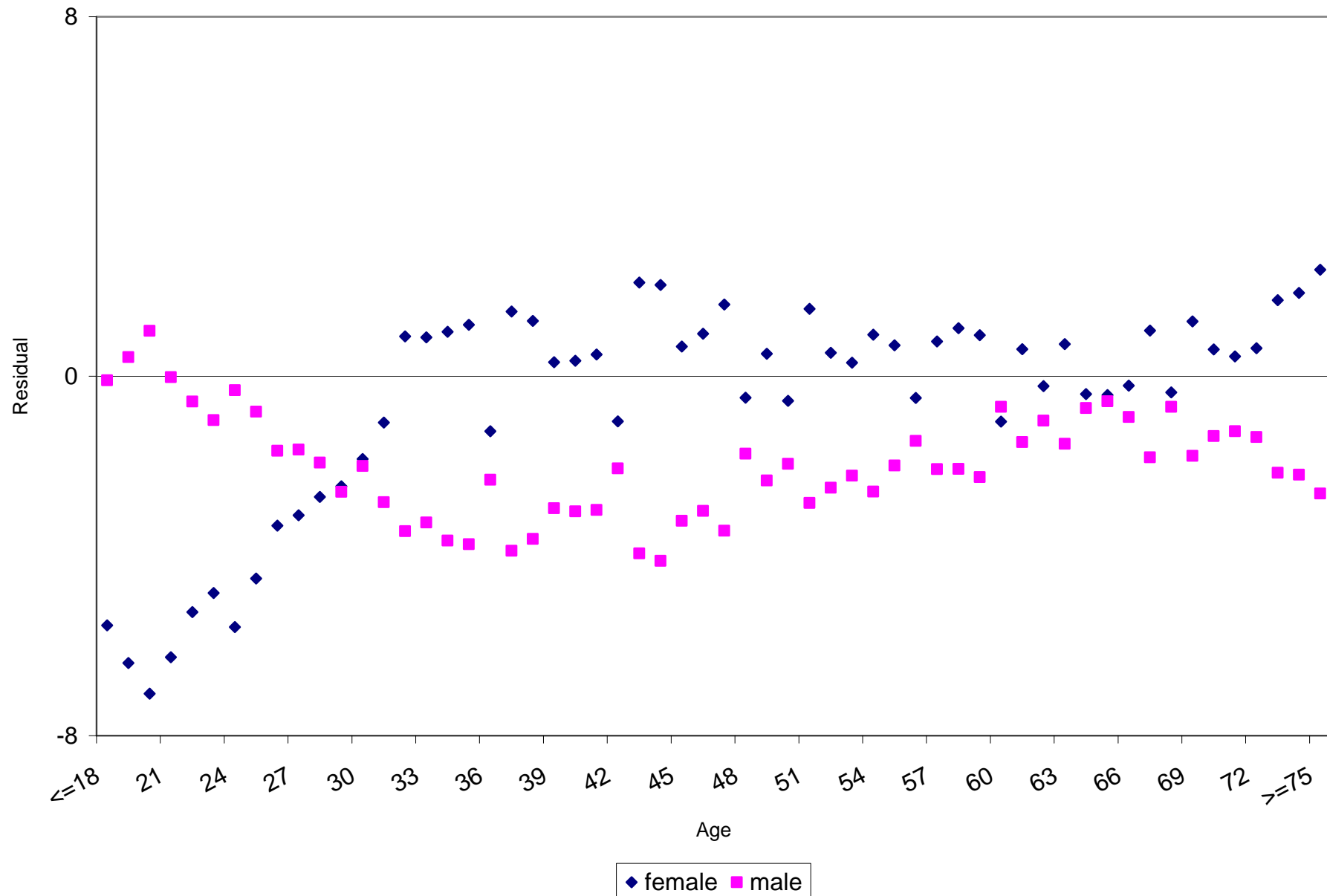
# Two way frequency

## A worked example of the tutorial job

Claim type 1 - Third party property damage  
Sex of policyholder (MSEX)



# Two way of deviance residual (age and sex)

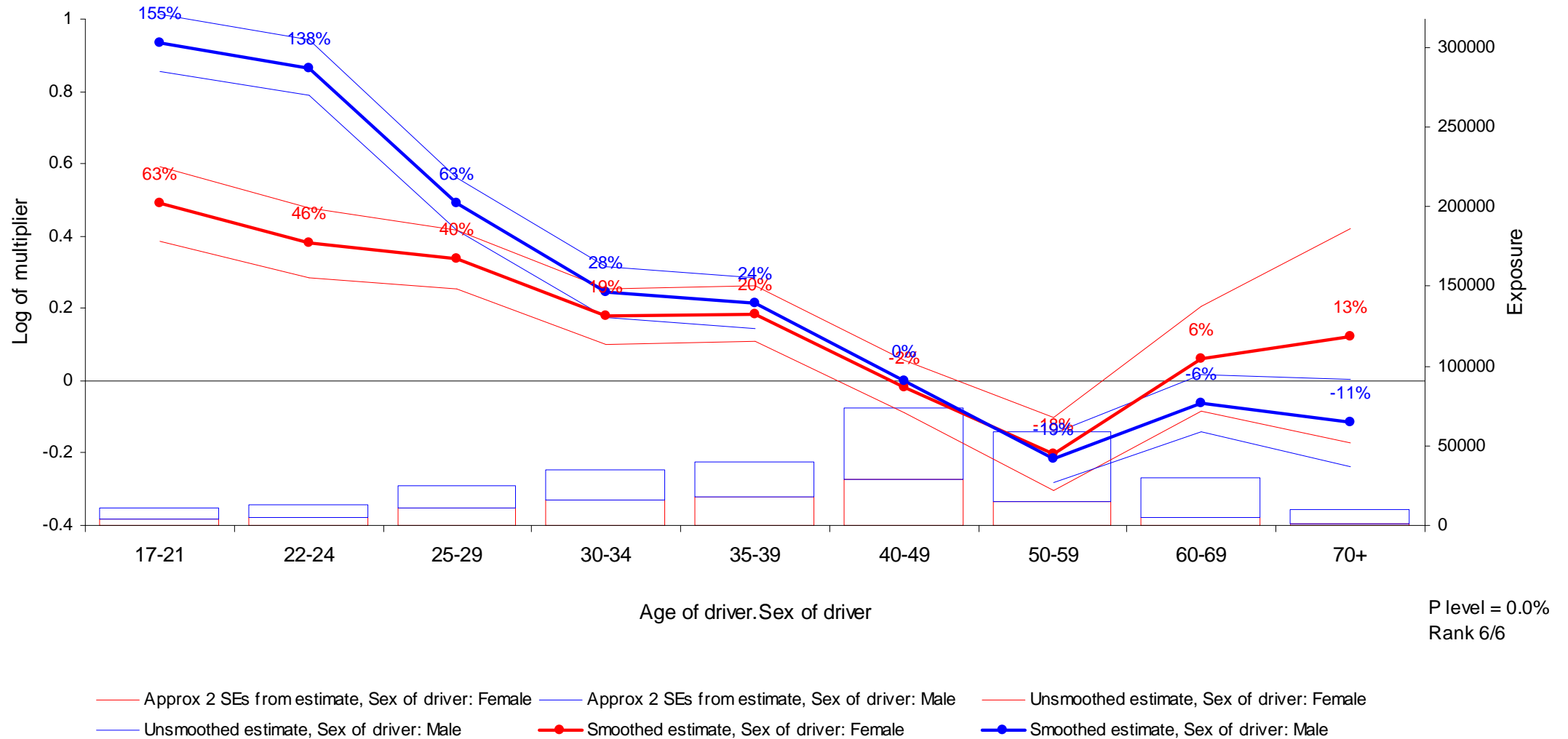




# Age - sex interaction (full interaction)

## Example job

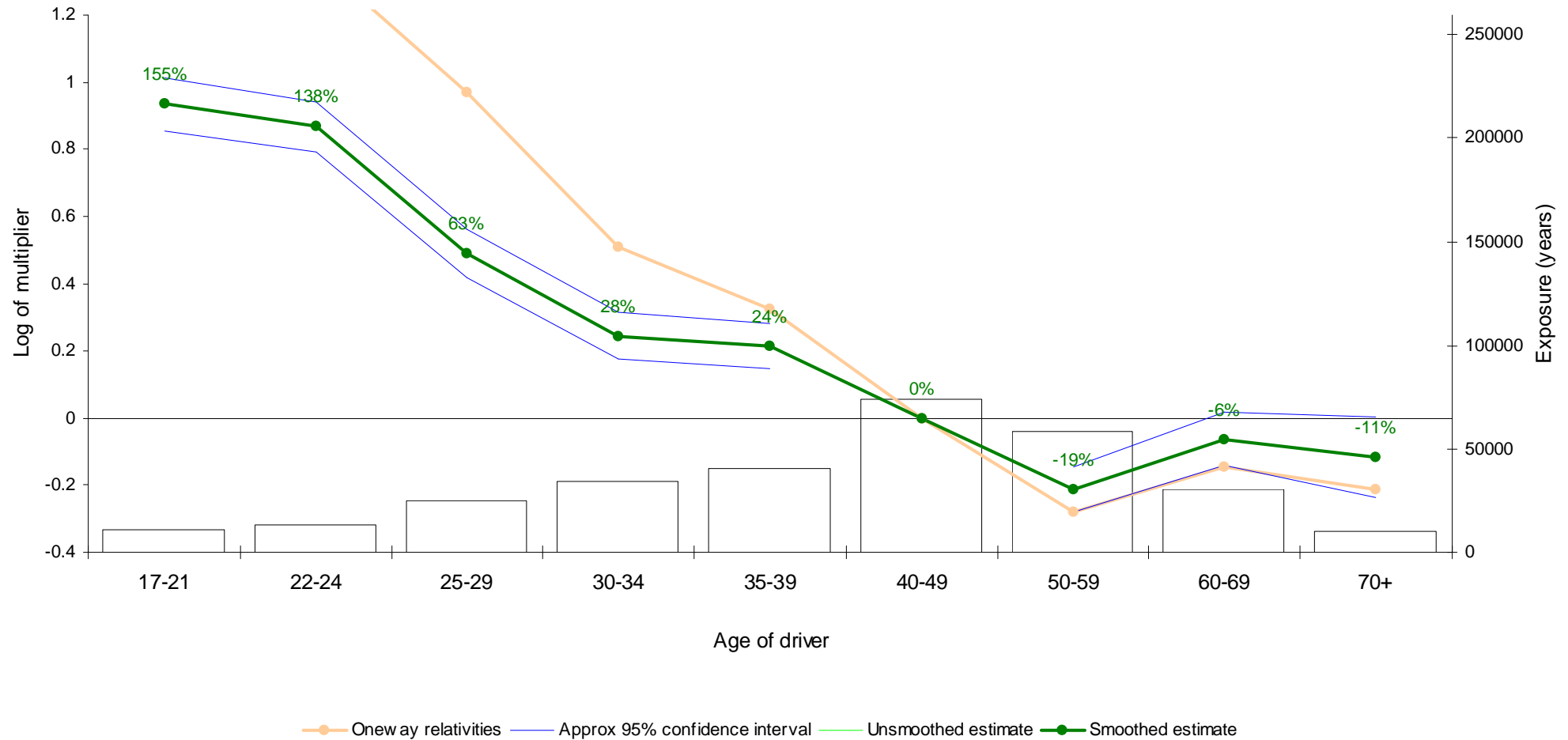
Run 5 Model 3 - Small interaction - Third party material damage, Numbers



