



**Fair value of property catastrophe reinsurance contracts**  
Theoretical considerations and a practical approach

Please see disclaimer on page 2 of this presentation

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**Outline**

- Introduction
  - Why we are interested in the fair value of (re)insurance contracts
  - How we define fair value
- A *mark-to-model* valuation framework
- Application to the valuation of property catastrophe reinsurance contracts in insurance-linked security (ILS) funds
- Concluding remarks




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**Introduction**

- Why we are interested in the fair value of (re)insurance contracts
  - Measure the performance of a (re)insurer or insurance-linked securities (ILS) fund, especially at intervals less than a year (e.g., weekly or monthly)
  - Share subscription/redemption for open-end ILS funds




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**Challenges**

- Two challenges make this problem intellectually interesting and practically important
  - No secondary market trading for most (re)insurance contracts → no observable market price (exception: cat bonds)
  - The commonly adopted approach of earning premium on a straight-line basis does not produce a fair valuation estimate when the underlying risk exhibits systematic seasonal variations (e.g., all weather-related risks)




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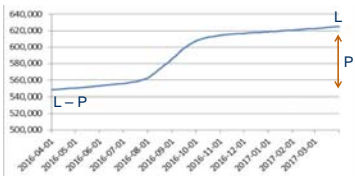
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**Defining fair value (1)**

- Consider a simple reinsurance contract with a limit = L; premium = P
- Intuitively, we know that
  - Without any loss, its value  $V = L$  at expiration
  - Without any loss, its value increases by P during the contract period
  - At inception, its value =  $L - P$
- The question: how does the fair value vary in between?




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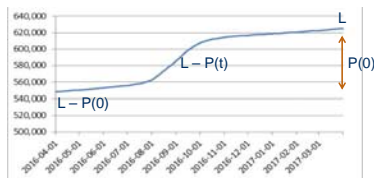
**Defining fair value (2)**

We define the fair value of the contract at a time t as:

$$V(t) = L - P(t)$$

where  $P(t)$  = the premium that the reinsurer must pay a third-party rational reinsurer to assume both

- (a) All losses that have occurred prior to t
- (b) The risk between t and expiration




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**Intuitive interpretation: Scenario 1**

Why does this definition represent the fair value of the contract at a time t?

$$V(t) = L - P(t)$$

where  $P(t)$  = the premium that the reinsurer must pay a third-party rational reinsurer to assume both

- (a) All losses that have occurred prior to t
- (b) The risk starting on t until expiration

- Case 1: the contract experienced a full-limit loss prior to t
- The third-party reinsurer will have to charge precisely L to assume (a) and (b) above  $\rightarrow V(t) = L - L = 0$
  - Consistent with the fact that the contract is "worthless" after a full-limit loss




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**Intuitive interpretation: Scenario 2**

Why does this definition represent the fair value of the contract at a time t?

$$V(t) = L - P(t)$$

where  $P(t)$  = the premium that the reinsurer must pay a third-party rational reinsurer to assume both

- (a) All losses that have occurred prior to t
- (b) The risk starting on t until expiration

- Case 2: A full-year contract (1/1/2016 – 12/31/2016) covers US hurricane only. What is its value on 4/1/2016? Suppose the market has not hardened or softened relative to 1/1/2016
- $P(t) = P(0) \rightarrow V(t) = L - P(0) = V(0)$
  - This is consistent with the fact that the contract has gained no value since no risk has been assumed as of 4/1/2016




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**Intuitive interpretation: Scenario 3**

Why does this definition represent the fair value of the contract at a time t?

$$V(t) = L - P(t)$$

where P(t) = the premium that the reinsurer must pay a third-party rational reinsurer to assume both

- (a) All losses that have occurred prior to t
- (b) The risk starting on t until expiration

Case 3: A full-year contract (1/1/2016 – 12/31/2016) covers US hurricane only. What is its value on 4/1/2016? Suppose the same risk now costs twice as much to reinsure as it did on 1/1 due to a massive loss event elsewhere.

