Property-Liability Insurance Loss Reserve Ranges Based on Economic Value

> Stephen P. D'Arcy, FCAS, PhD Alfred Y. H. Au, Actuarial Student Liang Zhang, Actuarial Student University of Illinois

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### Overview

- Background
  - Loss reserve ranges
  - Economic value of loss reserves
  - Inflation
- Methodology
- Running the model
- Results
- Further research
- Conclusions

# Background

- Traditional loss reserving methods
  - Nominal, undiscounted, for statutory requirements
  - Impacts of inflation on traditional methods

# Background

- Recent Developments
  - ALM
  - FASB & IASC: "Fair Value"
  - CEA: Solvency II
  - S&P criticism

#### Trends in Inflation



## Trends in Inflation

- Increasing oil prices
- Depreciation of the dollar
- Sub-prime mortgage, credit crunch
- Fed lowered discount rate

#### Trends in Inflation



# Methodology

- Loss generation model
- Loss decay model (payment pattern)
- Inflation model
  - Ornstein-Uhlenbeck
  - Masterson Claim Cost Index
- Nominal interest rate model
  - 2 factor Hull-White
- Fixed claim model
  - D'Arcy & Gorvett

# Loss Generation Model

- Nominal values:
  - Normally generated losses compounded by the nominal interest rate
- Economic values:
  - Nominal losses discounted by the inflation rate

#### Fixed Claim Model

FIXED CLAIM MODEL FORMULA FOR "FIXED" COSTS  $f(x) = k + (1-k-m)(t/T)^n$ k = 0.15, m = 0.5, n = 1



Portion of Payment Period (t/T)

# Fixed Claim Model

- Discrete approximation of continuous function
- Impact of inflation on fixed claim model

# Running the Model

http://www.business.uiuc.edu/~s-darcy/papers/LossReserveRangeModelv2.xls

- Input Sheet
- Loss Generator
- Nominal Interest Rate
- Inflation
- Inflation under Fixed Claim
- Fixed Claim Model
- Summary
- Masterson Claim Cost Index

# Input Sheet

Loss Model Parameters	
No. of Claims	1000
Loss Distribution	Lognormal
Mean	1000
Standard Deviation	500
Settlement type	Decay Model
Settlement (years)	10
Hull-White 2-Factor Nominal Interest Rate Mode	el Parameters
Short-Term Mean-Reversion Speed	0.06
Current Short-Term Rate	2.12%
Short-Term Volatility	1.55%
Long-Term Mean-Reversion Speed	0.07
Long-Term Mean	6.69%
Long-Term Volatility	0.96%
Ornstein-Uhlenbeck Inflation Rate Model Param	eters
Mean-Reversion Speed	0.23
Long-Term Mean	4.12%
Current Short-Term Rate	3.54%
Volatility	1.90%
Correlation between Nominal Interest Rate and Inflation	45%
Claim Cost Regression Slope	1.60
Claim Cost Regression Intercept	0.00
Simulation	
No. of Simulation Iterations	10000
Time Step	0.083
Decay Model: x(t+1) = (1-a)"x(t)	
Annual Decay Factor	0.5
Fized Claim Model: f(t) = k + (1-k-m)(t/T)*n	
Fixed Portion at time 0 (k)	0.15
Portion unknown until settlement (m)	0.5
Speed of fixed settlement (n)	1
<u>Generate Histogram</u>	×
Due Circulation	
Run Simulation	

#### Loss Generator

1												(	
Loss Ge	nerator							Nominal	Economic				
			Time to	Inflation	Discount	Nominal	Economic	Value	Value				
<u>Claim</u>	Bandom No.	<u>Severity</u>	Settlement	<u>Factor</u>	Factor	<u>Value</u>	<u>Value</u>	Mean	<u>Mean</u>	<b>Claim Settlement Distribution</b>			
i i	0.4381	830.9586	3.6667	1.2703	0.9365	1055.5872	988.5301	1061252	1032696	Decay Model: x(t+1) = (1-a)*x(t),	x(0) = No. o	f Claims	
2	0.8897	1595.4998	1.0000	1.0381	0.9755	1656.2912	1615.7112			а	0.5		
3	0.0269	359.7058	1.5833	1.0682	0.9679	384.2538	371.9190						
4	0.2730	672.5134	0.4167	1.0164	0.9904	683.5443	676.9713			Cumulative Pr	Time	Count	
5	0.2763	675.6815	3.0833	1.2025	0.9464	812.5386	768.9883			0.0000	0.0833	54	
6	0.0818	463.2301	1.6667	1.0747	0.9667	497.8462	481.2892			0.0561	0.1667	54	
7	0.8442	1442.4336	0.7500	1.0282	0.9815	1483.1201	1455.6399			0.1091	0.2500	56	
8	0.5448	943.2253	0.7500	1.0282	0.9815	969.8307	951.8611			0.1591	0.3333	55	
9	0.2735	672.9734	0.6667	1.0249	0.9840	689.7287	678.7073			0.2063	0.4167	59	
10	0.4702	863.4188	1.6667	1.0747	0.9667	927.9400	897.0793			0.2508	0.5000	39	
11	0.1937	594.6111	0.9167	1.0348	0.9773	615.3101	601.3587			0.2929	0.5833	42	
12	0.1593	558.3649	4.5833	1.3948	0.9258	778.8077	721.0074			0.3326	0.6667	43	
13	0.1226	516.5451	3.9167	1.3023	0.9326	672.7219	627.3883			0.3700	0.7500	45	
14	0 3887	782 6413	0.6667	10249	0 9840	802 1271	789 3097			0.4054	0.8333	38	