# Marginal interaction: Age effect

## Example job

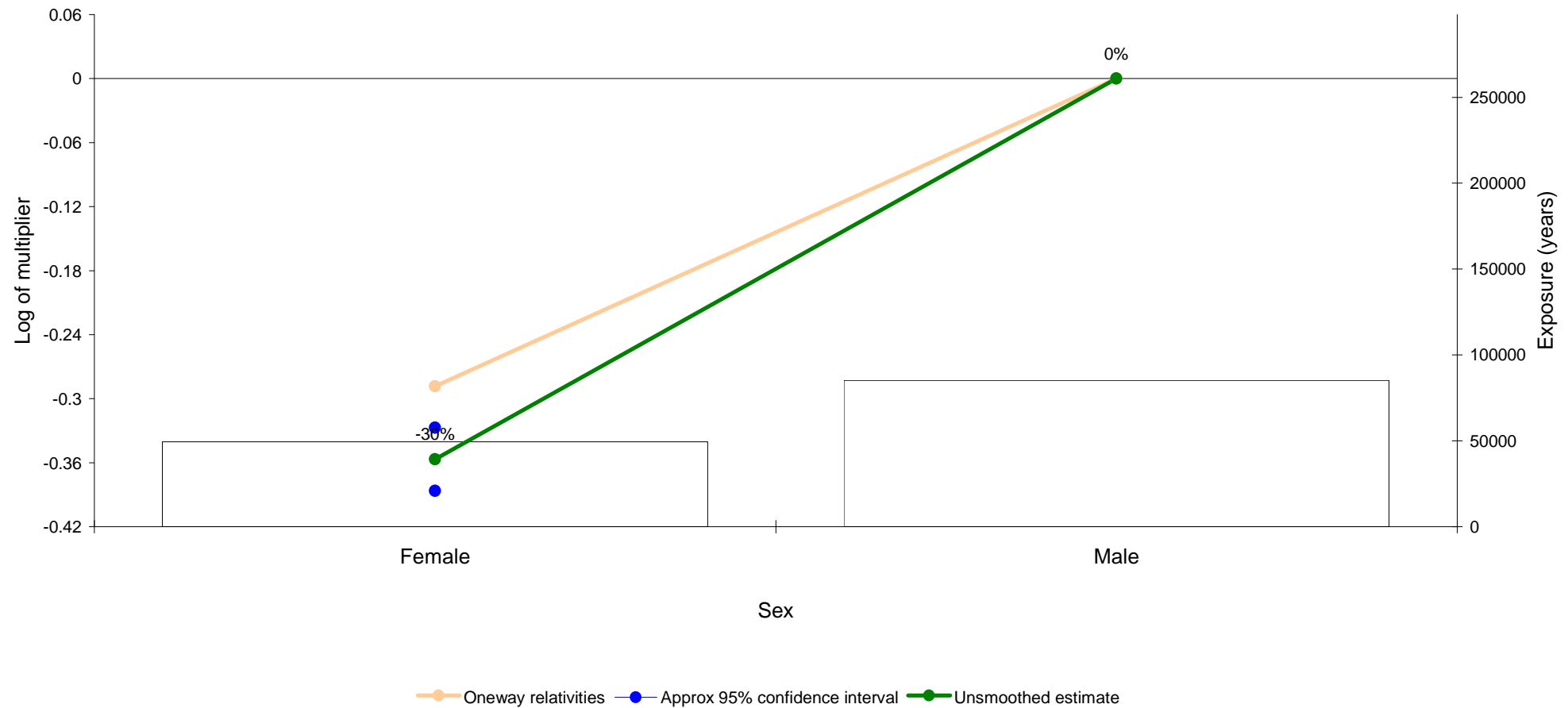
Run 16 Model 3 - Small interaction - Third party material damage, Numbers



# Marginal interaction: Sex effect

## Example job

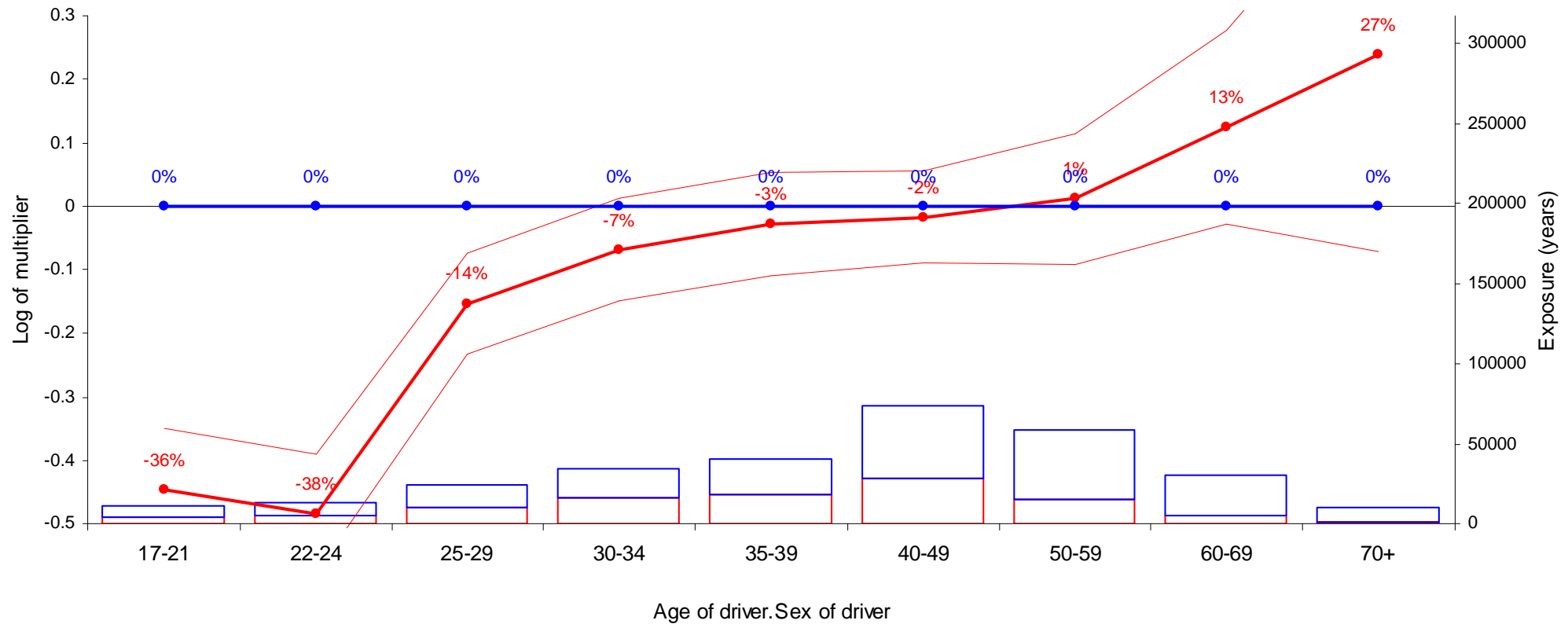
Run 16 Model 3 - Small Interaction - Third Party material damage - Numbers