- $P(t) = 2 \times P(0) \rightarrow V(t) = L - 2 \times P(0) < V(0)$
- This is equivalent to ↓value of a bond in an ↑interest rate environment even without any change of its own credit quality




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**Implementation**

- $V(t) = L - P(t)$ , where  $P(t) = P1(t) + P2(t) \times M(t)$

P1(t) = to account for losses that had occurred prior to t; there is generally uncertainty in the estimate (i.e., loss development risk)

P2(t) = the premium to cover the forward-looking risk between t and expiration (e.g., due to erosion of limit and aggregate deductible; seasonal pattern of the underlying risk)

M(t) = a modification factor to take into account market hardening/softening

- Ideally, the inputs used to calculate P(t) should be
  - Based on objectively observed parameters
  - Free from subjective judgments that vary idiosyncratically for different transactions




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**Application to property catastrophe reinsurance ILS funds (1)**

- Reasonably objective and observable parameters are available for the calculation of P(t) for property catastrophe reinsurance contracts in ILS funds




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**Application to property catastrophe reinsurance ILS funds (2)**

•  $V(t) = L - P(t)$ , where  $P(t) = P1(t) + P2(t) \times M(t)$

$P1(t)$  = reported losses that had occurred prior to  $t$

Assumption: the amount of losses that had occurred prior to  $t$  is treated as a deterministic number. This is a reasonable choice for ILS funds because loss-impacted contracts are generally excluded from the calculations related to redemption/subscription (known as *side-pocketed*) until the uncertainty is removed




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**Application to property catastrophe reinsurance ILS funds (3)**

•  $V(t) = L - P(t)$ , where  $P(t) = P1(t) + P2(t) \times M(t)$

$P2(t) = EL(t) \times P(0) / EL(0)$

$EL(0)$  = model-calculated expected loss of the contract calculated at the inception of the contract

$P(0)$  = actual premium for the contract

$EL(t)$  = model-calculated expected loss of the contract at the time  $t$

Assumption: without a systematic hardening/softening, the market demands a constant premium/EL ratio for a specific contract

Alternative assumptions: the market demands constant Sharpe Ratio or other risk/return measures




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**Application to property catastrophe reinsurance ILS funds (4)**

•  $V(t) = L - P(t)$ , where  $P(t) = P1(t) + P2(t) \times M(t)$

If the contract term is less than one year,  $M(t) = 1$

Otherwise  $M(t)$  is to be determined by the premium/EL ratio of similar contracts incepting at  $t$

Assumptions:

- Systematic market conditions do not change significantly within a year;
- Comparable contracts can be found in the market to estimate  $M(t)$




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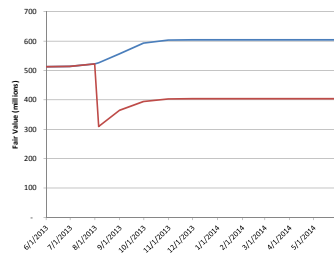
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**Example 1**

- Excess-of-loss contract
  - US hurricane risk only
  - Limit = 604mm
  - Premium = 91mm
- Scenario 1: no loss
- Scenario 2: 200mm loss on Aug 1<sup>st</sup>; no other loss




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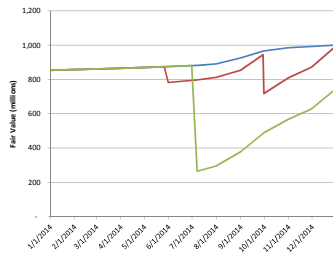
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**Example 2**

- Aggregate stop-loss contract
  - World-wide cat
  - Limit = 1bn
  - Premium = 150mm
- Scenario 1: no loss
- Scenario 2: greater-than-expected deductible erosions reported on May 31<sup>st</sup> and Sept 30<sup>th</sup>; aggregate loss never exceeded AAD
- Scenario 3: loss in excess of AAD reported on July 7<sup>th</sup> and Dec 31<sup>st</sup>




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**Concluding remarks**

- For the purpose of ILS fund performance reporting and share subscription/redemption, we must establish the fair value of catastrophe reinsurance contracts in the absence of secondary market trades
- We have presented
  - A general “mark-to-model” framework applicable to most reinsurance contracts
  - A set of assumptions and rules to implement the framework for property catastrophe reinsurance contracts in ILS funds, enabling an ILS fund and/or fund administrator to establish a reasonably accurate and unbiased estimate of the fair value of a contract at any given time primarily based on observed and objectively calculated inputs
- Expanding the application to a broader subset of the (re)insurance business is an intellectually interesting and challenging problem. A solution will be extremely useful in practice




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