#### Nominal Interest Rate

	· ·		<b>_</b>		· · ·			· ·	1.5			
Nominal I	Interest Rat	e Generato	<u>)r</u>									
										Correlation W	eights_	
	Short-Term	Long-Term	Hull-White	Hull-White		Cumulative	!					
	Random	Random	Short-Term	Long-Term	Discount	Discount		Correlated		Correlated	0.45	
Time	<u>Z</u>	<u>Z</u>	Nominal Interest Rate	Nominal Interest Rate	Factor	Factor		Random Z		Independent	0.89302855	
0			0.0212	0.0669								
0.0833	0.1359	-1.9551	0.0244	0.0615	0.9980	0.9980		1.1829				
0.1667	-0.1162	-0.1944	0.0271	0.0610	0.9977	0.9957		1.5057				
0.2500	-1.2944	-0.2926	0.0210	0.0602	0.9982	0.9940		-0.5297				
0.3333	1.0519	-0.9875	0.0234	0.0575	0.9981	0.9921		-1.0350				
0.4167	-0.2128	0.0147	0.0202	0.0576	0.9983	0.9904		-1.2206				
0.5000	1.1043	-1.3444	0.0251	0.0539	0.9979	0.9883		0.1589				
0.5833	-0.0566	-1.4798	0.0244	0.0499	0.9980	0.9863		-0.3366				
0.6667	0.8381	-0.6815	0.0279	0.0481	0.9977	0.9840		0.0357				
0.7500	0.4038	-0.0661	0.0312	0.0480	0.9974	0.9815		0.7613				
0.8333	-0.3806	1.3761	0.0275	0.0520	0.9977	0.9792		-1.0885				
0.9167	-1.4776	-0.4073	0.0233	0.0509	0.9981	0.9773		0.7657				
1.0000	0.1953	-0.7562	0.0225	0.0489	0.9981	0.9755		-0.8689				
1.0833	-2.1182	-1.1637	0.0177	0.0458	0.9985	0.9741		1.7445				
1 1667	0 1006	-0.3456	0.0197	0.0450	0.9984	0.9725		0.7249				

# Inflation

Inflation F	<u>late Gener</u>	<u>rator</u>			Increase in
				Cumulative	Cumulative
			Claim Cost	Claim Cost	Claim Cost
	Random	Inflation	Inflation	Inflation	Inflation
<u>Time</u>	<u>Z</u>	<u>Rate</u>	<u>Factor</u>	<u>Factor</u>	<u>Factor</u>
0.0000		0.0354		1	
0.0833	0.4988	0.0409	1.0054	1.0054	0.0054
0.1667	-1.0937	0.0392	1.0052	1.0107	0.0053
0.2500	0.4863	0.0404	1.0054	1.0161	0.0054
0.3333	-0.3208	0.0362	1.0048	1.0211	0.0049
0.4167	-0.6122	0.0303	1.0040	1.0252	0.0041
0.5000	0.1730	0.0318	1.0042	1.0295	0.0043
0.5833	-0.3752	0.0293	1.0039	1.0336	0.0040
0.6667	-0.5383	0.0270	1.0036	1.0373	0.0037
0.7500	1.5781	0.0368	1.0049	1.0424	0.0051
0.8333	-0.1838	0.0333	1.0044	1.0470	0.0046
0.9167	0.6971	0.0388	1.0052	1.0524	0.0054
1.0000	-0.2964	0.0352	1.0047	1.0574	0.0049