# Marginal interaction: Age.Sex (ie additional female multipliers)

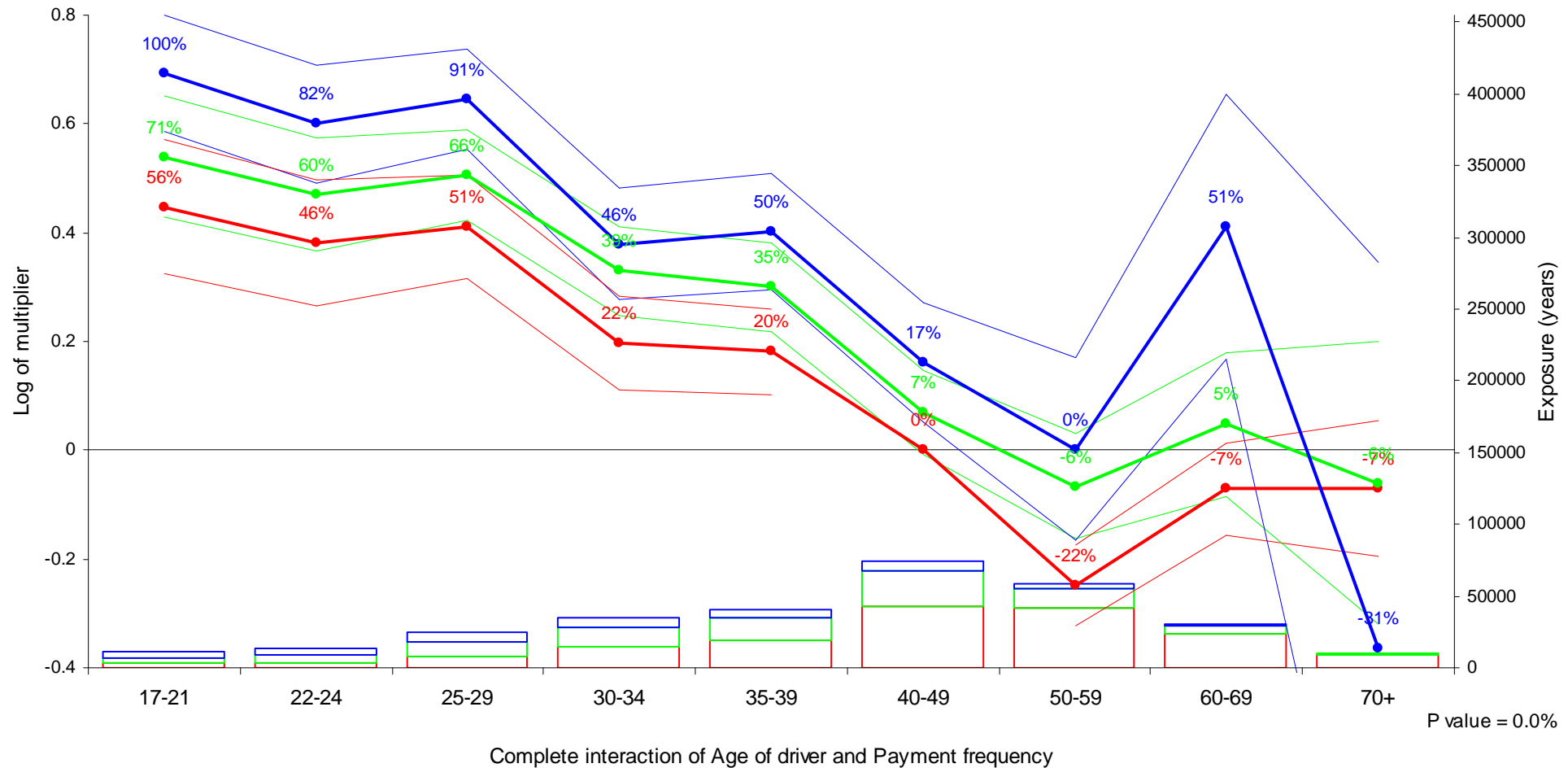
## Example job

Run 16 Model 3 - Small interaction - Third party material damage, Numbers



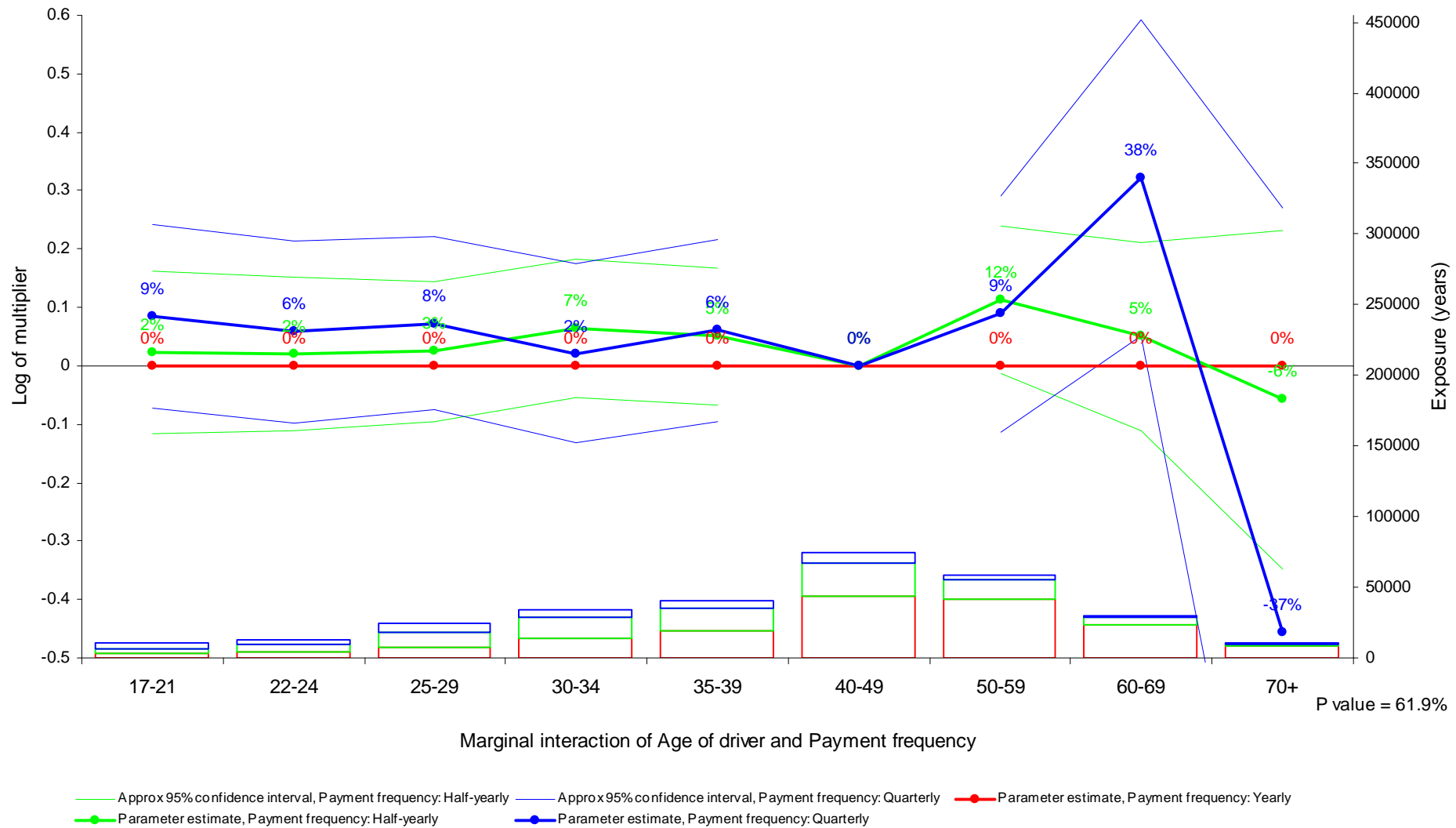
— Approx 95% confidence interval, Sex of driver: Female   
 —● Unsmoothed estimate, Sex of driver: Female   
 — Unsmoothed estimate, Sex of driver: Male  
—● Smoothed estimate, Sex of driver: Female   
 —● Smoothed estimate, Sex of driver: Male

# An example of no interaction (full interaction)



— Approx 95% confidence interval, Payment frequency: Yearly    
 — Approx 95% confidence interval, Payment frequency: Half-yearly    
 — Approx 95% confidence interval, Payment frequency: Quarterly  
● Parameter estimate, Payment frequency: Yearly    
 ● Parameter estimate, Payment frequency: Half-yearly    
 ● Parameter estimate, Payment frequency: Quarterly

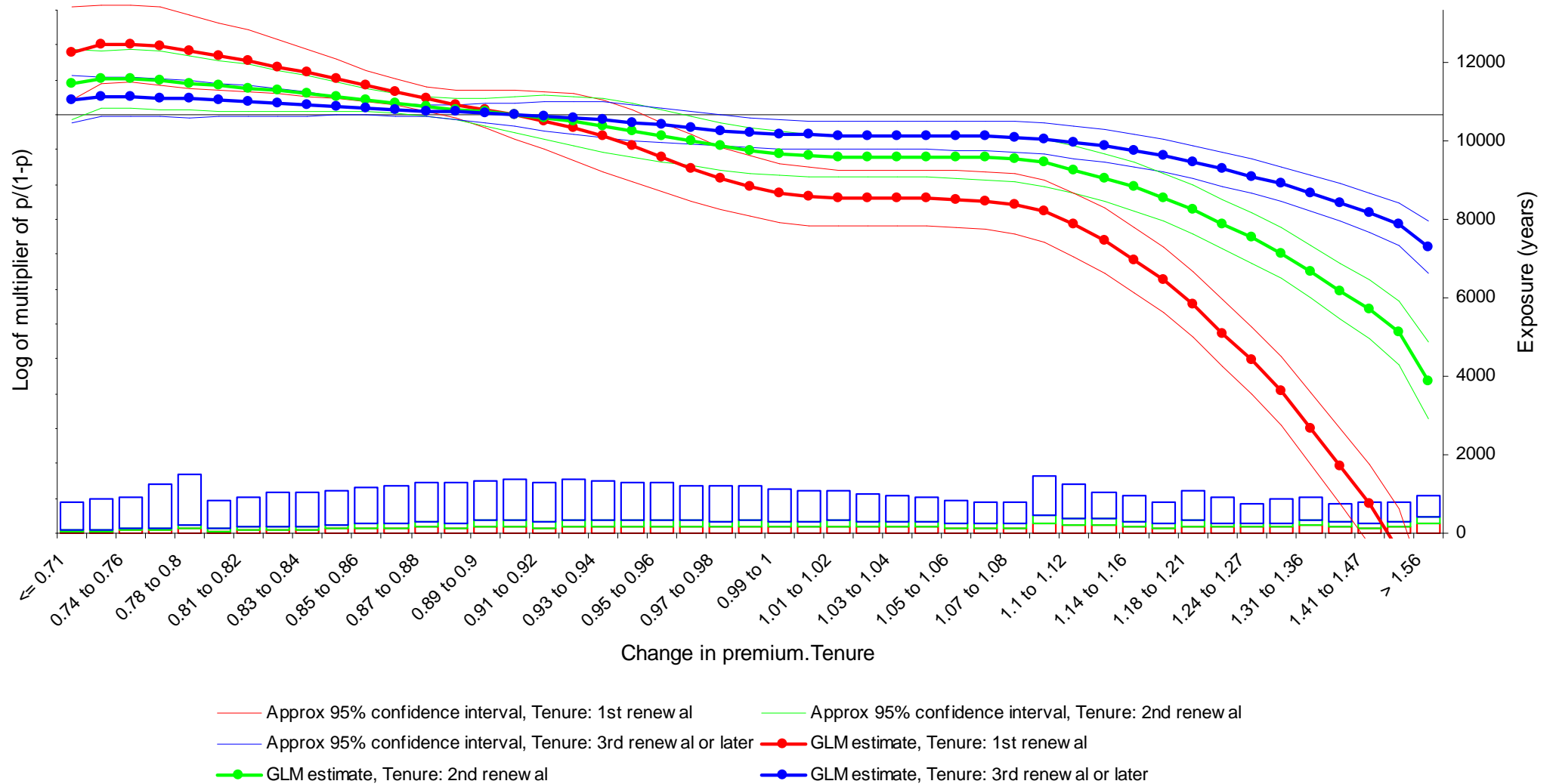
# An example of no interaction (marginal)



# Example interaction - elasticity curve

## Retention analysis

Run 4 Model 2 - Interactions - Retention model



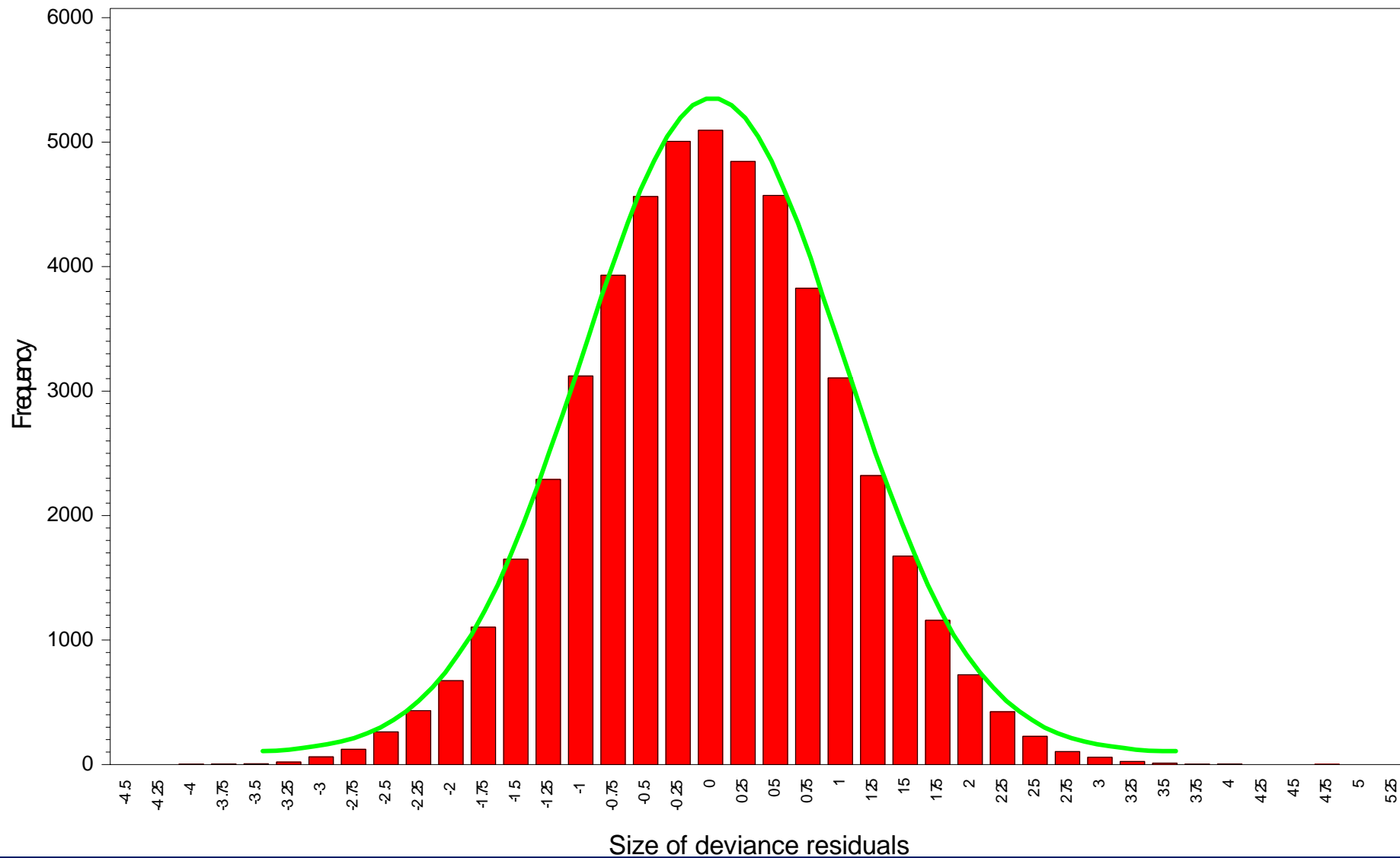
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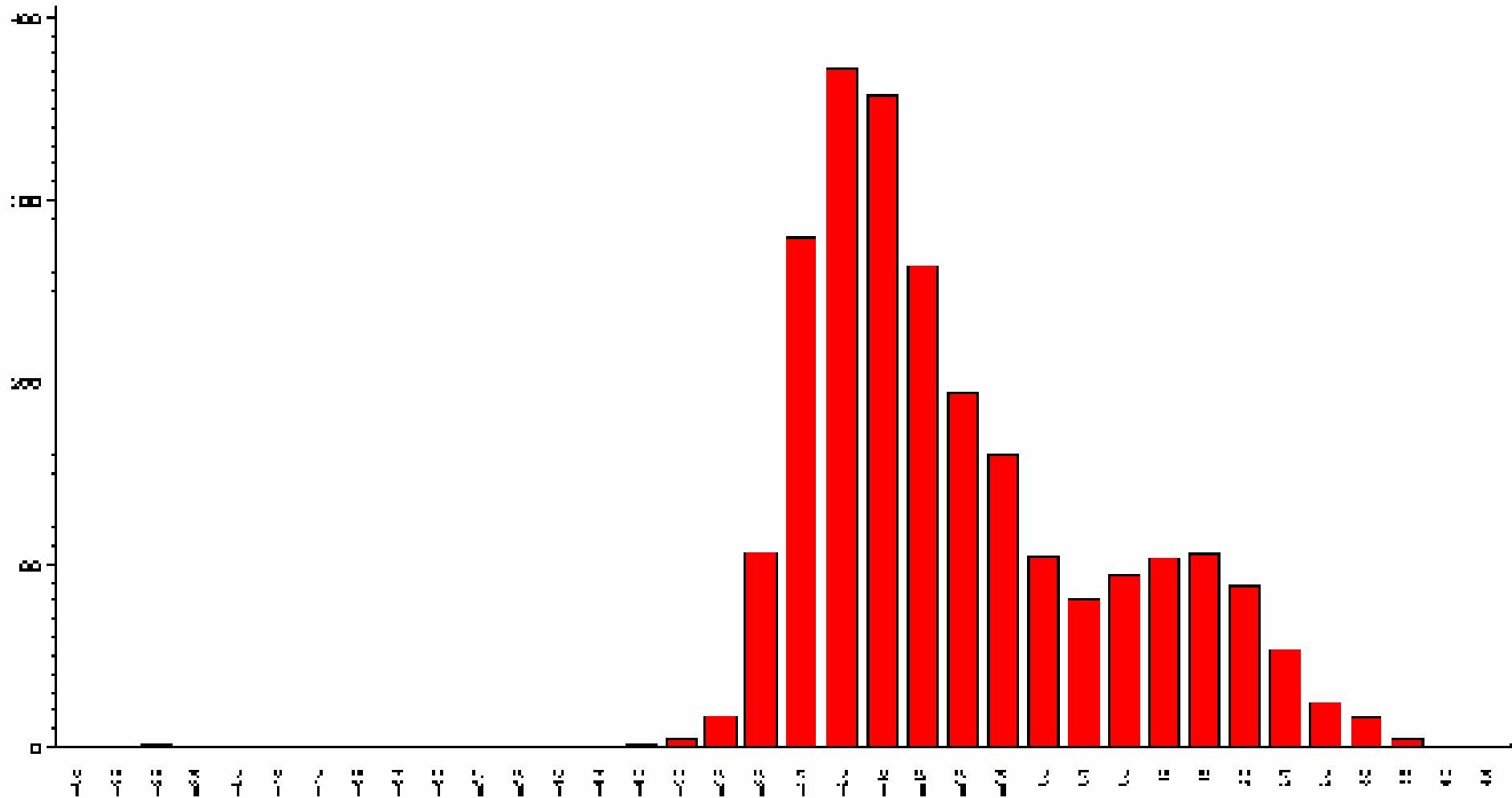


# Residuals

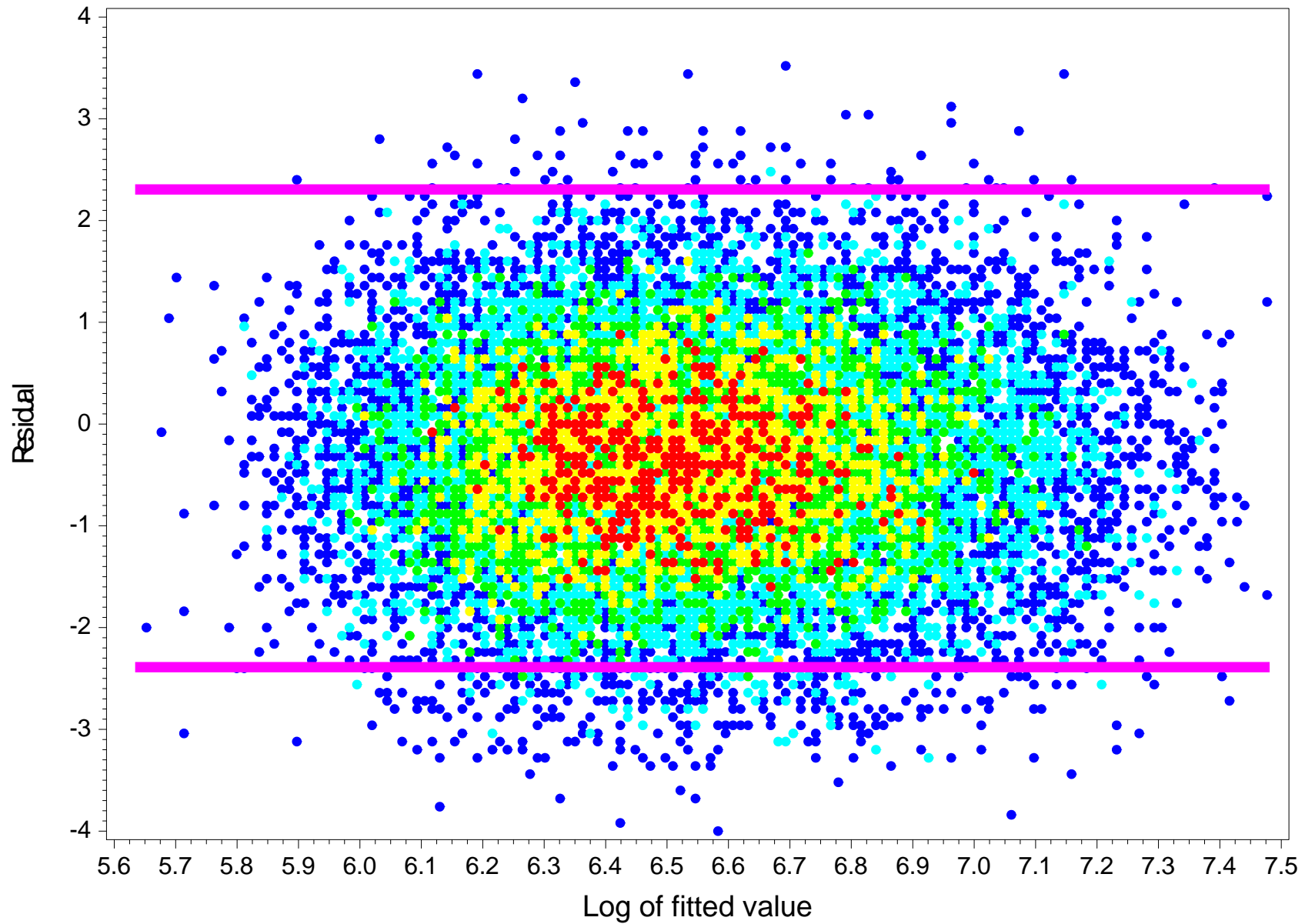
Histogram of Deviance Residuals  
Run 12 (Final models with analysis) Model 8 (AD amounts)