### Impact of Inflation on Claims

k	0.15											
m	0.5											
п	1											
	1.0028	1.0064	1.0100	1.0134	1.0164	1.0194	1.0222	1.0249	1.0282	1.0313	1.0348	1.0381
t / T	0.0833	0.1667	0.2500	0.3333	0.4167	0.5000	0.5833	0.6667	0.7500	0.8333	0.9167	1.0000
0.0833	0.3501	0.1750	0.1167	0.0875	0.0700	0.0583	0.0500	0.0438	0.0389	0.0350	0.0318	0.0292
0.1667		0.1760	0.1173	0.0880	0.0704	0.0587	0.0503	0.0440	0.0391	0.0352	0.0320	0.0293
0.2500			0.1179	0.0885	0.0708	0.0590	0.0505	0.0442	0.0393	0.0354	0.0322	0.0295
0.3333				0.0889	0.0711	0.0593	0.0508	0.0445	0.0395	0.0356	0.0323	0.0296
0.4167					0.0715	0.0596	0.0511	0.0447	0.0397	0.0357	0.0325	0.0298
0.5000						0.0598	0.0513	0.0449	0.0399	0.0359	0.0326	0.0299
0.5833							0.0515	0.0450	0.0400	0.0360	0.0328	0.0300
0.6667								0.0452	0.0402	0.0362	0.0329	0.0301
0.7500									0.0403	0.0363	0.0330	0.0303
0.8333										0.0365	0.0332	0.0304
0.9167											0.0333	0.0305
1.0000												0.0307

### Fixed Claim Model

Fixed Clai	<u>im Model: f(t)</u>	<u>) = k + (1-k-m</u>	<u>)(t/T)^n</u>									
k	0.15											
m	0.5											
n	1											
Fixed Porti	on of Claim at f	time t										
t / T	0.0833	0.1667	0.2500	0.3333	0.4167	0.5000	0.5833	0.6667	0.7500	0.8333	0.9167	1.0000
0.0000	0.1500	0.1500	0.1500	0.1500	0.1500	0.1500	0.1500	0.1500	0.1500	0.1500	0.1500	0.1500
0.0833	0.5000	0.3250	0.2667	0.2375	0.2200	0.2083	0.2000	0.1938	0.1889	0.1850	0.1818	0.1792
0.1667		0.5000	0.3833	0.3250	0.2900	0.2667	0.2500	0.2375	0.2278	0.2200	0.2136	0.2083
0.2500			0.5000	0.4125	0.3600	0.3250	0.3000	0.2813	0.2667	0.2550	0.2455	0.2375
0.3333				0.5000	0.4300	0.3833	0.3500	0.3250	0.3056	0.2900	0.2773	0.2667
0.4167					0.5000	0.4417	0.4000	0.3688	0.3444	0.3250	0.3091	0.2958
0.5000						0.5000	0.4500	0.4125	0.3833	0.3600	0.3409	0.3250
0.5833							0.5000	0.4563	0.4222	0.3950	0.3727	0.3542
0.6667								0.5000	0.4611	0.4300	0.4045	0.3833
0.7500									0.5000	0.4650	0.4364	0.4125
0.8333										0.5000	0.4682	0.4417
0.9167											0.5000	0.4708
1.0000												0.5000

# Summary

Summary			
	Delete Run		
Run	Donoto ritari	1	2
Nominal Yalue			
Mean		1051975.894	1063793.761
SD		24747.6774	28823.52596
Min		969136.51	955976.76
5%		1012563.39	1018224.14
25%		1035024.77	1044242.94
75%		1068167.85	1082153.27
95%		1093894.54	1113307.5
Max		1144274.58	1191628.65
50% CI Range		33143.08	37910.33
90% Cl Range		81331.15	95083.36
Economic Yalue			
Mean		1011037.946	1021737.452
SD		25424.31721	29024.89057
Min		914064.1	899359.65
5%		970082.28	974414.89
25%		993713.91	1001955.87
75%		1027731.83	1040576.3
95%		1053385.3	1069878.12
Max		1103185.18	1139477.87
50% Cl Range		34017.92	38620.43
90% Cl Range		83303.02	95463.23
50% Cl Range Ratio		102.64%	101.87%
90% Cl Range Ratio		102.42%	100.40%

## Masterson Claim Cost Index

Masterson Claim Cost In		
YearlCoverage	CPI All Items	Auto BI
1995	2.73%	4.84%
1996	3.04%	3.89%
1997	1.57%	3.96%
1998	1.67%	3.90%
1999	2.74%	4.48%
2000	3.73%	5.60%
2001	1.14%	4.43%
2002	2.60%	5.16%
2003	1.93%	4.36%
2004	2.97%	4.11%

# Results

#### Taylor Method vs. D'Arcy-Gorvett Approach



# Results Higher Claim Cost Inflation



# Results

#### Higher Inflation/Interest Rate Correlation



# Results

#### Higher and More Volatile Inflation



# Further Research

- Two factor approach to loss reserving
  - Deflate loss triangle
  - Generate reserve ranges on deflated losses
  - Incorporate inflation variability separately
  - Useful when inflation rate or variability changes
- ALM issues
  - Some companies intentionally mismatch assets and liabilities to pick up yield
  - Mismatching would increase the risk of an increase in inflation

# Summary

- Traditional loss reserving methods do not reflect the economic value of loss reserves
- Economic value ranges can be smaller than the nominal value ranges
- Results are more significant during periods of high inflation rates and increased inflation volatility