# Residuals – example of bimodality

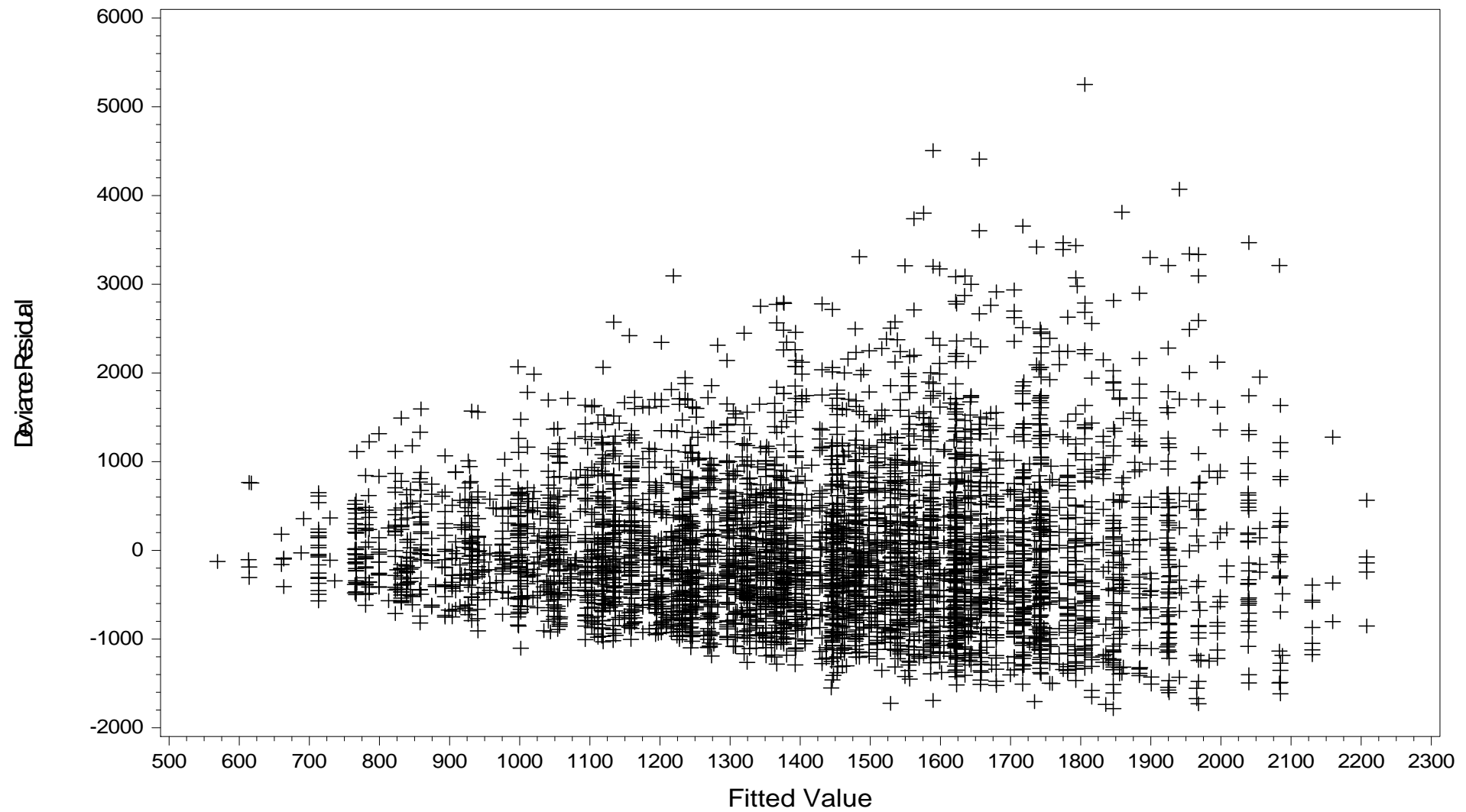


# Residuals



# Gamma data, Normal error

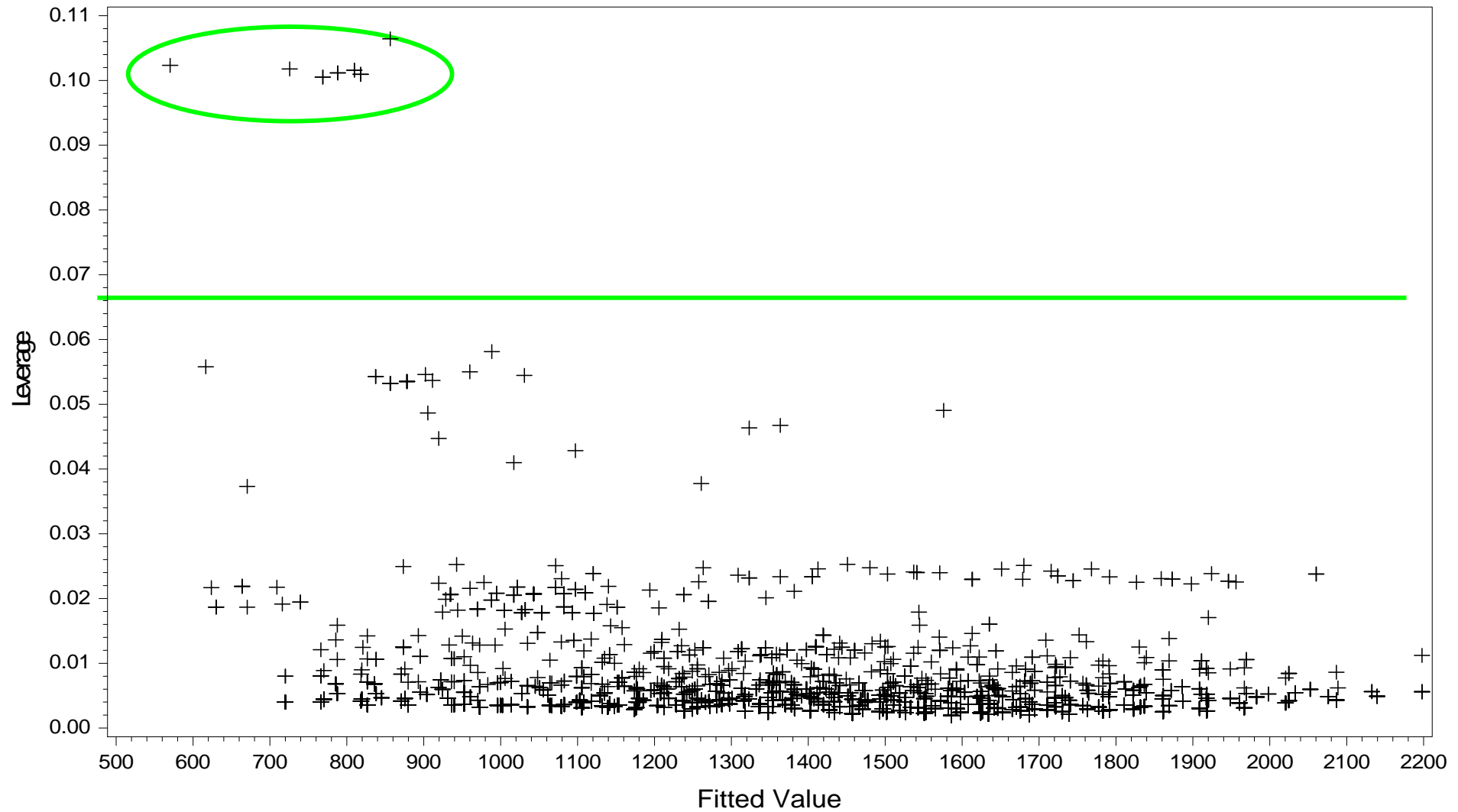
Plot of deviance residual against fitted value  
Run 12 (All claim types, final models, N&A) Model 7 (Own damage, Amounts)



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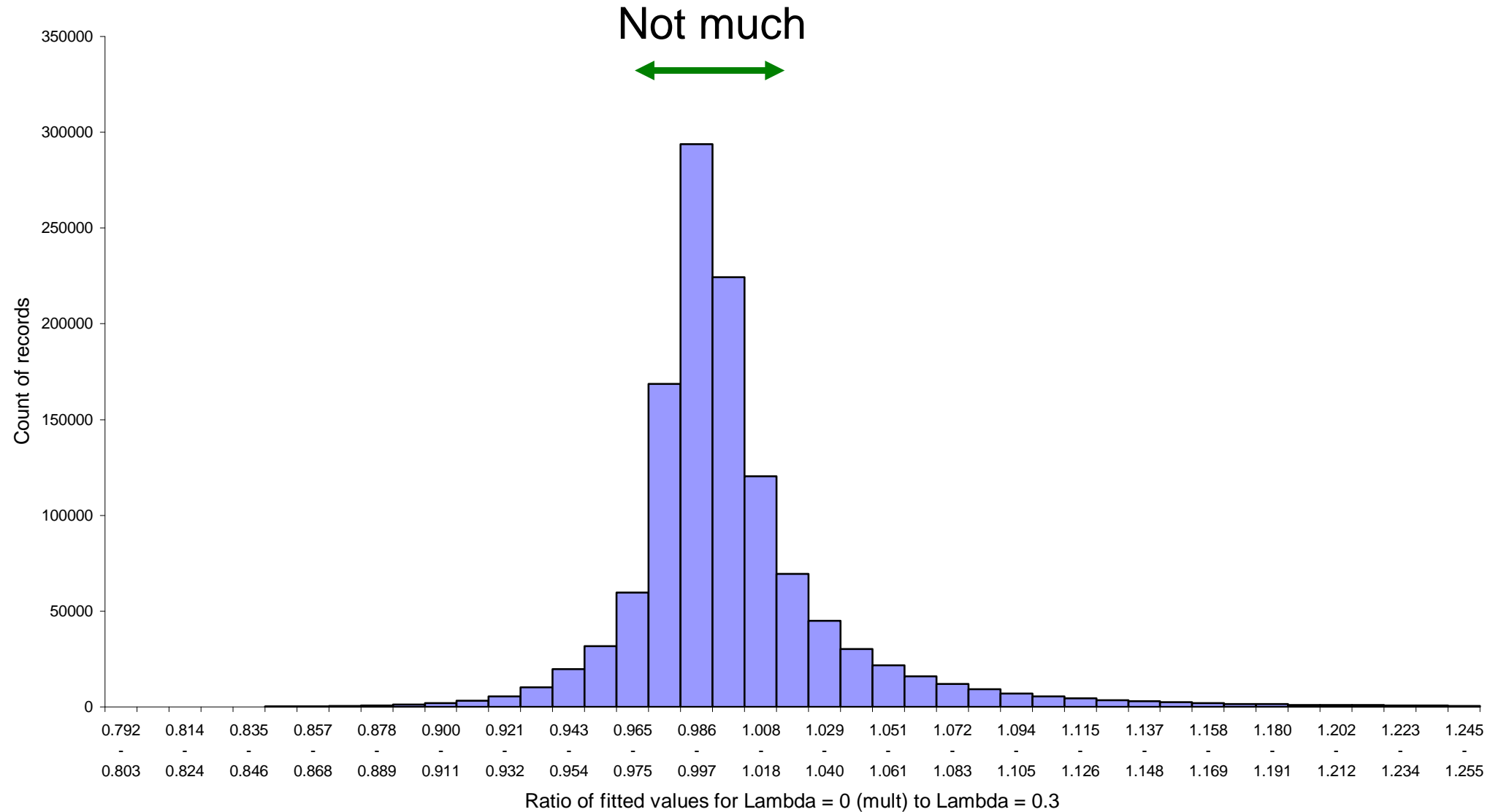
# Leverage

Plot of leverage against fitted value  
Run 12 (All claim types, final models, N&A) Model 6 (Own damage, Amounts)



# Box-Cox link function investigation

## Comparing fitted values of different link functions

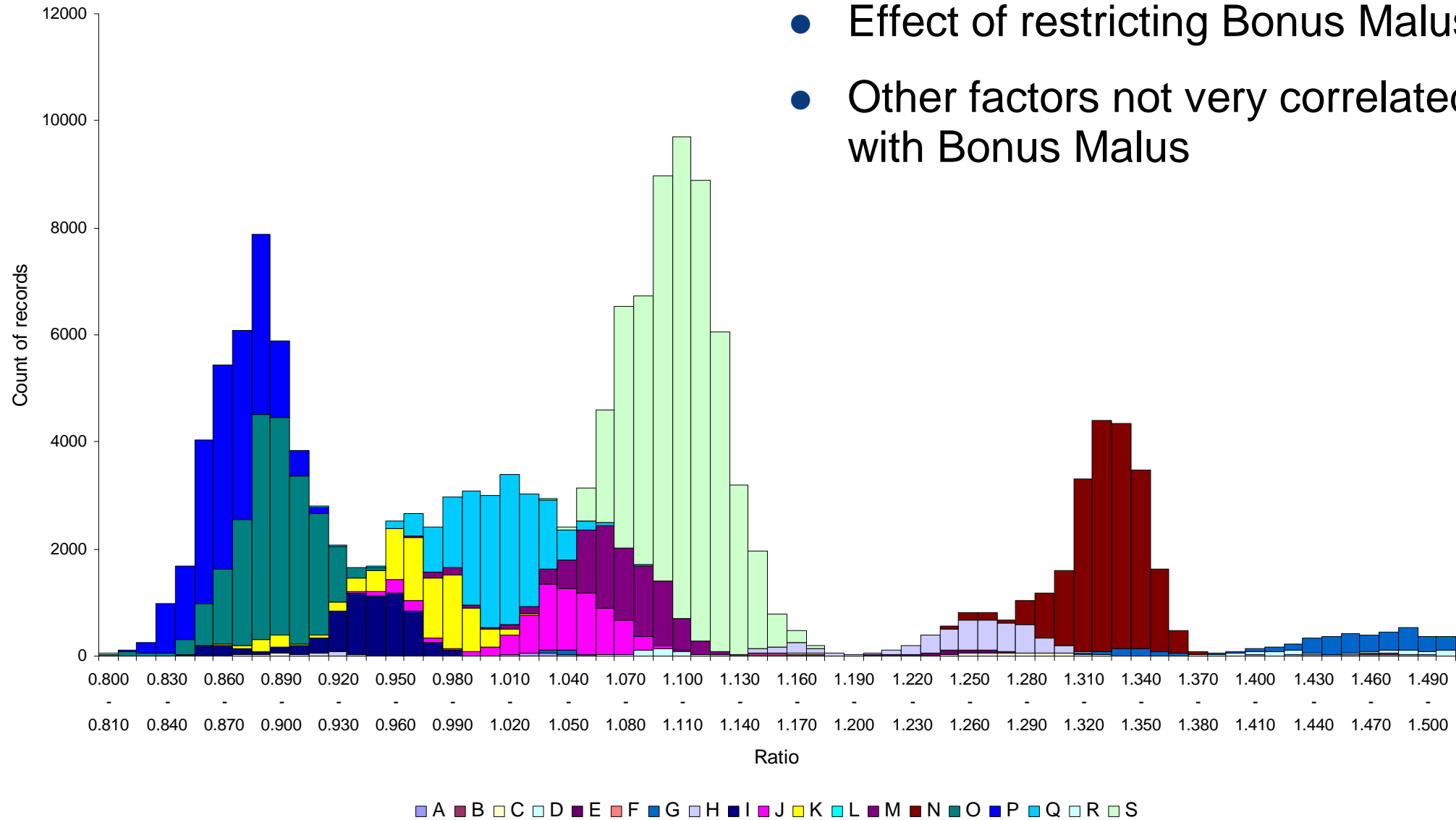


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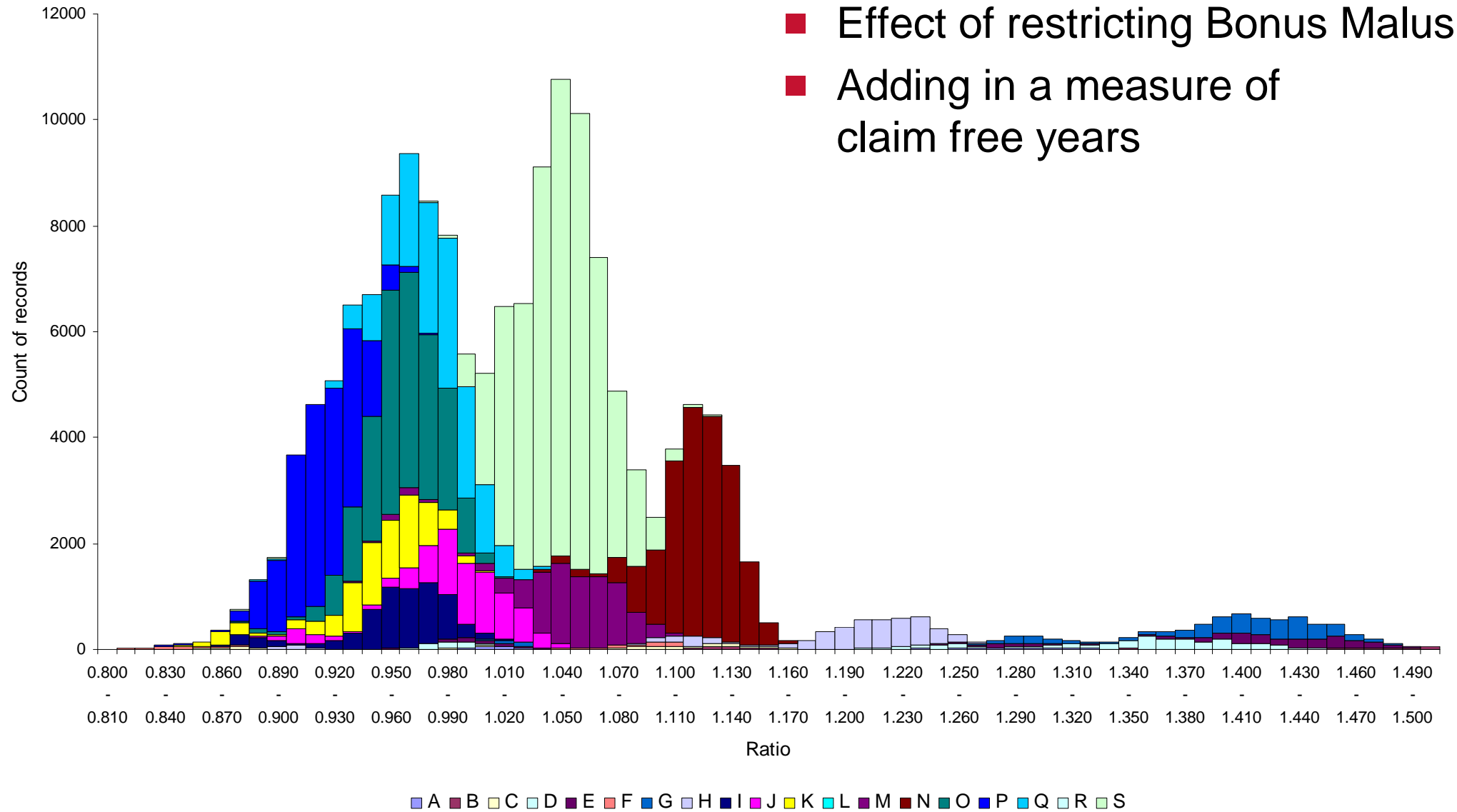
# Testing the effectiveness of restrictions

- Effect of restricting Bonus Malus
- Other factors not very correlated with Bonus Malus





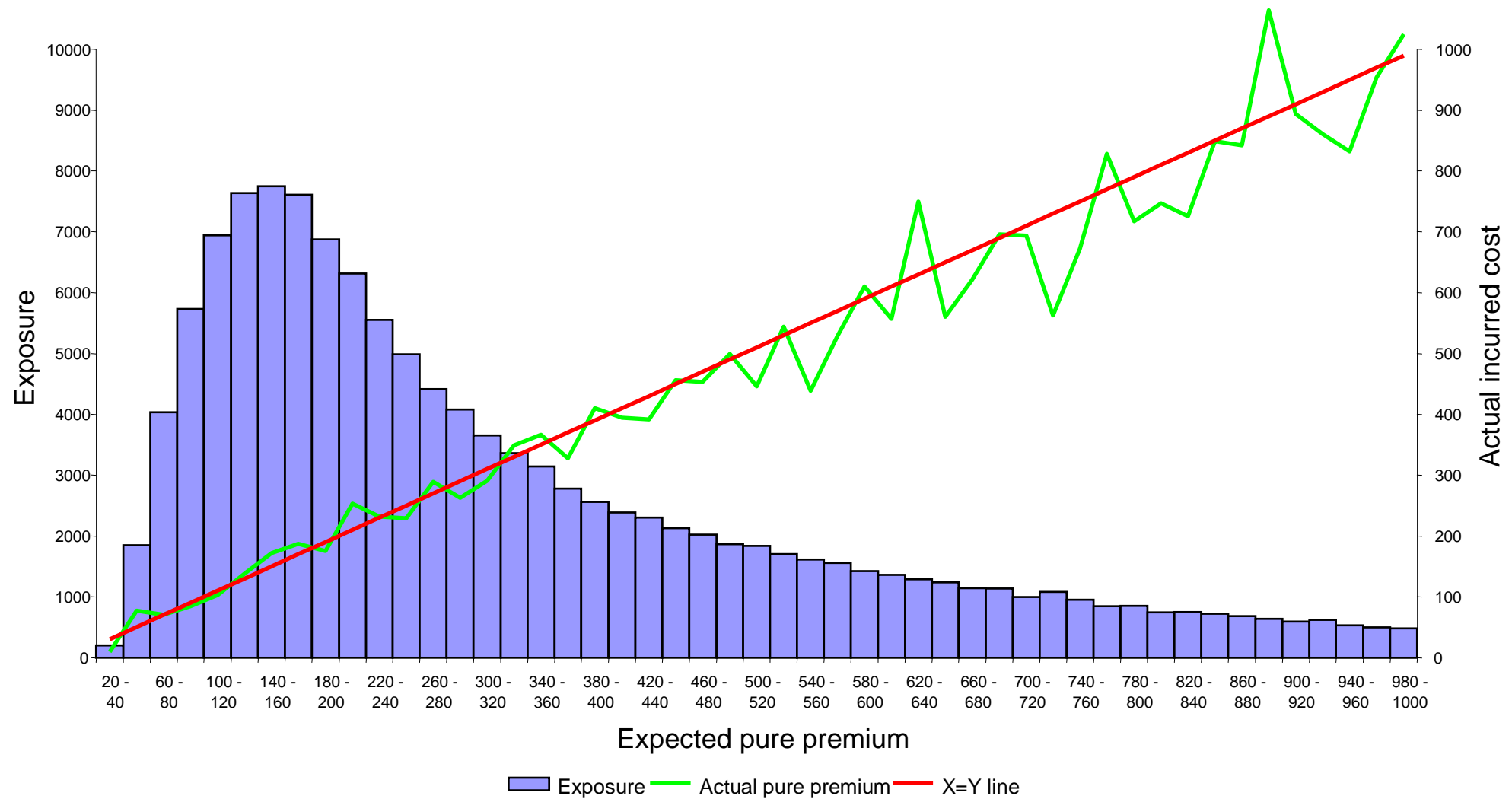
# Testing the effectiveness of restrictions



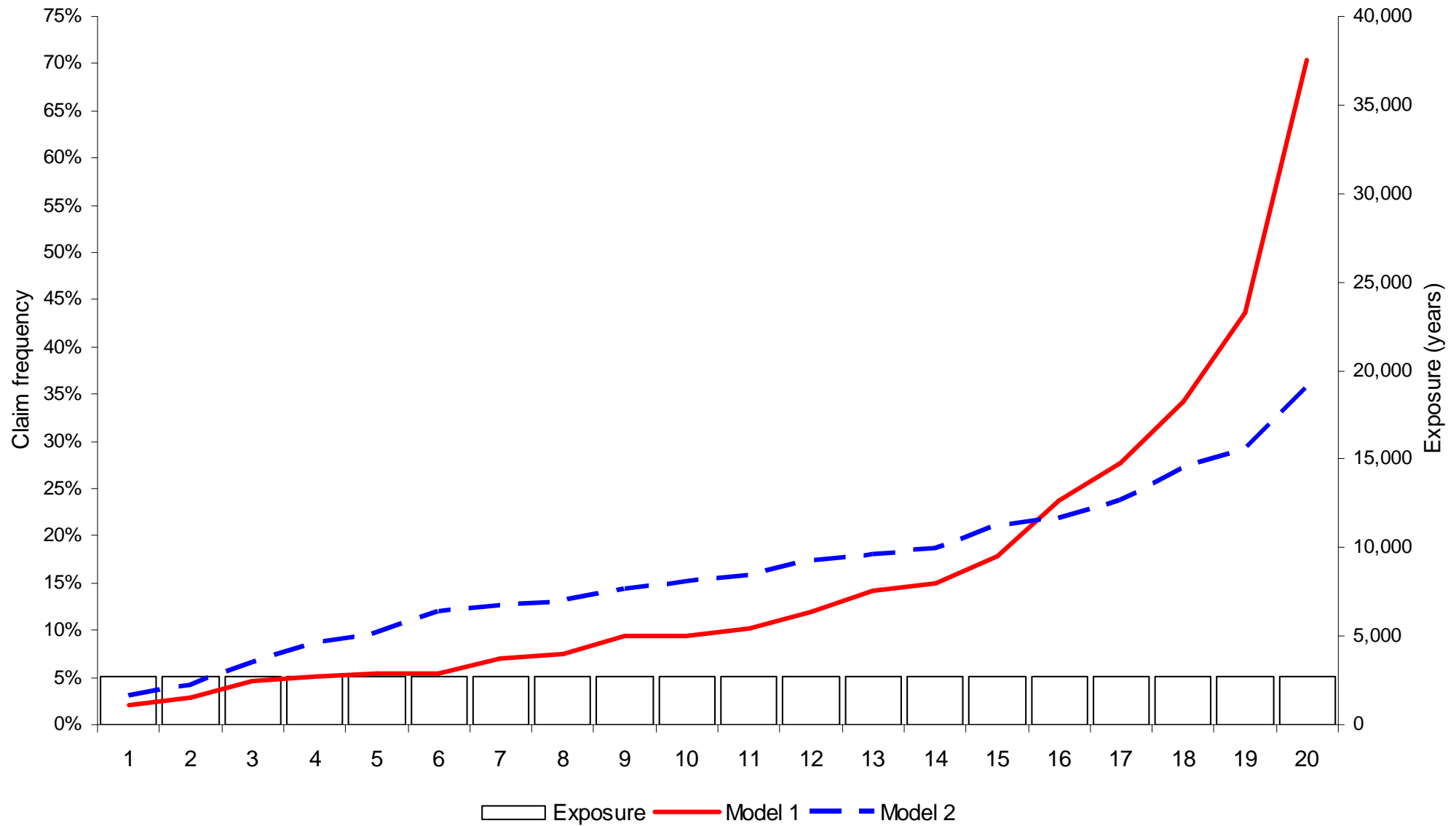
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# Model validation



# Lift curves

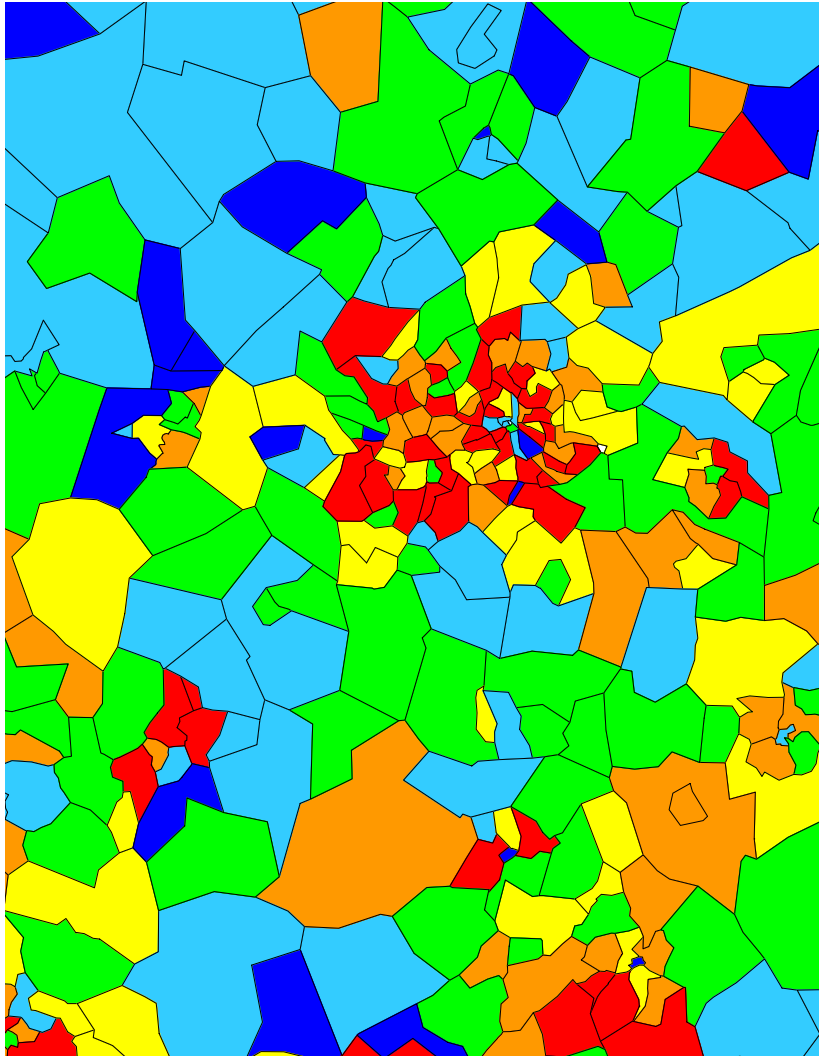


# Technical stories

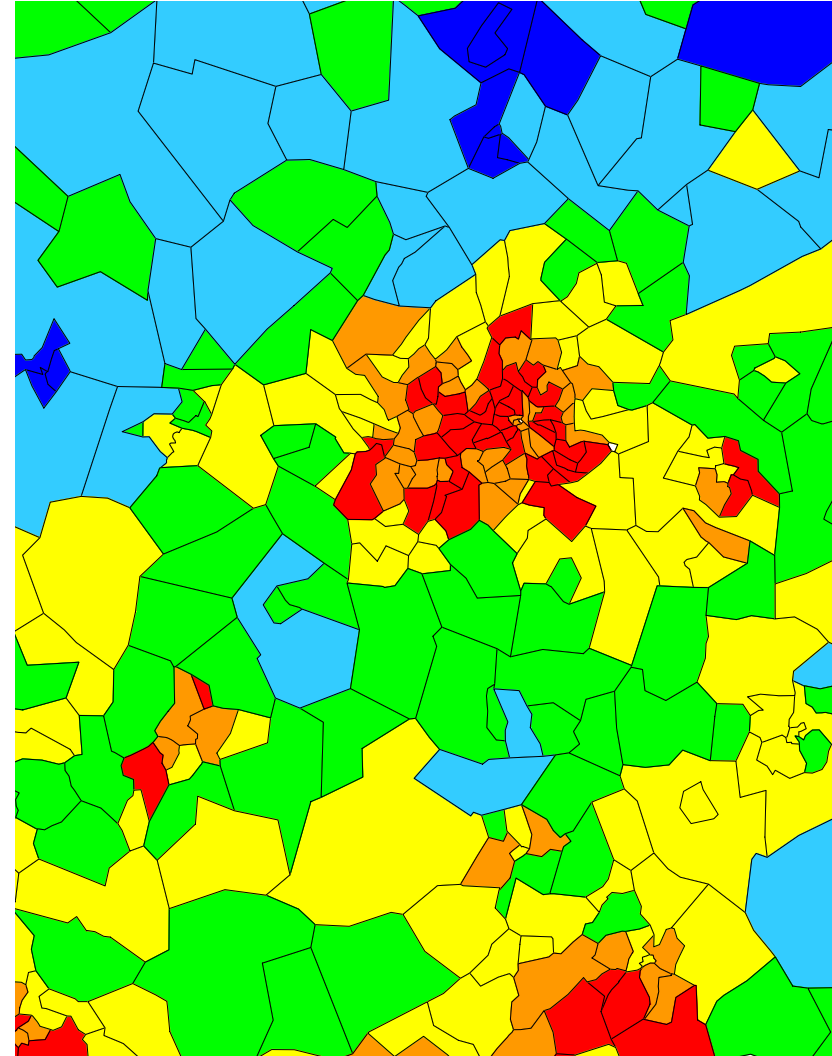
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# Example spatial smoothing results

Unsmoothed residuals



Smoothed residuals



# Comparing indicated results with existing rates and the market

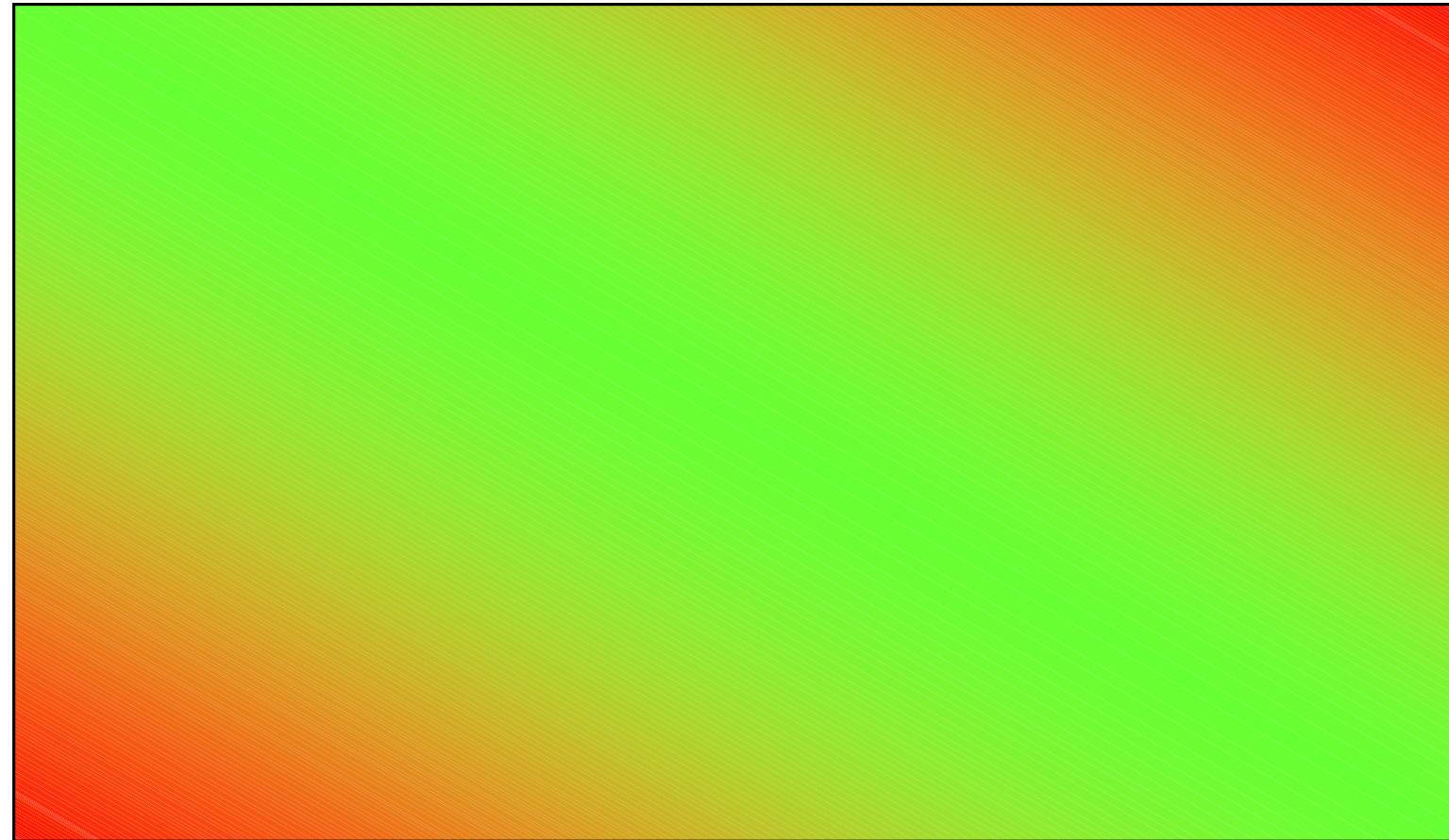
Theoretically desired change in premium

Increase  
Decrease

## Our premium vs market

Below market

Above market



# Comparing indicated results with existing rates and the market

Theoretically desired change in premium

## Our premium vs market

Below market

Above market

Increase

Decrease



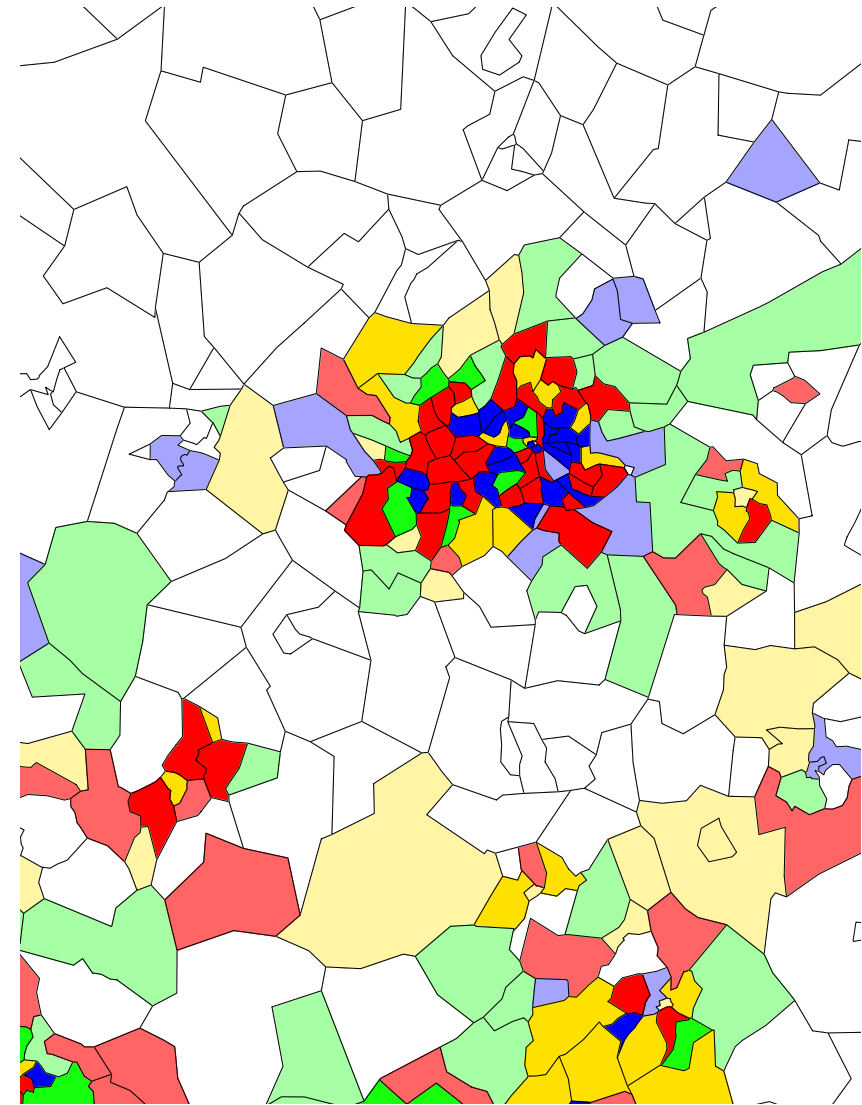
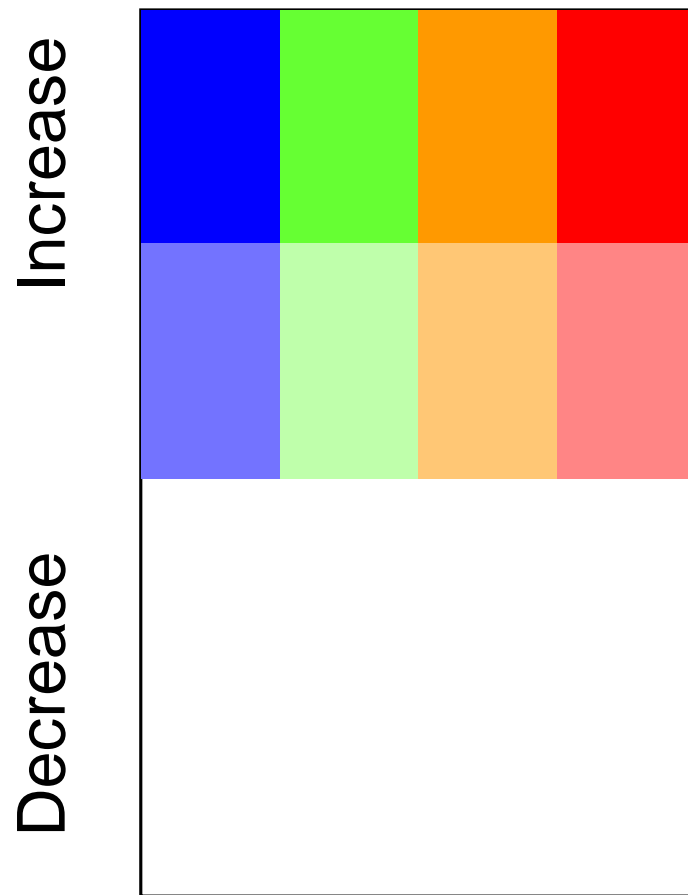


# Comparing indicated results with existing rates and the market

Theoretically desired change in premium

Our premium vs market

Below Above



# Comparing indicated results with existing rates and the market

Theoretically desired change in premium

## Our premium vs market

Below market

Above market

Increase

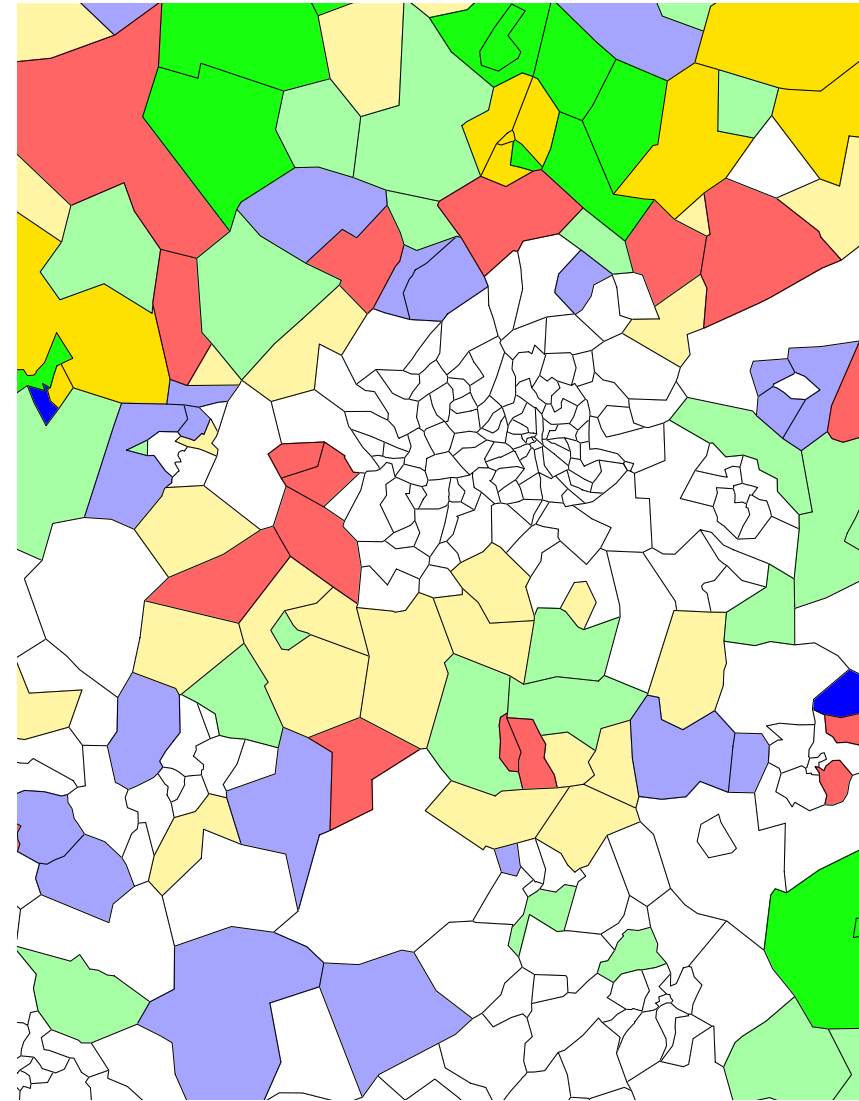
Decrease



# Comparing indicated results with existing rates and the market

Theoretically desired change in premium

Our premium vs market  
Below Above



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- **Monitoring**

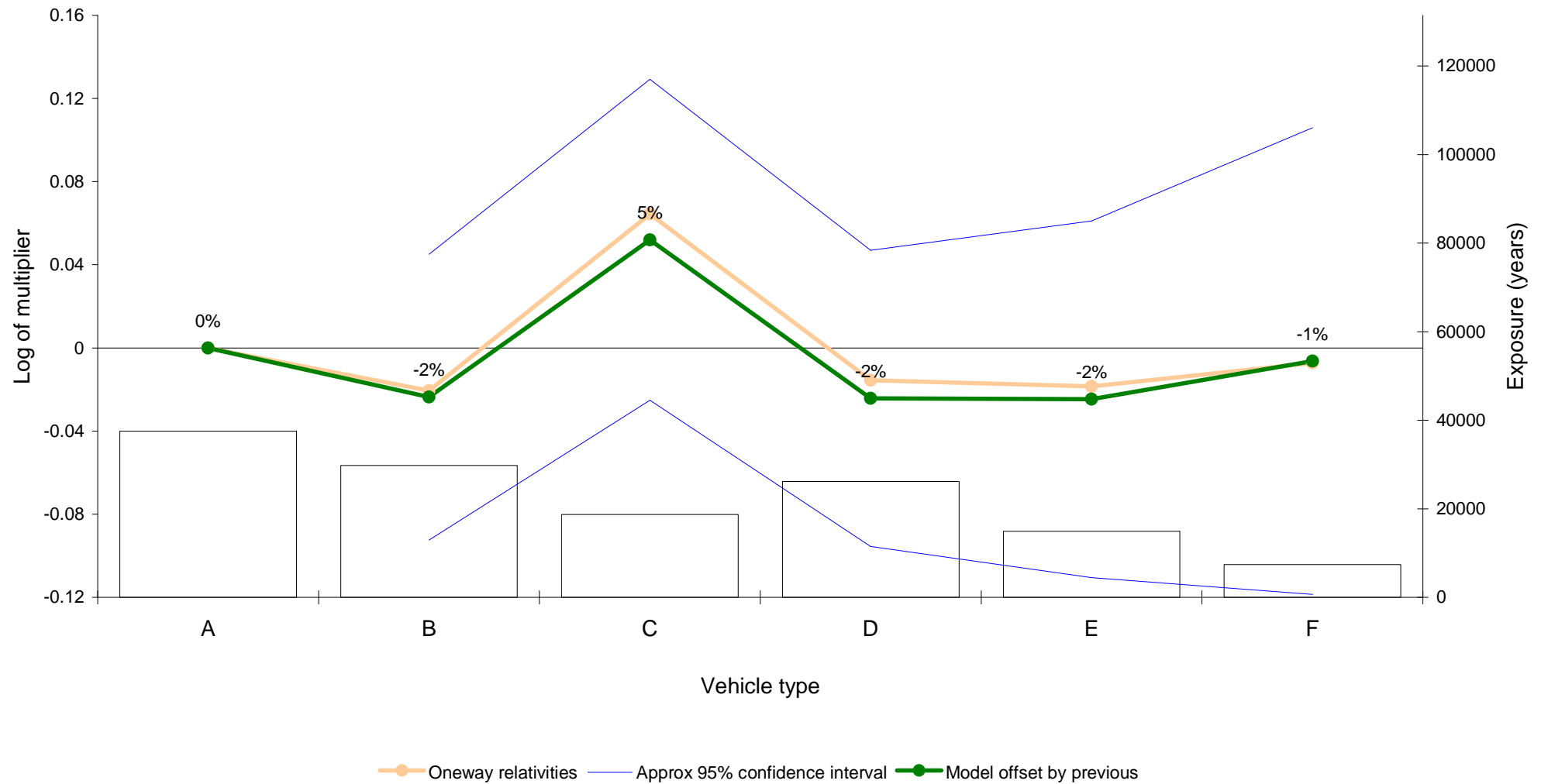
# Monitoring (one-way comparison)

## Benchmark renewal cohort - 6 months after implementation

<u>Age</u>	<u>E(Volume)</u>	<u>Volume</u>	<u>% Difference</u>	<u>E(Freq)</u>	<u>Actual Freq</u>	<u>% Difference</u>	<u>E(Sev)</u>	<u>Actual Sev</u>	<u>% Difference</u>	<u>E(PP)</u>	<u>Actual PP</u>	<u>% Difference</u>
16-20	11,500	11,845	3.0%	12.5%	13.1%	5.0%	3,200	3,213	0.4%	400	422	5.4%
21-24	46,910	45,972	-2.0%	8.9%	8.4%	-6.0%	3,034	3,094	2.0%	270	259	-4.1%
25-29	46,002	47,382	3.0%	6.0%	6.2%	3.0%	3,000	2,982	-0.6%	180	184	2.4%
30-39	55,517	53,296	-4.0%	5.1%	4.8%	-6.0%	2,941	2,990	1.7%	150	143	-4.4%
40-49	51,170	52,193	2.0%	4.8%	4.7%	-3.0%	2,708	2,778	2.6%	130	129	-0.5%
50-59	62,500	61,875	-1.0%	4.6%	4.6%	-1.0%	2,717	2,772	2.0%	125	126	1.0%
60-69	50,940	50,940	0.0%	4.8%	4.8%	0.0%	2,583	2,661	3.0%	124	128	3.0%
70+	44,602	43,709	-2.0%	5.4%	5.3%	-2.0%	3,333	3,278	-1.7%	180	173	-3.6%
	369,140	367,212	-0.5%	5.8%	5.7%	-1.8%	2,896	2,931	1.2%	170	169	-0.7%

## Testing differences over previous analysis

Run 1 Model 2 Bodily Injury



# Communicating modeling results visually

- Stakeholder approach
  - focus on the value of the results
- Technical / actuarial approach
  - tell the story of the model development in a chronological fashion



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## C-6: Communicating Predictive Modeling Results

**CAS Predictive Modeling Seminar  
San Diego, October 6-7, 2008  
Louis Mak FCAS FIAA  
Watson Wyatt Worldwide**

